

Evolution of dark matter structures

- 1) substructure
- 2) density profiles

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Aug 27, 2007

TeV particle astrophysics, Venice

the “via lactea” simulation

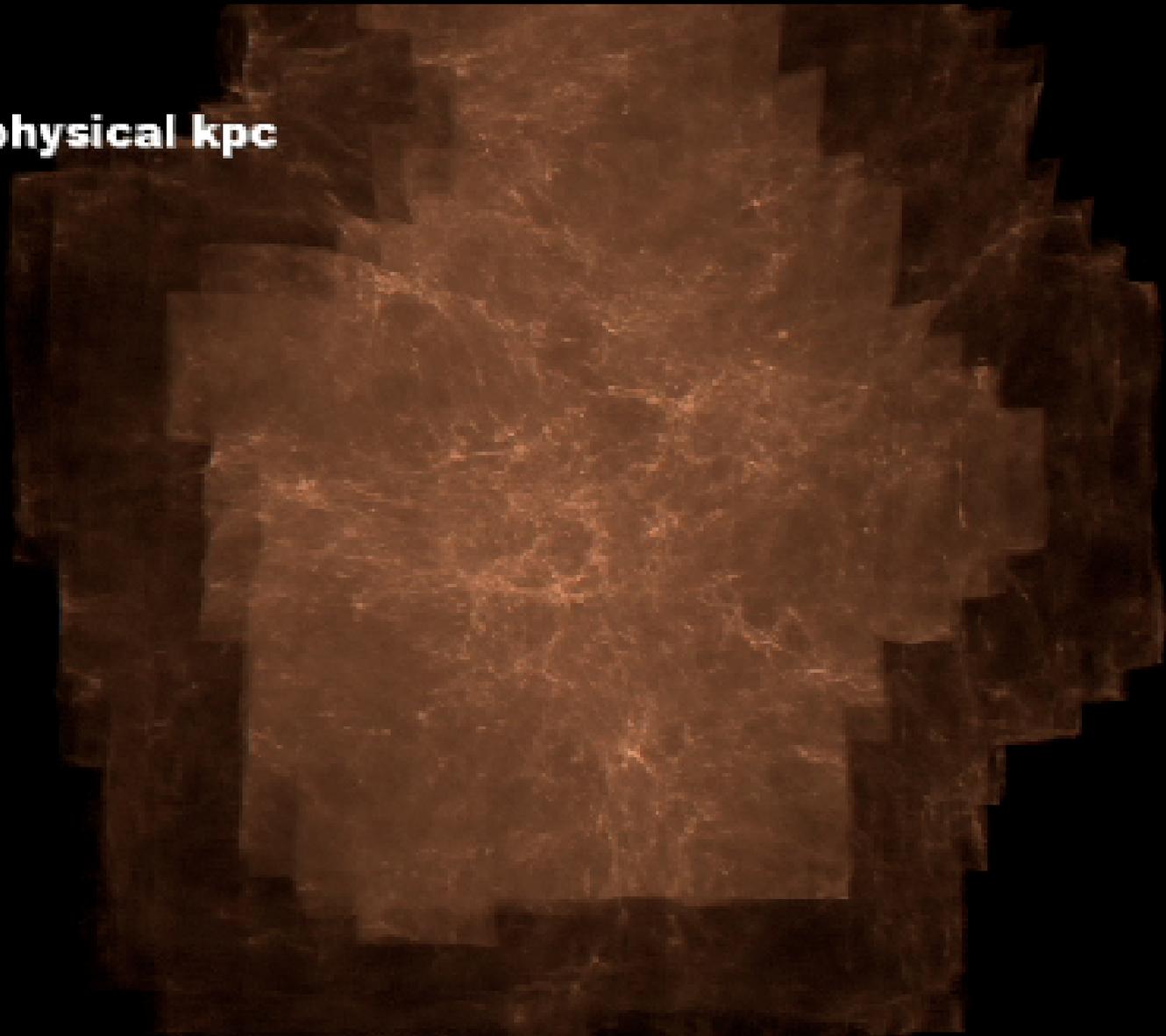
a Milky Way halo simulated with over 200 million particles

- collision-less (no hydro) → accurate solution of an idealized problem
no free parameters, no subgrid physics
- largest DM simulation to date
320,000 cpu-hours on NASA's Project Columbia supercomputer
- 213 million high resolution particles, embedded in a periodic 90 Mpc box
sampled at lower resolution to account for tidal field.
- WMAP (year 3) cosmology:
 $\Omega_m=0.238$, $\Omega_L=0.762$, $H_0=73$ km/s/Mpc, $n_s=0.951$, $\sigma_8=0.74$.
- force resolution: 90 parsec
- time resolution: adaptive time steps as small as 68,500 years
- mass resolution: 20,900 M_\odot



$z=11.9$

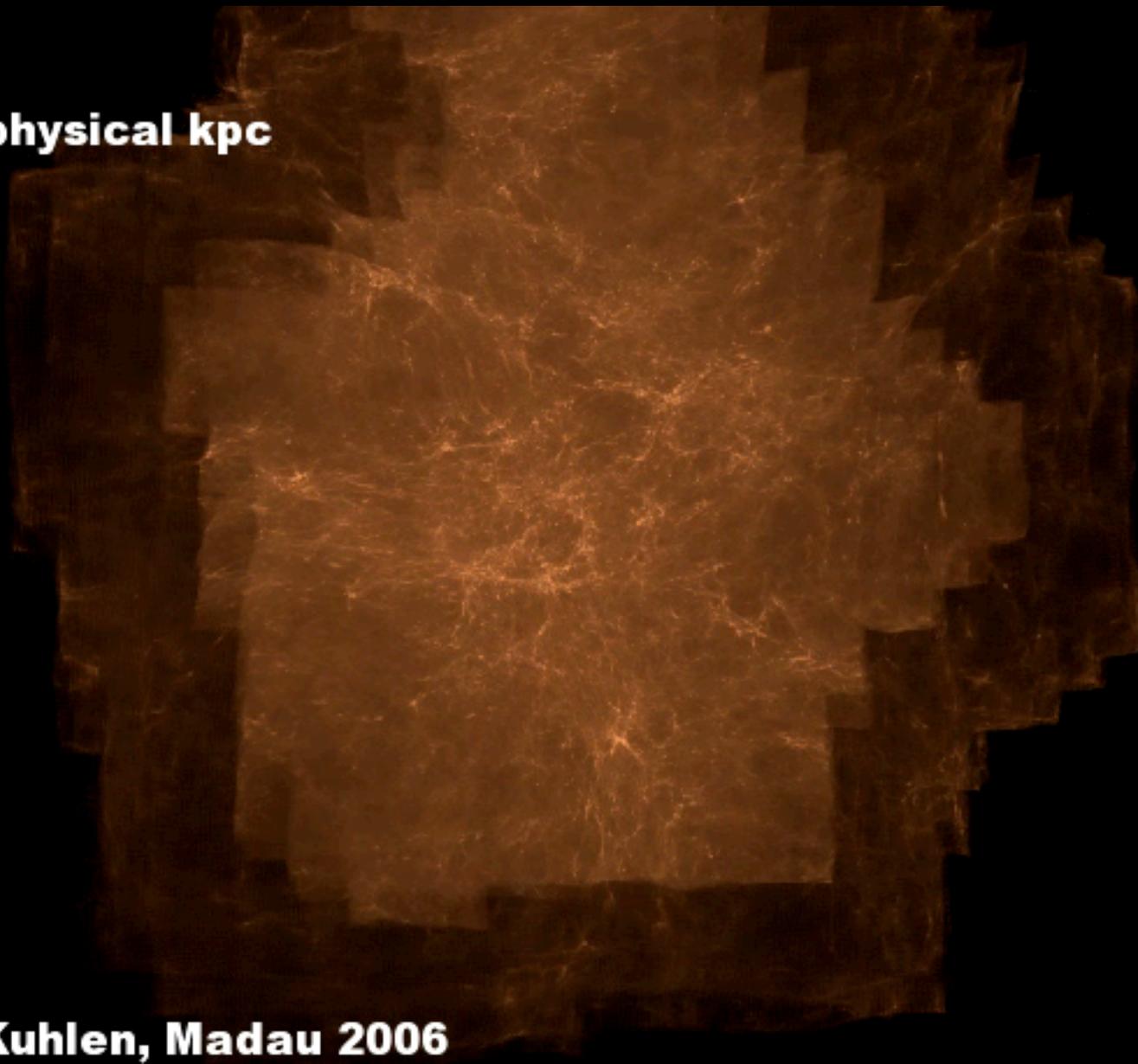
800 x 600 physical kpc



Diemand, Kuhlen, Madau 2006

$z=11.9$

800 x 600 physical kpc



Diemand, Kuhlen, Madau 2006

via lactea

a Milky Way dark matter halo simulated with 234 million particles on NASA's [Project Columbia](#) supercomputer

[main](#)

movies

[movies](#)

These animations show the projected dark matter density-square maps of the simulated Milky Way-size halo Via Lactea. The logarithmic color scale covers the same 20 decades in projected density-square in physical units in each frame. All movies are encoded in MPEG format and some are available in different quality versions.

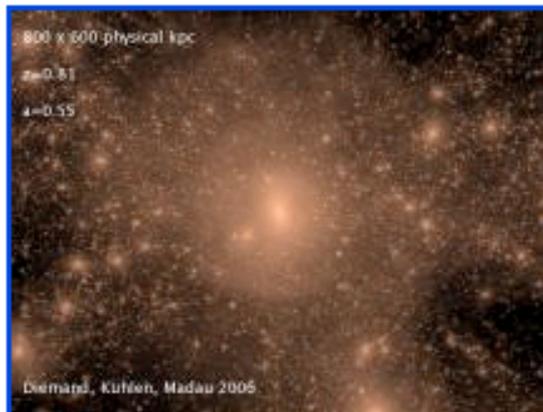
[images](#)

[publications](#)

the formation of the via lactea halo

[data](#)

[screensavers](#)



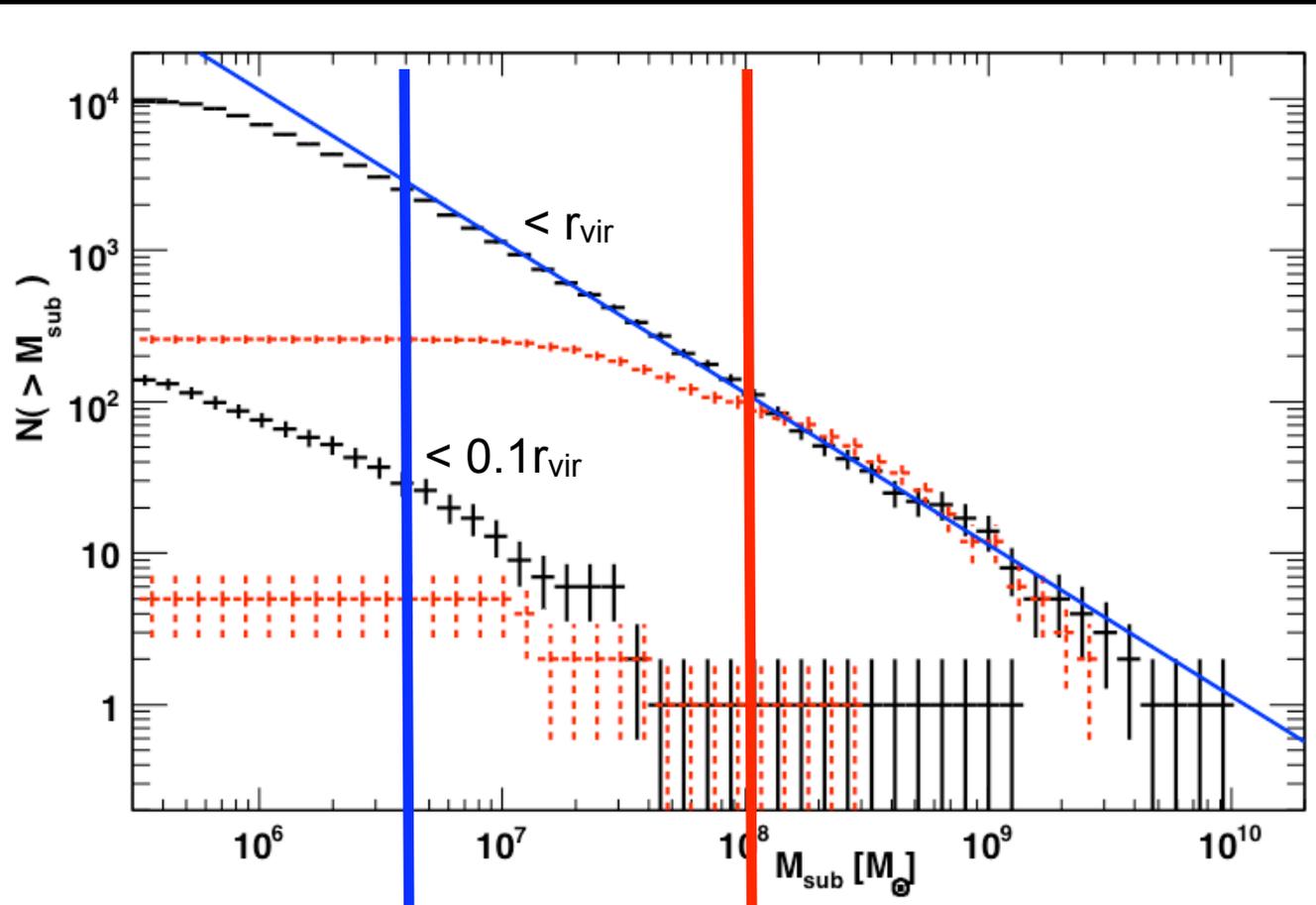
- entire formation history ($z=12$ to 0): [high quality \(218 MB\)](#)
smaller frames, quality: [high\(55 MB\)](#) [medium\(11 MB\)](#) [low\(4.7 MB\)](#)
- entire formation history, plus rotation and zoom at $z=0$:
quality: [high\(433 MB\)](#) [medium\(72 MB\)](#)
- early, active phase of merging and mass assembly ($z=12$ to 1.3): [\(81 MB\)](#)
- late, passive and stationary phase ($z=1.3$ to 0): [\(137 MB\)](#)

rotation and zoom into the via lactea halo at $z=0$ (today)



$z=0$ results from “via lactea” subhalo mass functions

JD, Kuhlen, Madau, astro-ph/0611370



200 particle limits
via lactea
lower resolution run

$$N(>M) \sim M^{-a}$$

with a between 0.9 and 1.1,
depending on mass range:

steeper at high M
due to dynamical friction

shallower at low M
due to numerical limitations

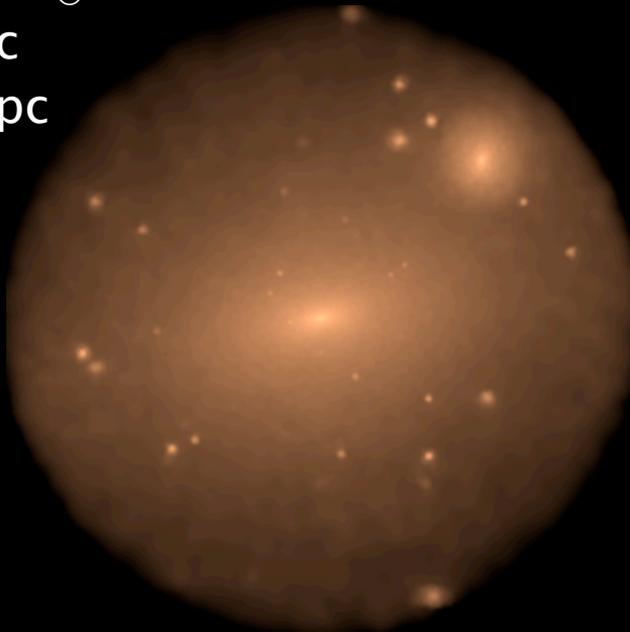
Close to constant contribution
to mass in subhalos
per decade in subhalo mass

sub-subhalos in all well resolved subhalos

$M_{\text{sub}} = 9.8 \cdot 10^9 M_{\odot}$

$r_{\text{tidal}} = 40.1 \text{ kpc}$

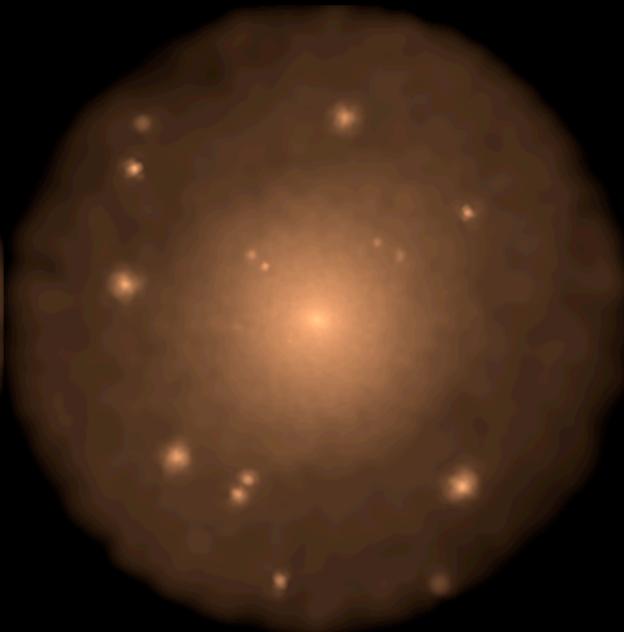
$D_{\text{center}} = 345 \text{ kpc}$



$M_{\text{sub}} = 3.7 \cdot 10^9 M_{\odot}$

$r_{\text{tidal}} = 33.4 \text{ kpc}$

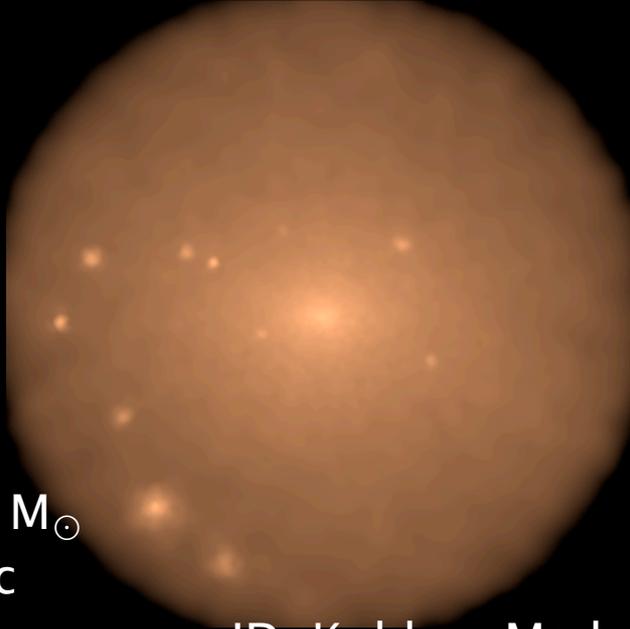
$D_{\text{center}} = 374 \text{ kpc}$



$M_{\text{sub}} = 2.4 \cdot 10^9 M_{\odot}$

$r_{\text{tidal}} = 14.7 \text{ kpc}$

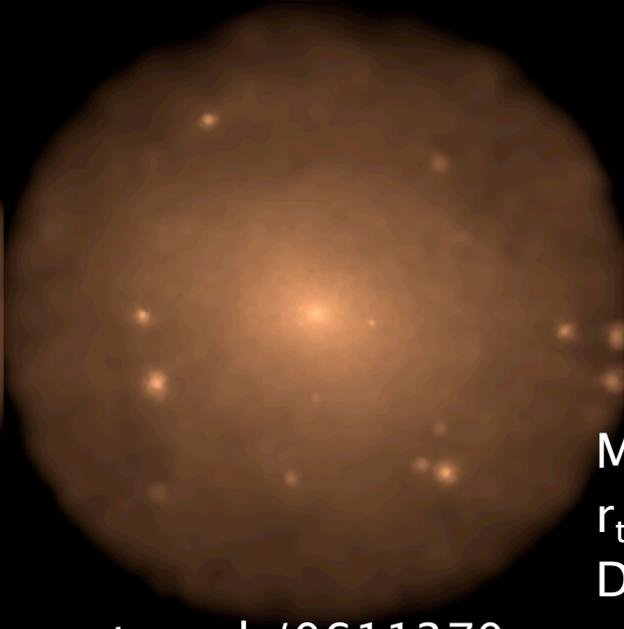
$D_{\text{center}} = 185 \text{ kpc}$



$M_{\text{sub}} = 3.0 \cdot 10^9 M_{\odot}$

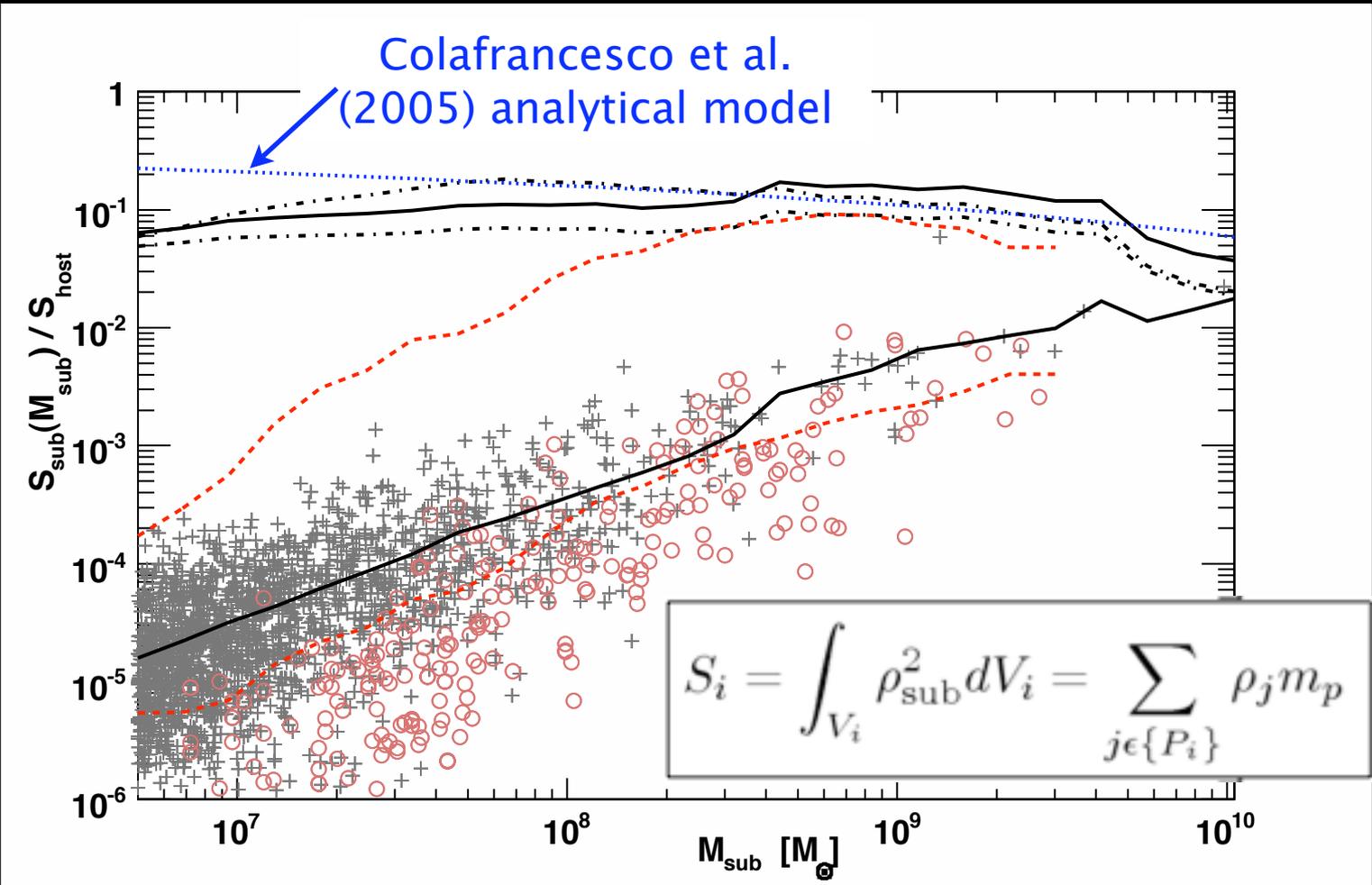
$r_{\text{tidal}} = 28.0 \text{ kpc}$

$D_{\text{center}} = 280 \text{ kpc}$



JD, Kuhlen, Madau, astro-ph/0611370

DM annihilation signal from subhalos



Total signal from subhalos is constant per decade in subhalo mass

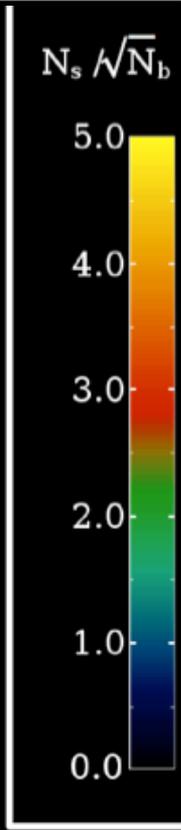
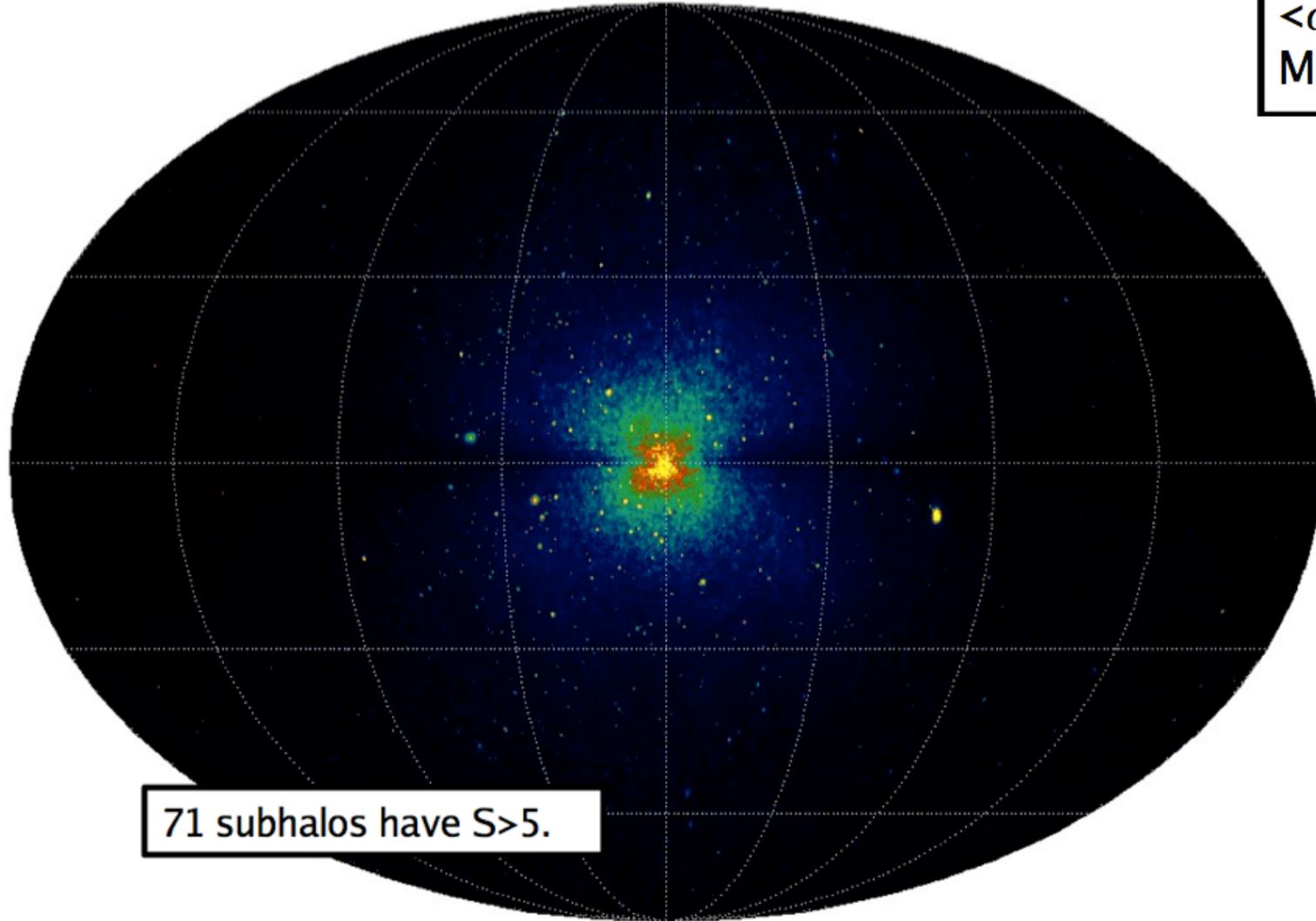
The spherically averaged signal is about half of the total in Via Lactea, but the total signal has not converged

total boost factor from subhalos:
between 3 (constant) and 8 (more from small subs)

total boost factor including sub-sub-....-halos:
between 13 (constant) and about 80

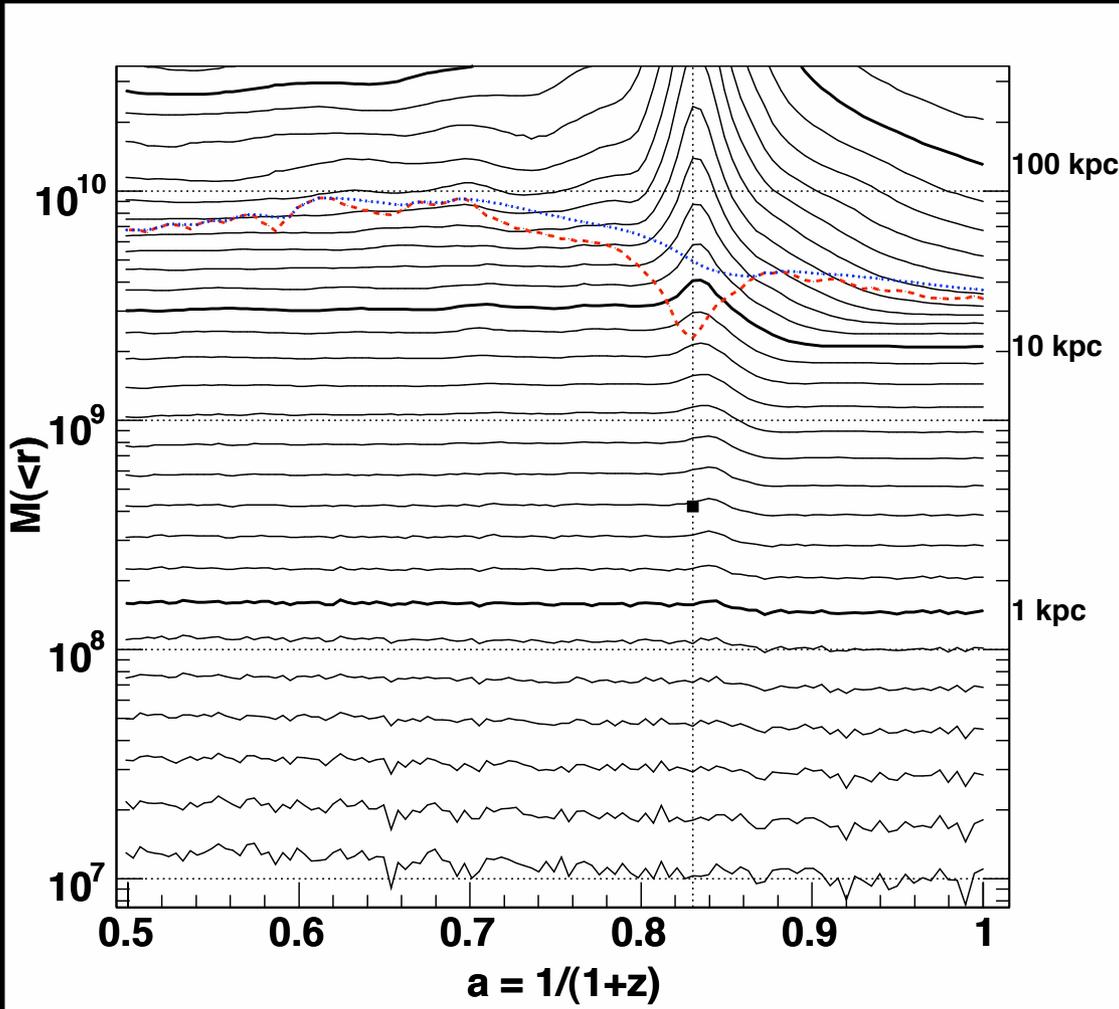
(optimistic) detection significance for GLAST

$$\langle\sigma v\rangle=5\times 10^{-26}\text{ cm}^3\text{ s}^{-1}$$
$$M_\chi=46\text{ GeV}$$



PRELIMINARY allsky map by Mike Kuhlen
assuming sub-substructure boosts subhalo luminosities by a factor of 10
includes extragalactic and galactic (cosmic ray protons on H) backgrounds (Baltz et al 1999)
NOTE: We do not resolve all relevant subhalos yet !

evolution of subhalo density profiles



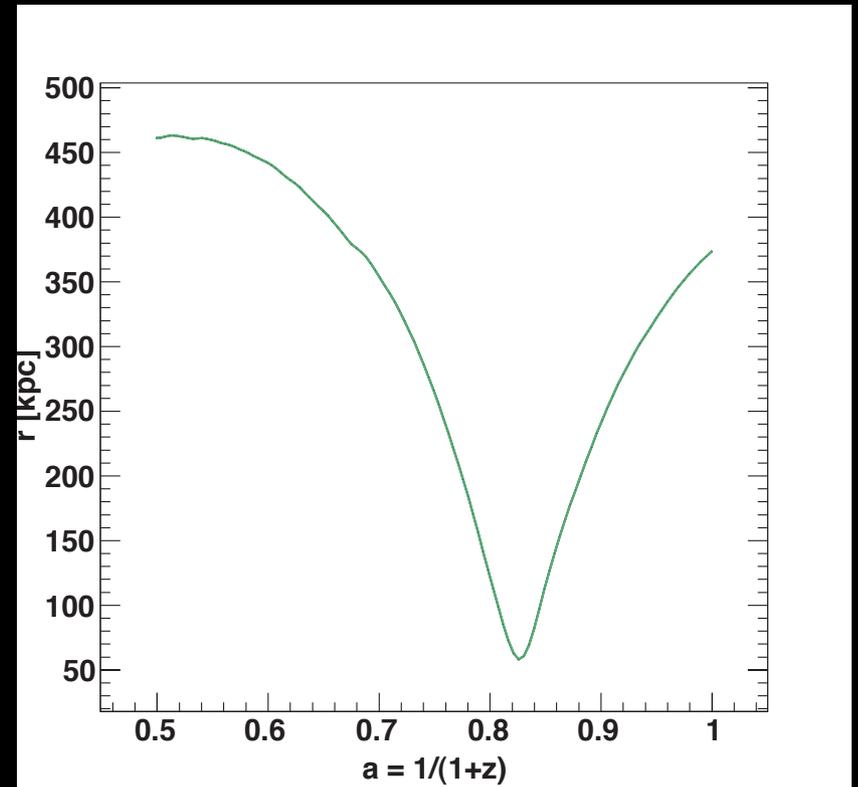
weak, long tidal shock

duration :

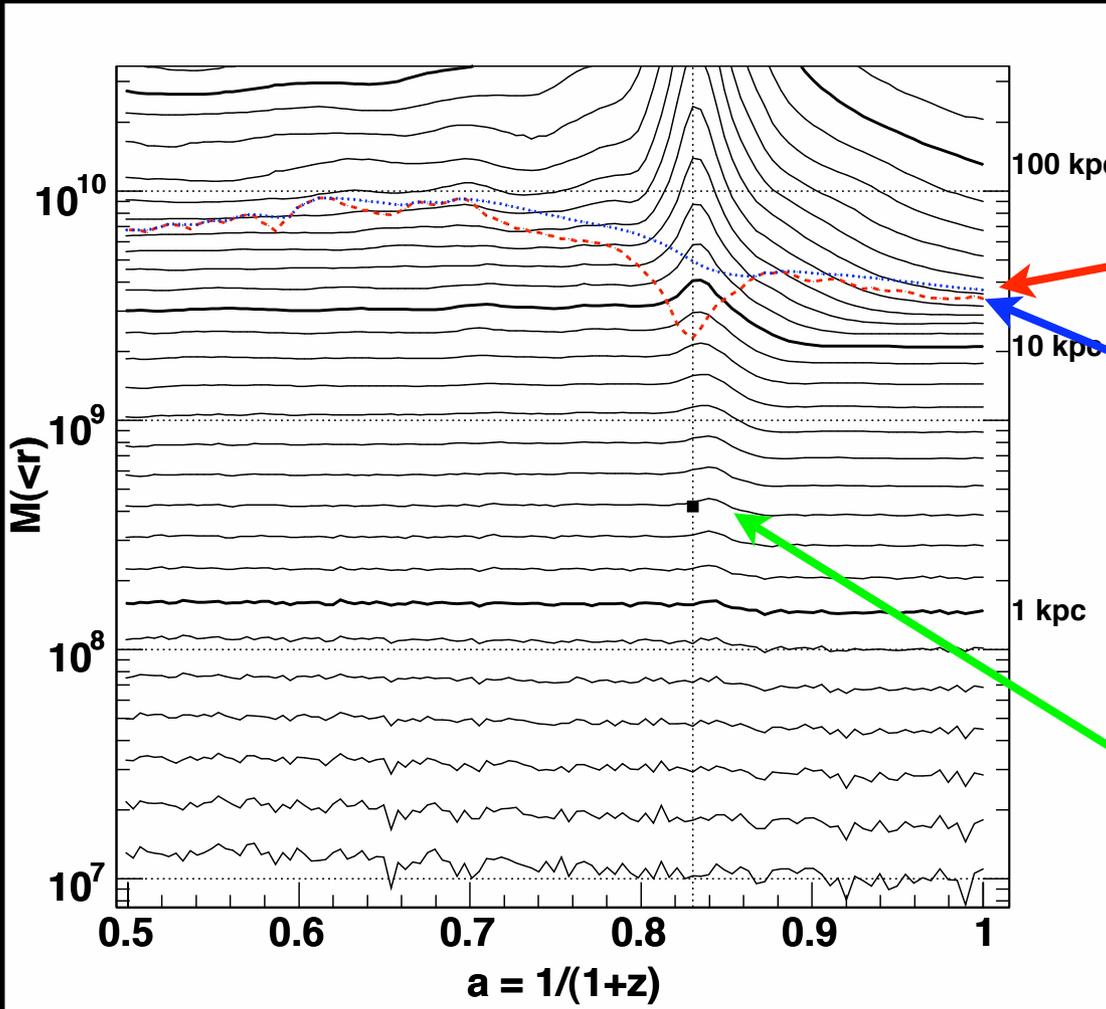
$$\tau = \pi(56 \text{ kpc}) / (423 \text{ km/s}) = 406 \text{ Myr}$$

total mass in spheres around subhalo center

this subhalo has one pericenter passage at 56 kpc



evolution of subhalo density profiles



tidal mass is smaller than the bound mass at pericenter

“delayed” tidal mass

$$\Delta m = M(> r_t) \delta t / T_s$$

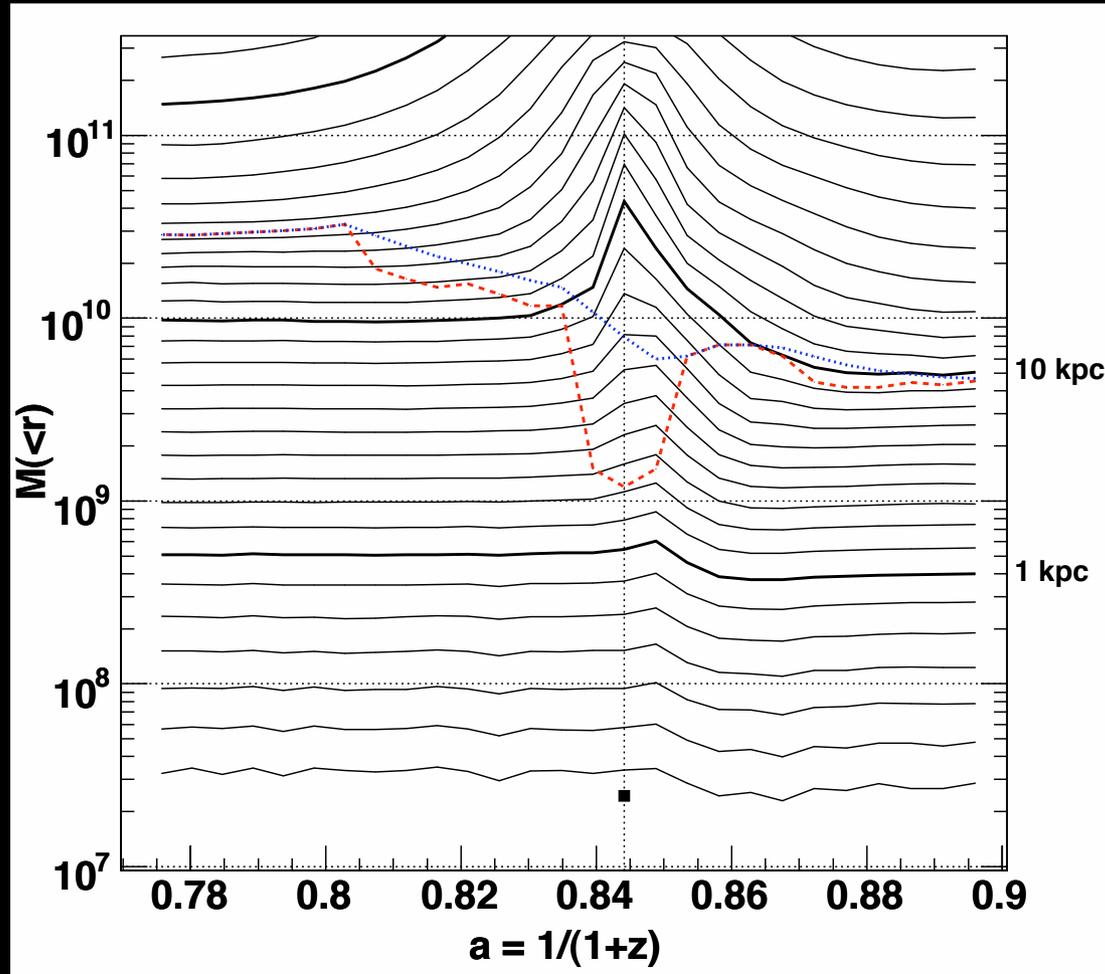
with $T_s = T_{\text{orbit}} / 6$

shock duration = internal subhalo orbital time

weak, long tidal shock
causes quick compression followed by expansion

mass loss is larger further out

evolution of subhalo density profiles

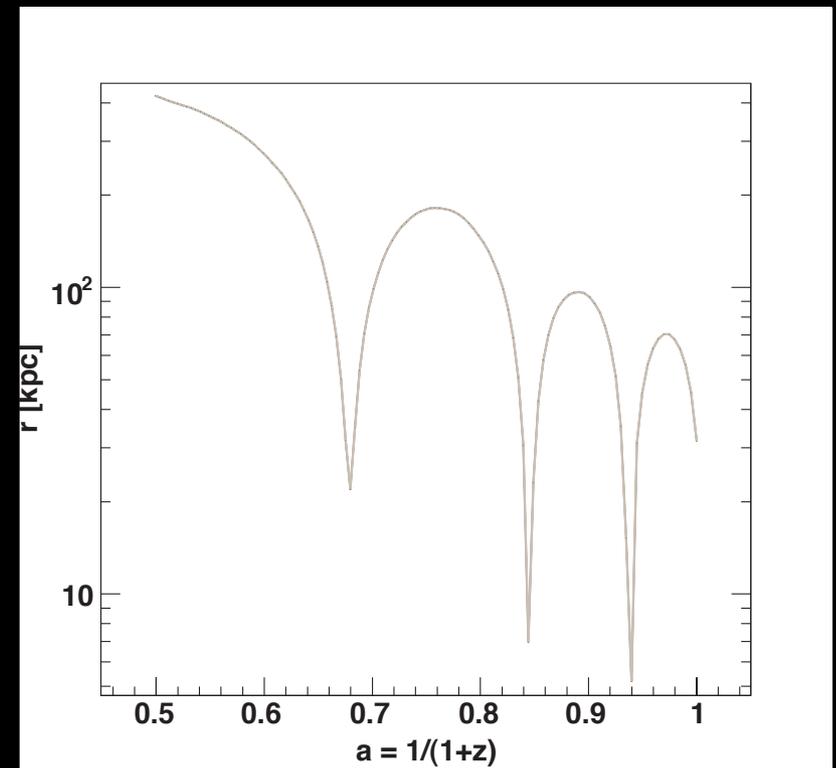


strong, short tidal shock

short duration : 43 Myr ➡ also affects inner halo, but mass loss still grows with radius

at pericenter $r_{\text{tidal}} = 0.2 r_{\text{Vmax}}$, but the subhalo survives this and even the next pericenter

this subhalo has its second of three pericenter passages at 7.0 kpc



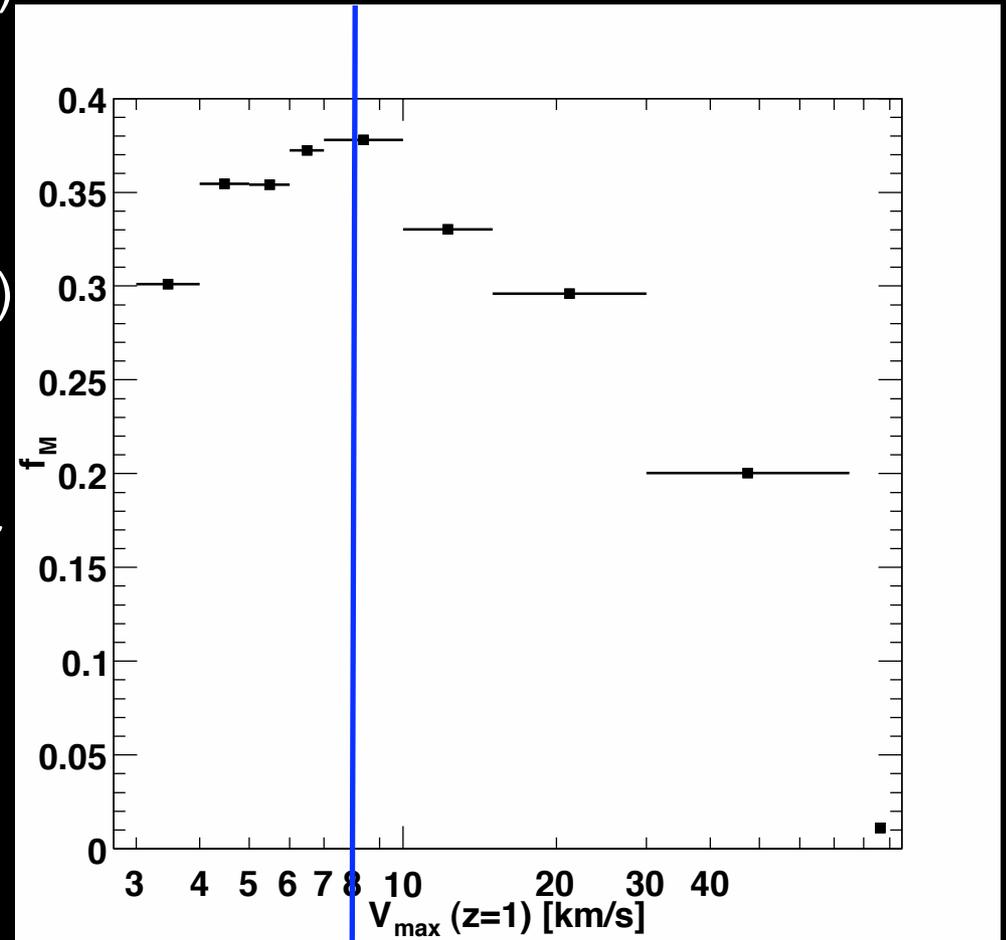
subhalo survival and merging

out of 1542 well resolved ($V_{\max} > 5$ km/s)
 $z=1$ subhalos:

97 % survive until $z=0$

(only 1.3% merge into a larger subhalo)

The average mass fraction that remains
bound to them until $z=0$ depends on their
(initial) size



← affected by numerical limitations

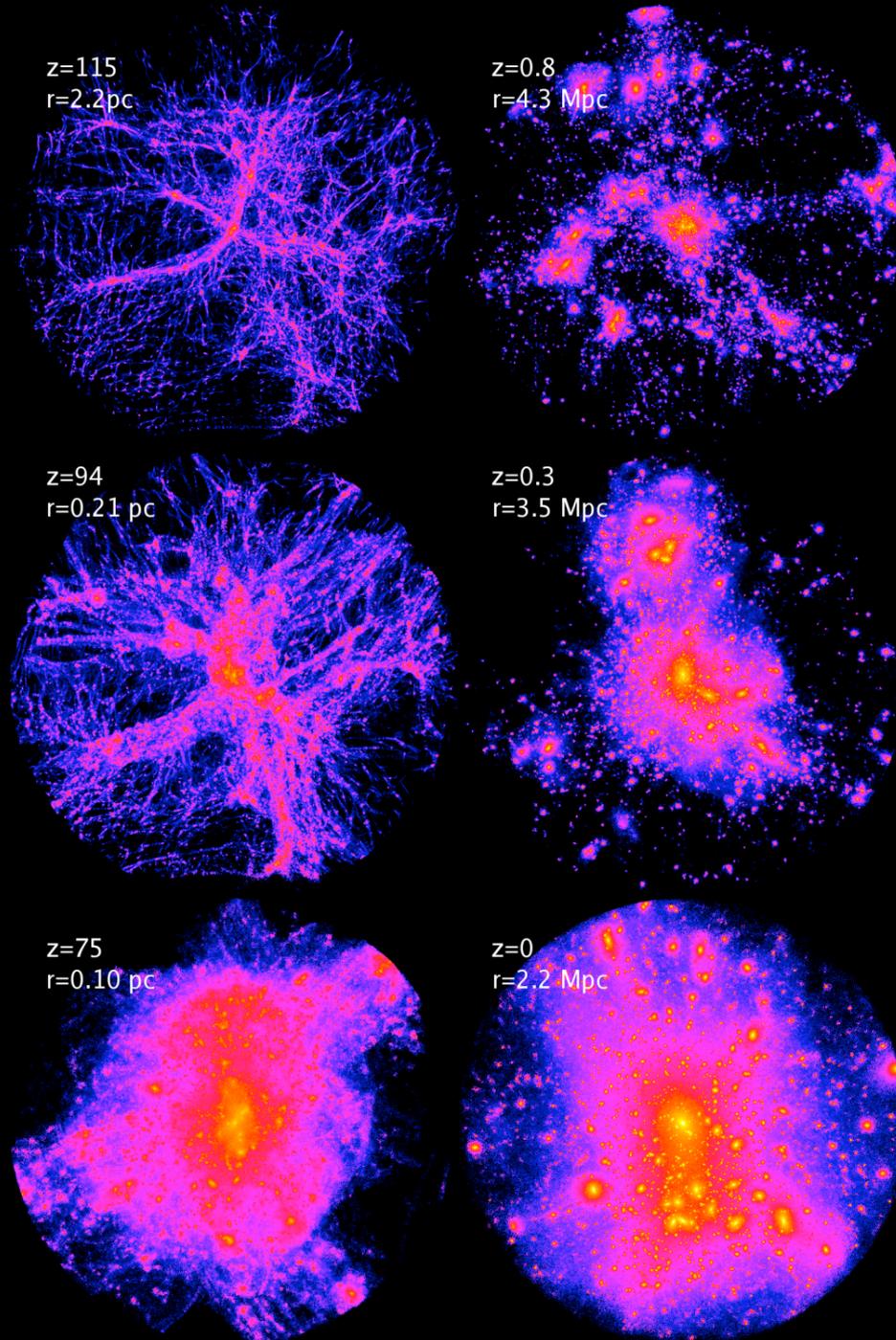
→ stronger dynamical friction

high redshift micro-subhalos are only slightly more fragile despite the flat $\sigma(M)$

almost simultaneous collapse of a $0.01 M_{\text{sun}}$ halo at $z=75$

lower density contrast, but similar subhalo abundance as in a $z=0$ cluster

JD, Kuhlen, Madau
astro-ph/0603250



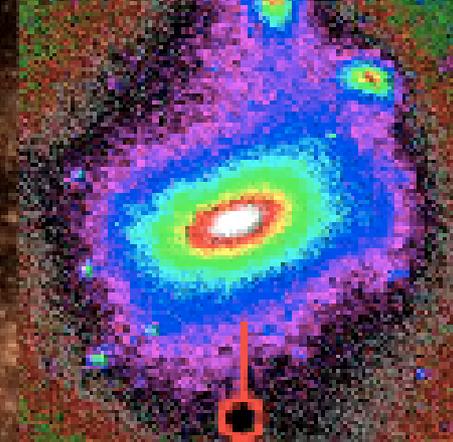
hierarchical formation of a $z=0$ cluster

same comoving DM density scale from 10 to 10^6 times the critical density

in each panel the final $M_{\text{vir}} \sim 20$ million particles are shown

$z=2.0$

800 x 600 physical kpc



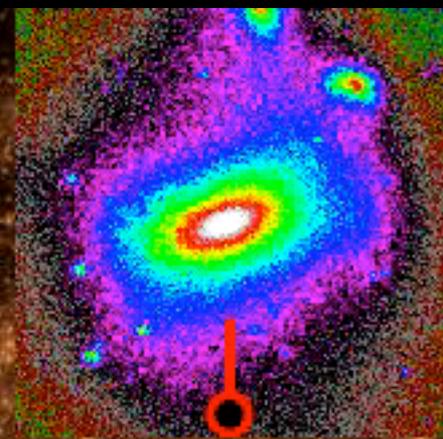
$M_t = 1.6 \times 10^{10} M_\odot$

Diemand, Kuhlen, Madau 2006

subhalos becomes rounder with time
major axes tend to point towards the host center
(Kuhlen, JD, Madau 0705.2037, Faltenbacher+0706.0262, Pereira+0707.1702)

$z=2.0$

800 x 600 physical kpc



$M_t = 1.6e+10 \text{ Mo}$

Diemand, Kuhlen, Madau 2006

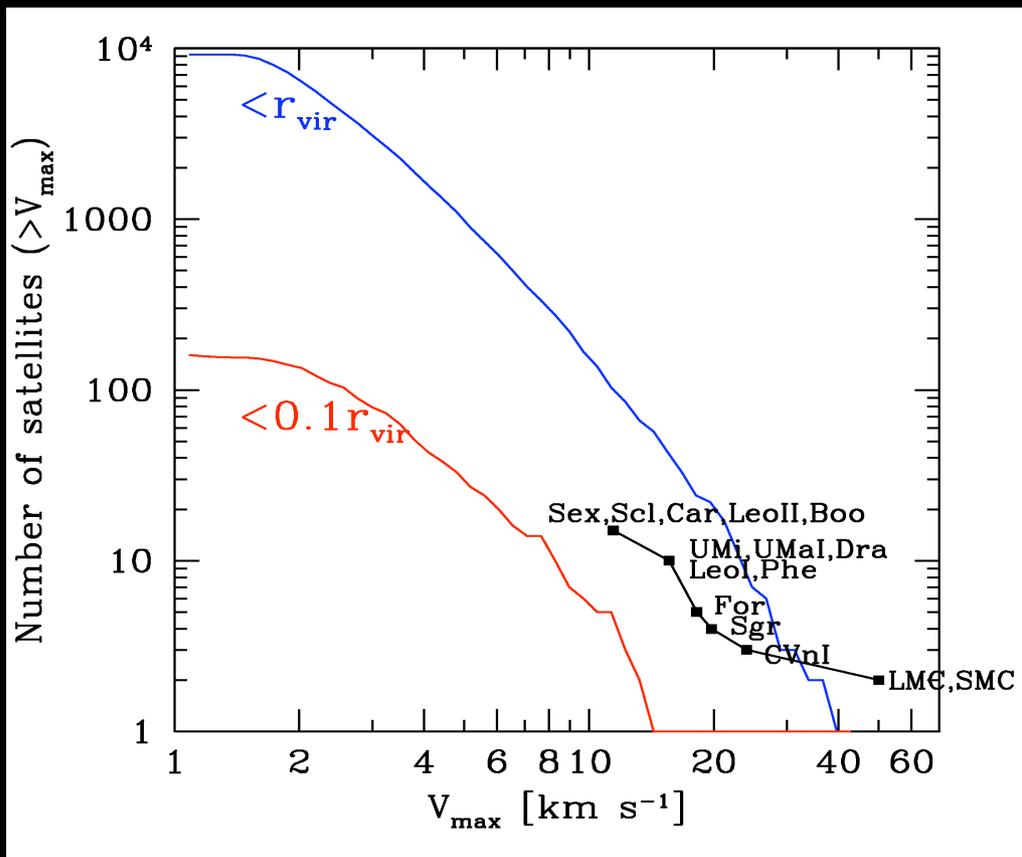
subhalos becomes rounder with time
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missing satellites?

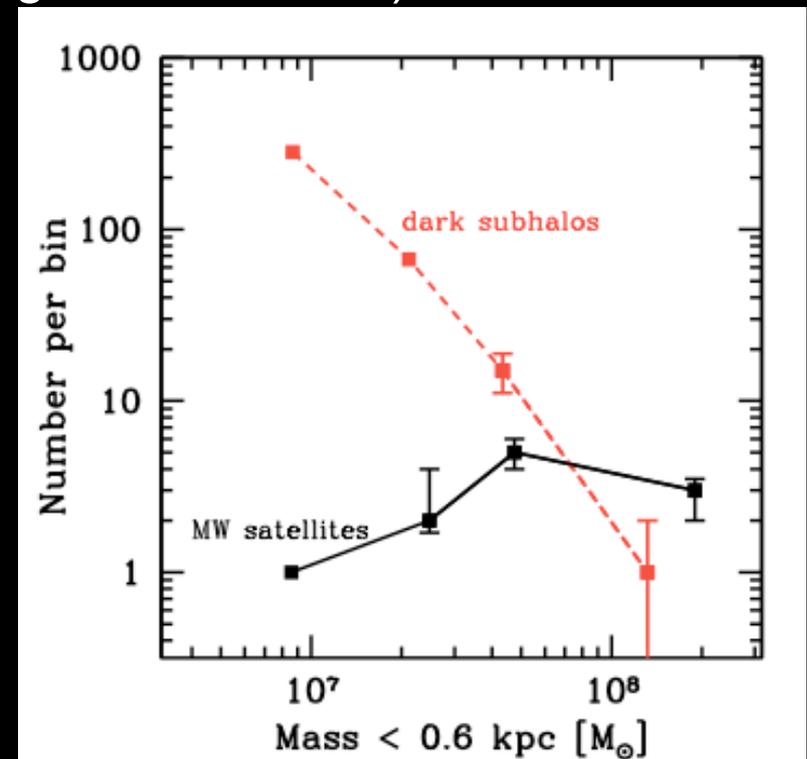
CDM only predicts subhalos, not dwarf galaxies. Luckily, CDM predicts (more than) enough structures to host all known Local Group satellites.

Plausible galaxy formation models roughly reproduce the observed numbers of dwarfs. Many CDM subhalos remain dark (Governato et al. 2007)

As in the original (Moore+99, Klypin+99) comparisons we assumed $\sqrt{3} \sigma^* = V_{\max}$

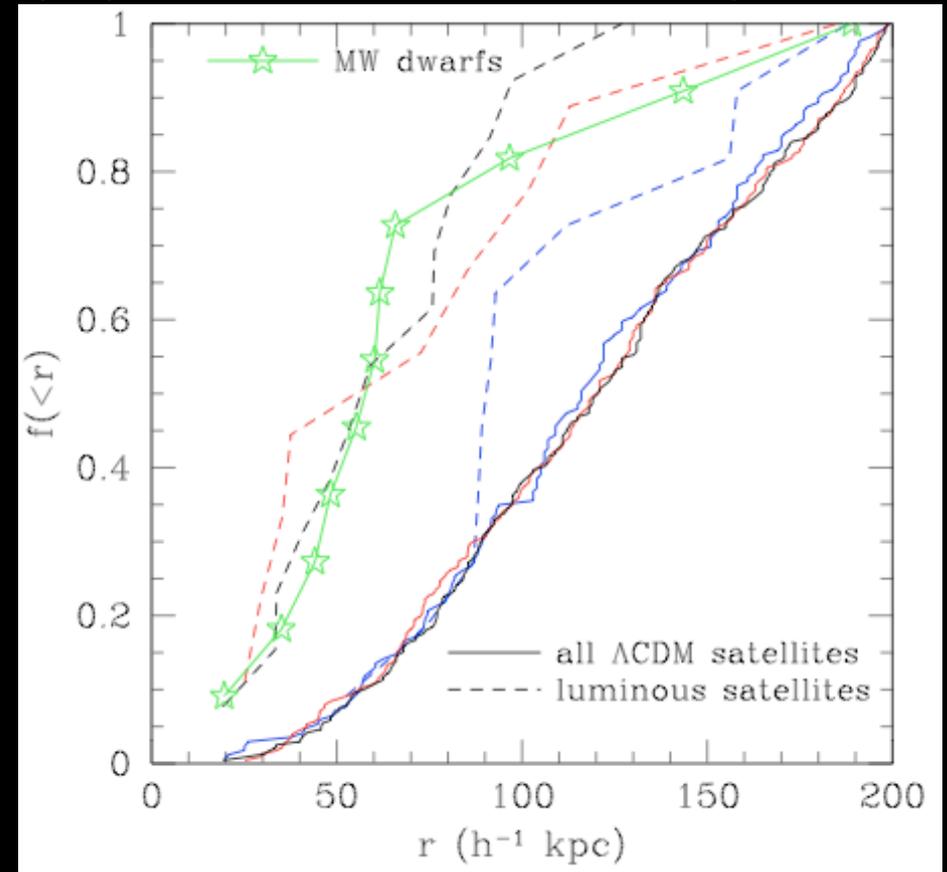
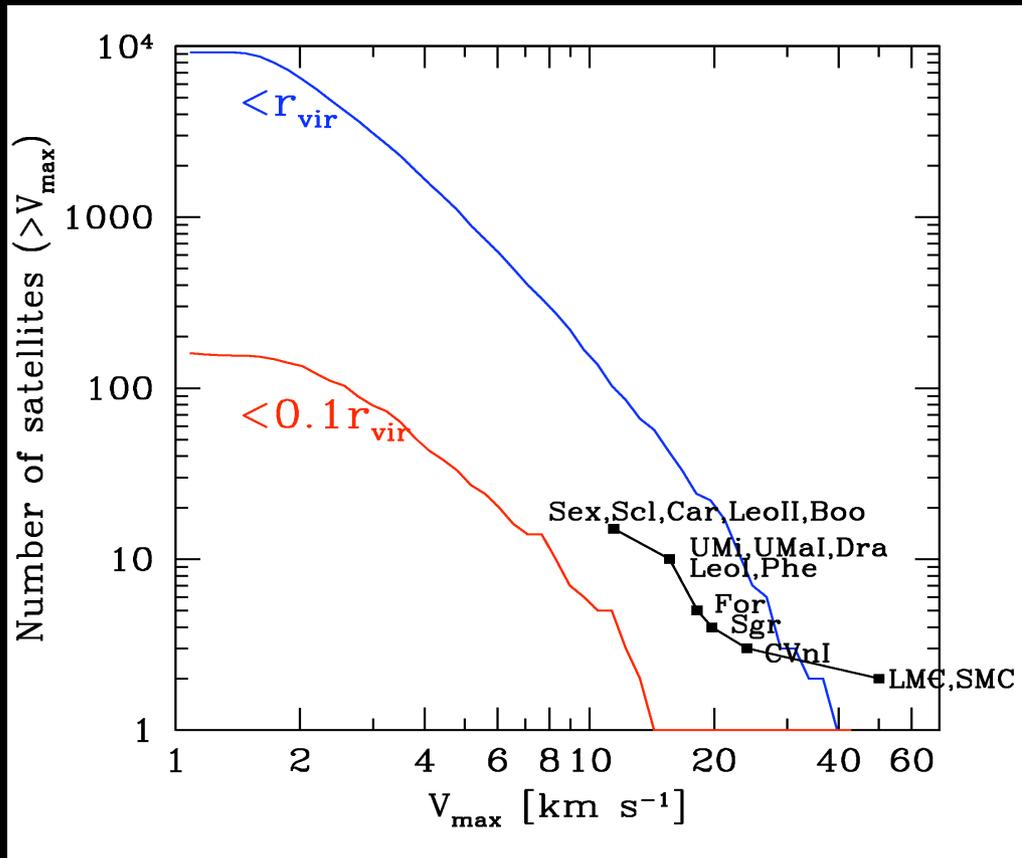


this seems to be roughly right (Strigari+0704.1817):



missing satellites?

the largest subhalos are much further away (Taylor+2003, Kravtsov+2004):

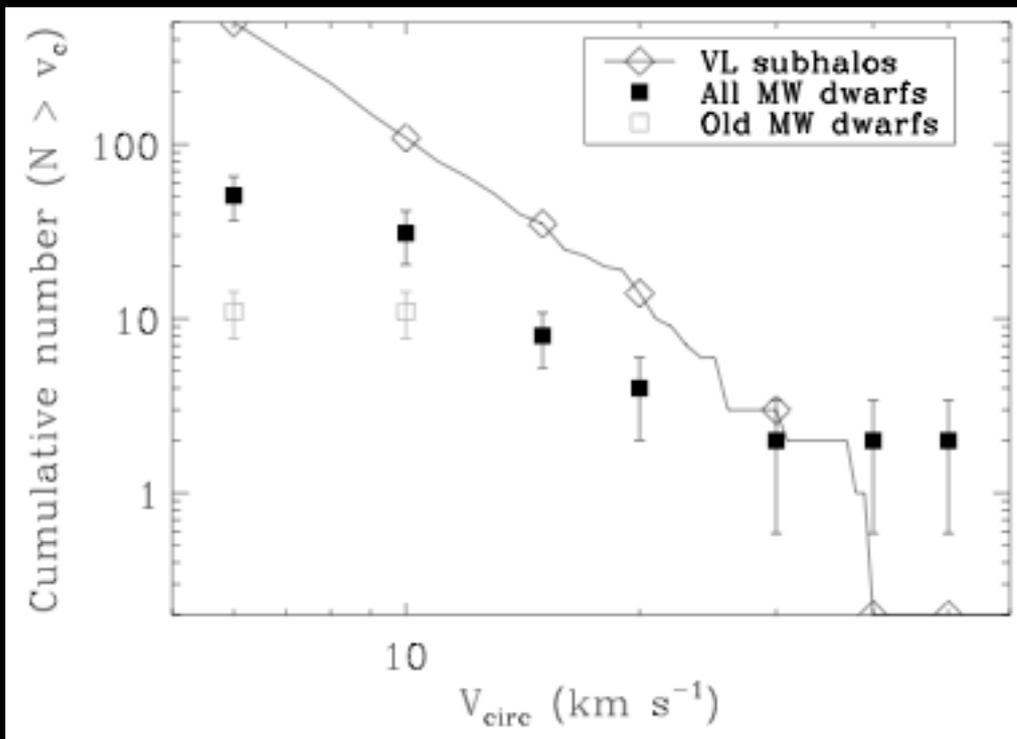


we need more subhalos than dwarf at a given size to find enough that are also at the correct distances!

(lowering the normalization would be a problem on LMC/SMC scales
Via Lactea is near the median, rms halo to halo scatter is about a factor of two)

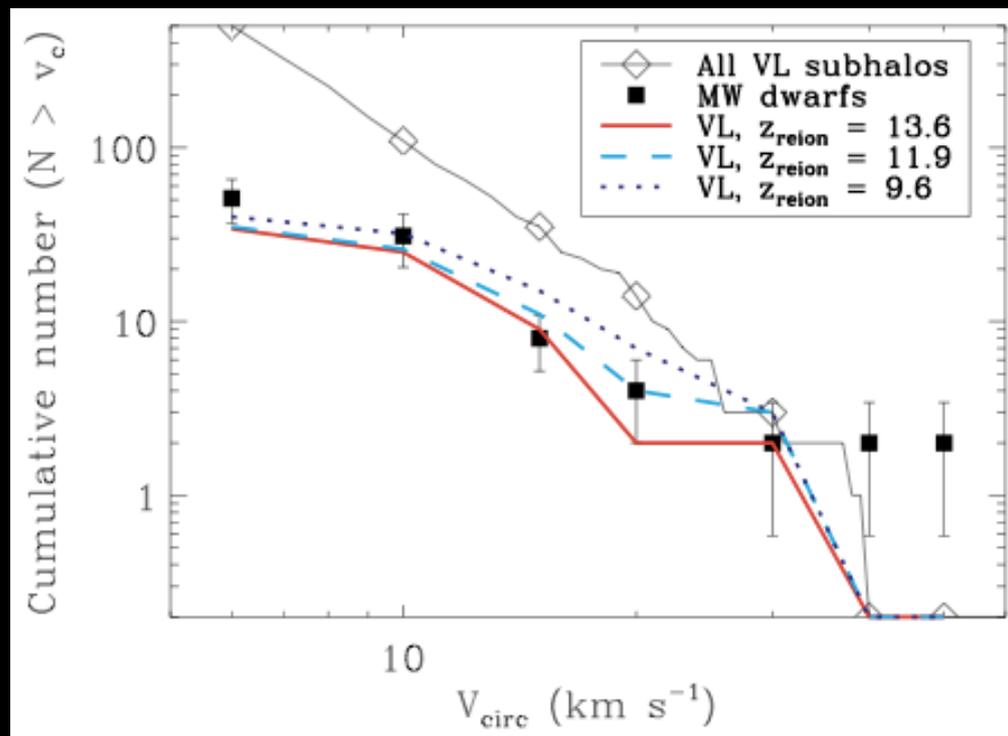
missing satellites?

adding the new ultra faint dwarfs from SDSS helps (Simon+Geha2007):

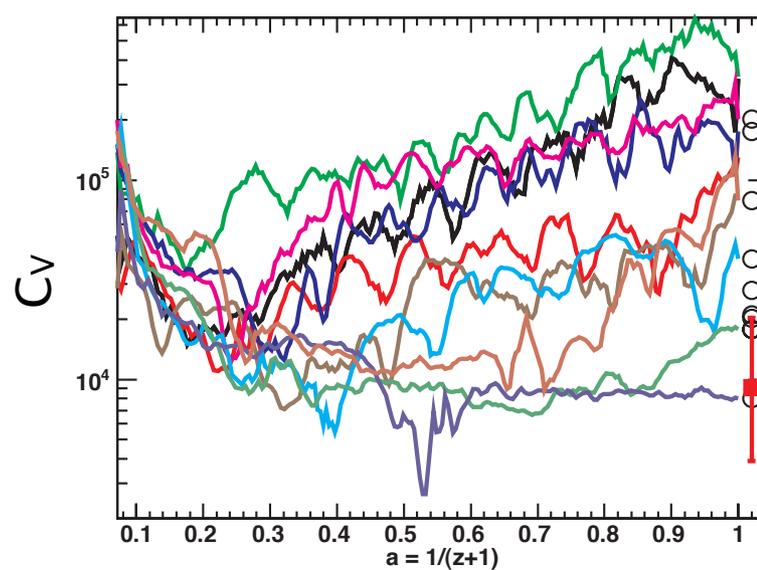
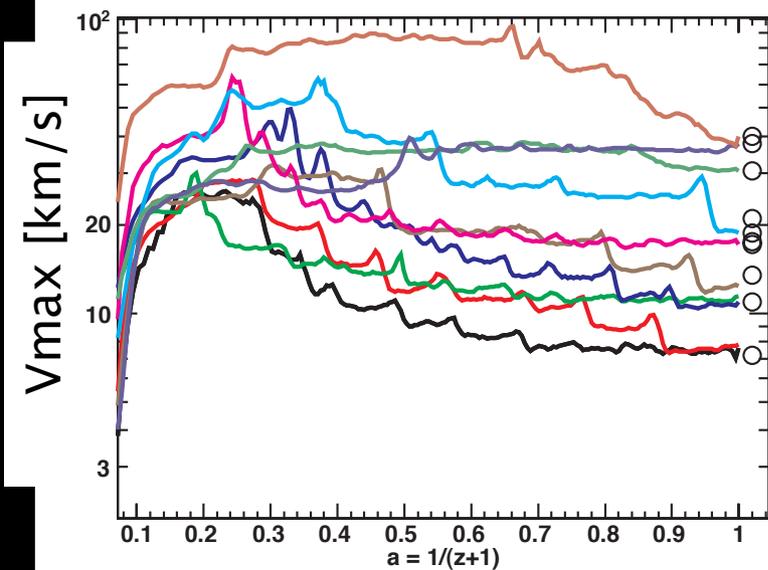
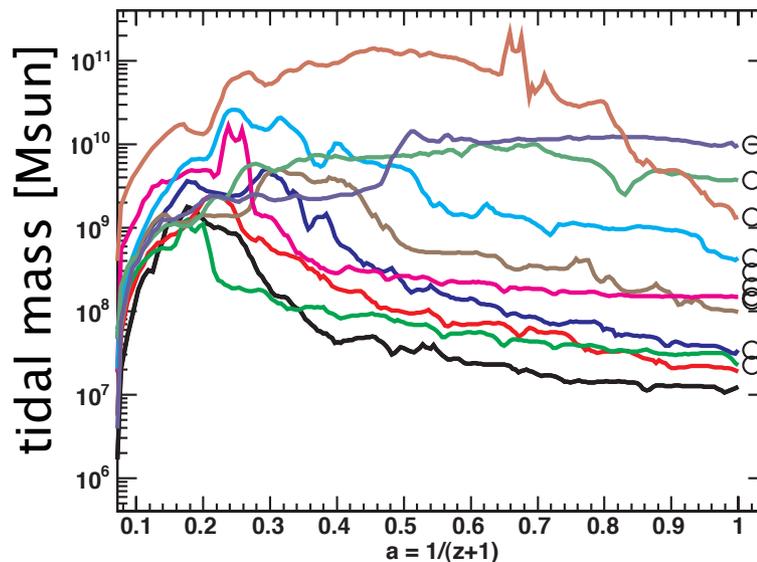
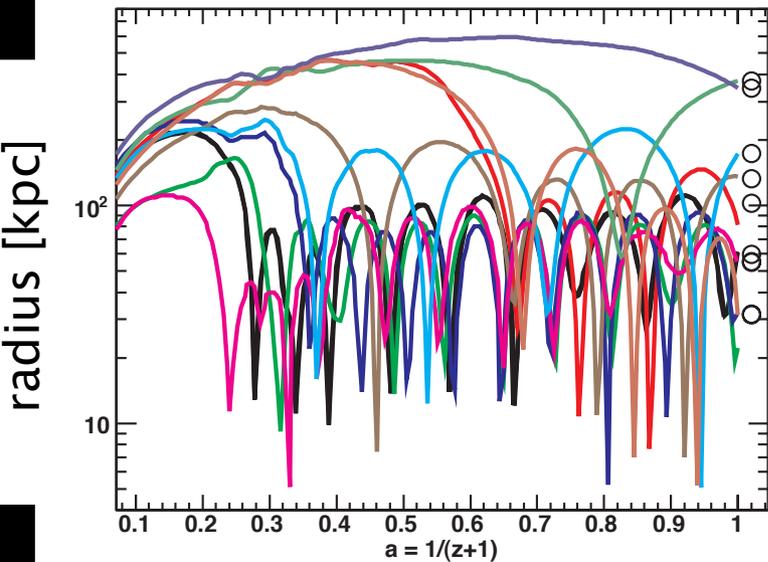


early forming subhalos would have the right sizes (Simon+Geha2007)

and also the right spatial distribution (Moore+2006)



possible hosts for Local Group dwarfs



diverse histories:

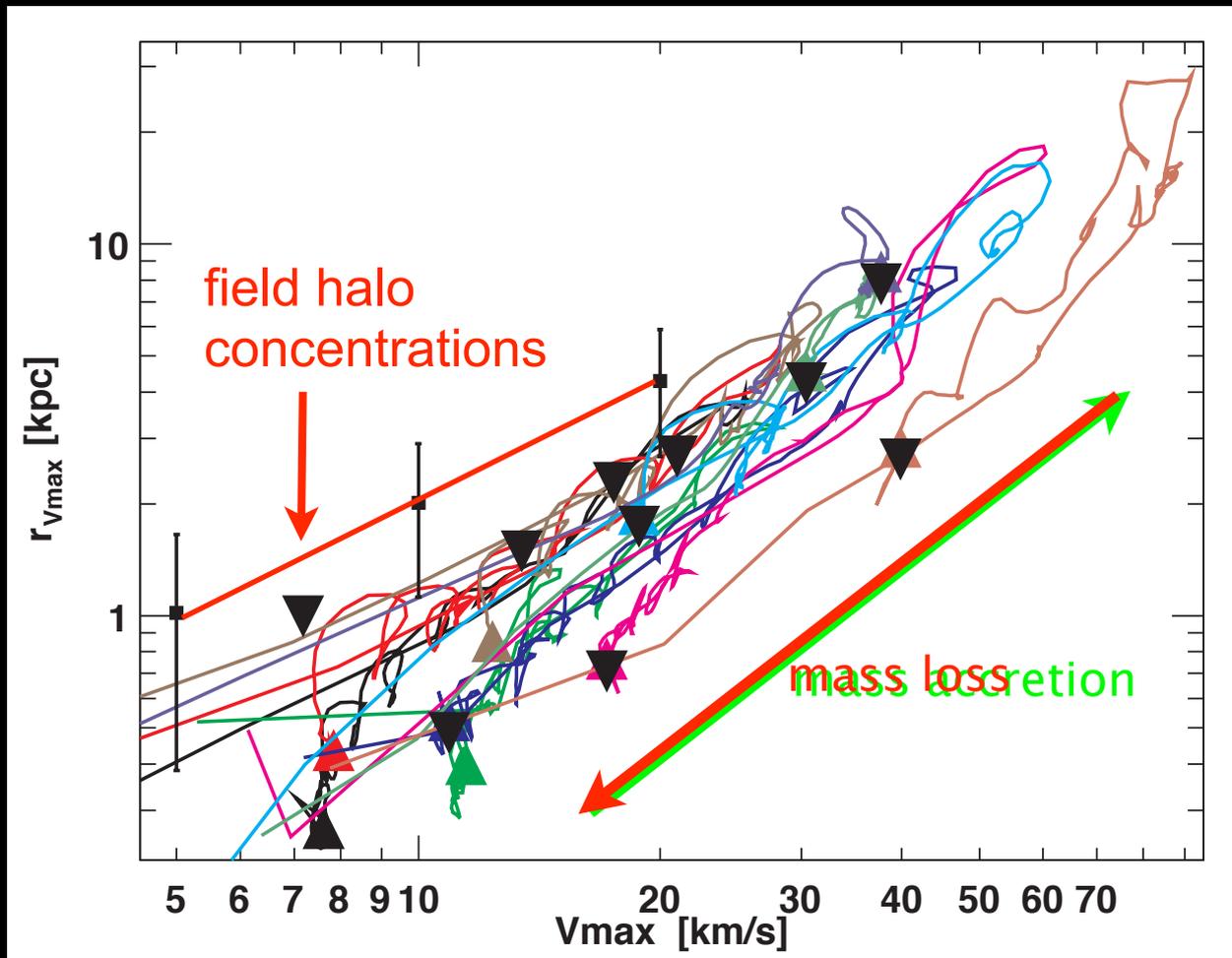
0 to 11
pericenters
inner subhalos
tend to have
more of them
and starting
earlier

none to very
large mass loss

concentrations
increase during
tidal mass loss

field halo
concentrations

possible hosts for Local Group dwarfs



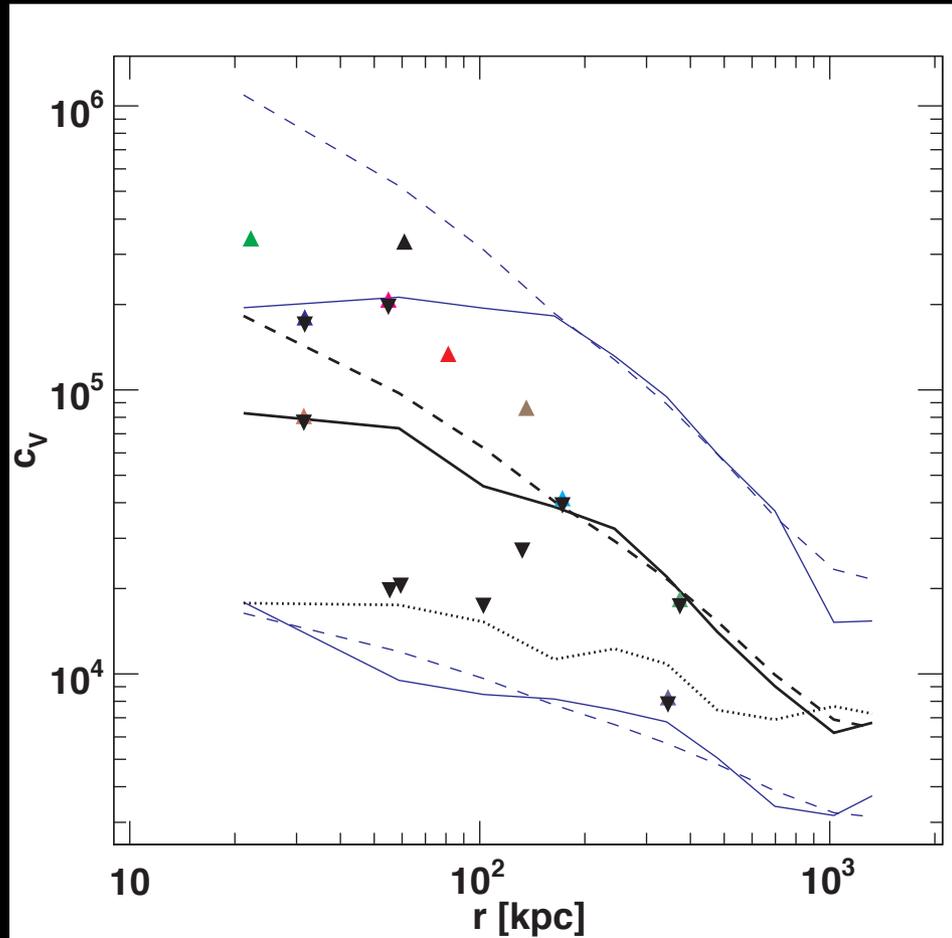
same 10 EF tracks

tidal mass loss from the outside in partially undoes the inside out halo assembly

→ stripped halos resemble high redshift systems

→ they have high concentrations

subhalo concentrations

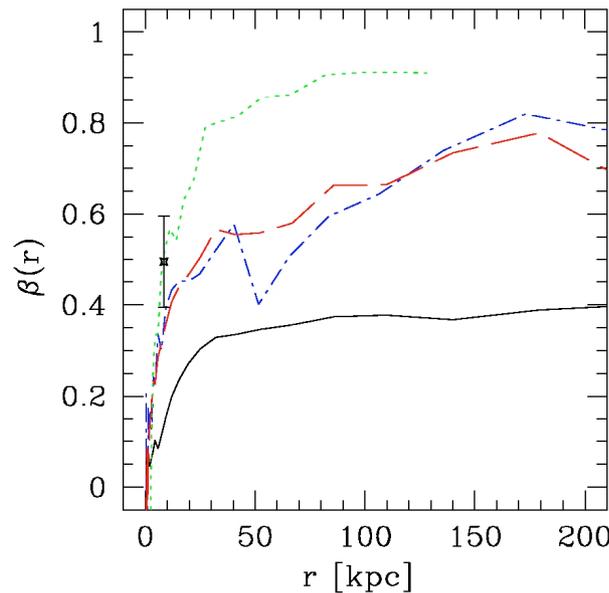
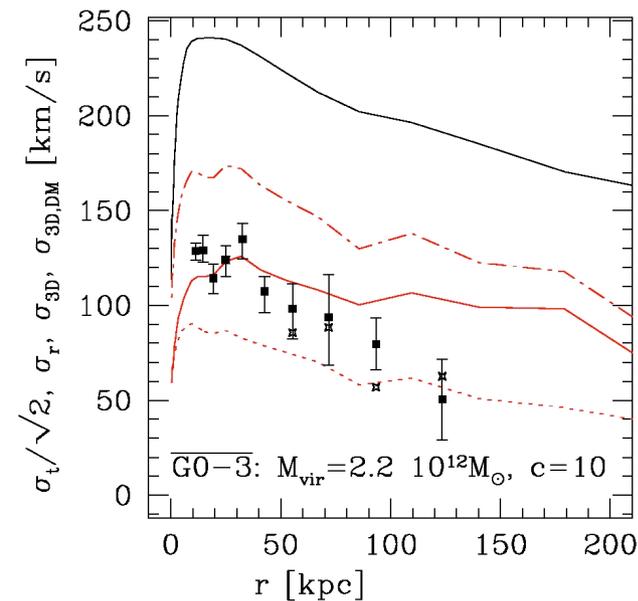
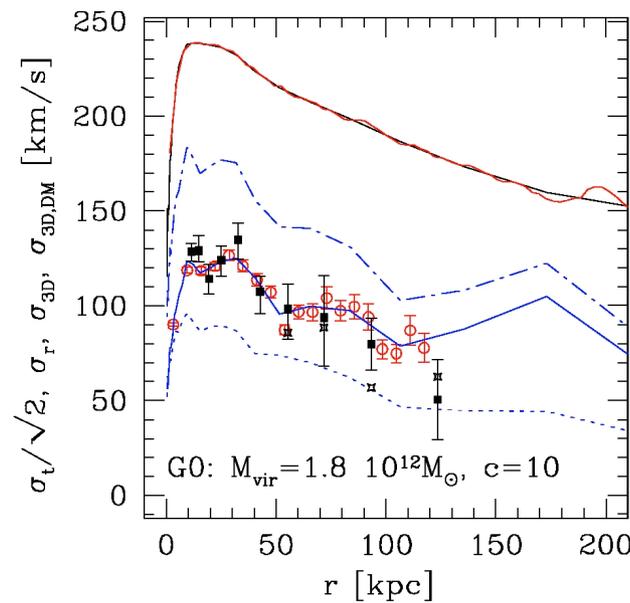
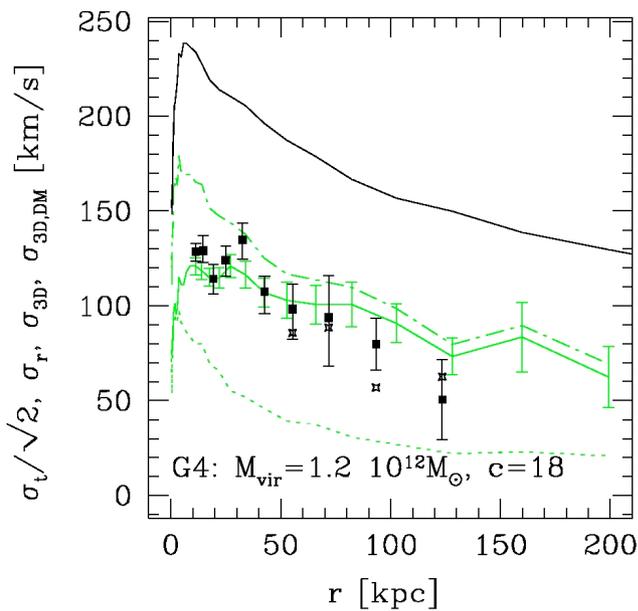


median concentrations increase towards the galactic center

the 68% scatter also increases

earlier formation times alone cannot fully explain this trend (dotted line)

EF model fits Milky Way stellar halo radial velocities



cosmological stellar halo kinematics fit the observations well

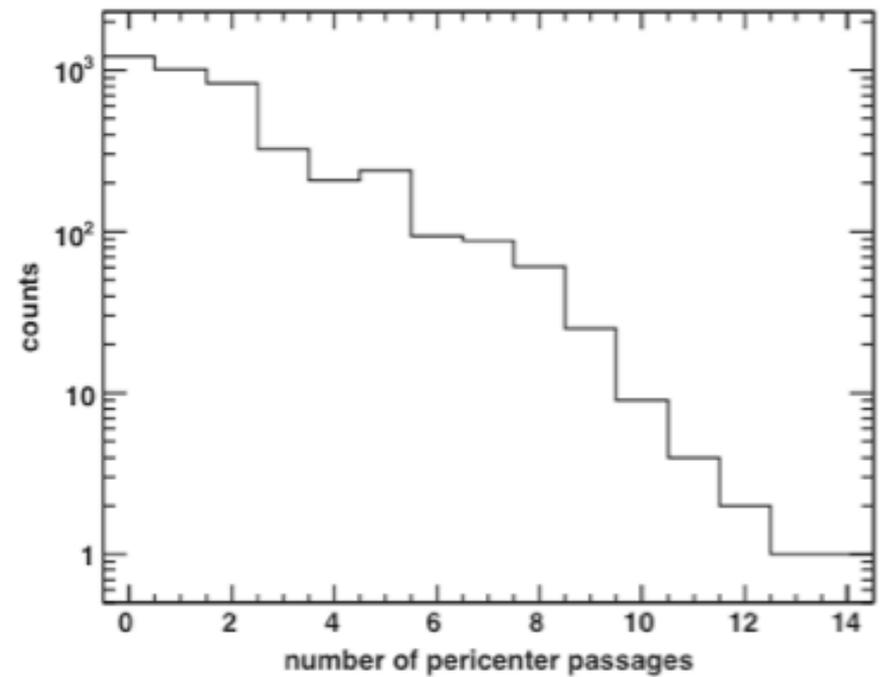
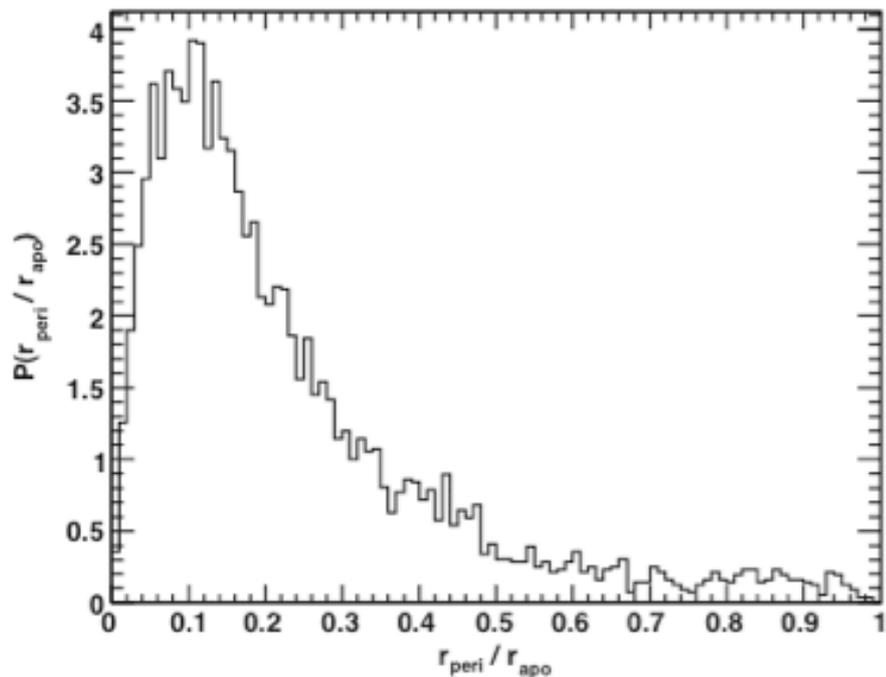
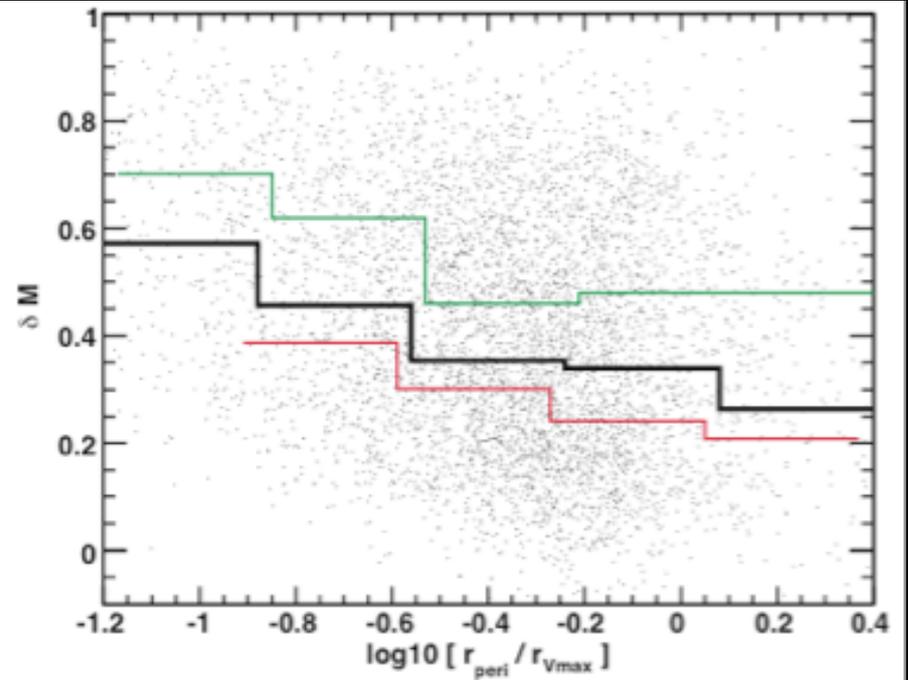
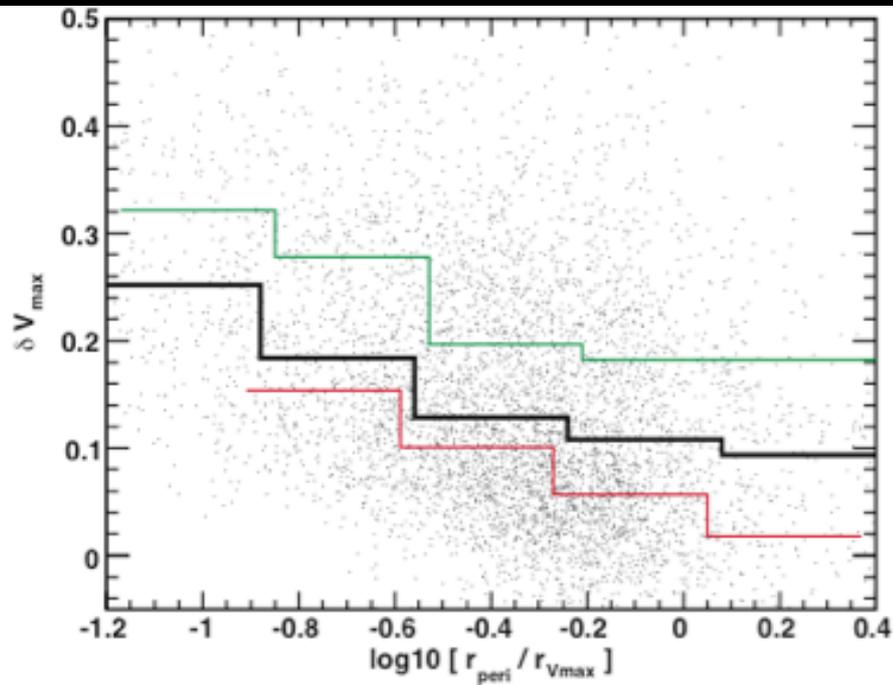
The outer halo is not well constrained:

low M_{vir} / high c
high M_{vir} / low c
both possible

$\beta(r)$ relates to tracer profile slope as in Hansen&Moore, 2004

JD, Madau, Moore 2005

larger mass loss at first pericenter



summary : substructure

small subhalos contribute significantly to the mass fraction in subhalos and to the total DM annihilation signal. therefore both quantities have not converged

tides remove subhalo mass from the outside in and lead to higher concentrations for subhalos. the effect is stronger near the galactic center

CDM predicts enough subhalos to host all the currently known Local Group dwarfs

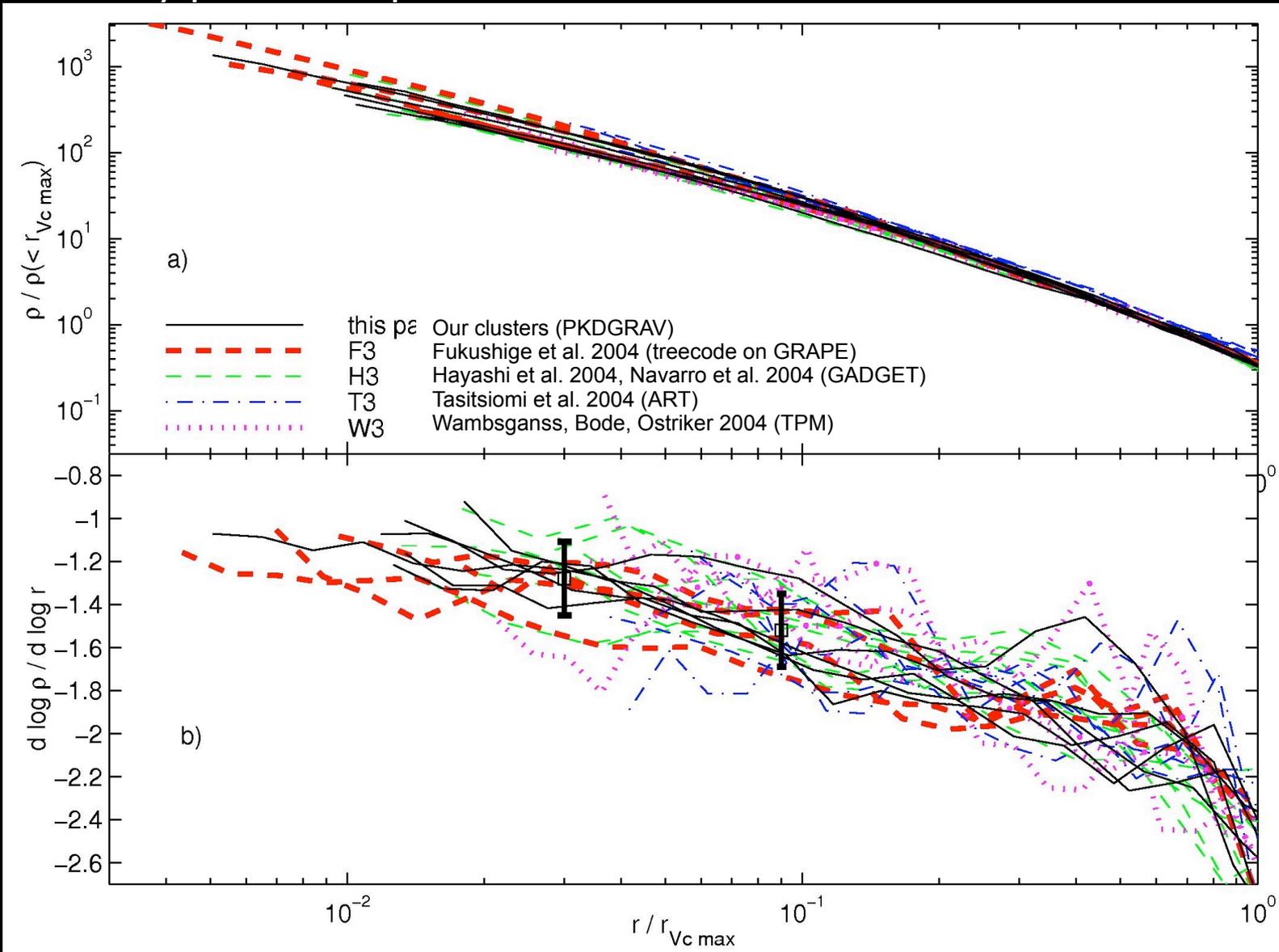
most (97%) subhalos survive from $z=1$ until today. smaller ones loose less mass

high redshift micro-subhalos are only slightly more fragile despite thier flat $\sigma(M)$

scatter in CDM cluster density profiles

eg. Fukushige et al 2004, Navarro et al 2004, JD et al 2004

CDM density profiles are close to universal (e.g. NFW), but individual halo density profile shapes have scatter:



JD, Moore, Stadel,
MNRAS, 2004

scatter in CDM cluster density profiles

	$1\%r_{\text{vir}}$	$3\%r_{\text{vir}}$	$3\%r_{\text{Vcmax}}$	$9\%r_{\text{Vcmax}}$
<i>A9</i>	1.22	1.36	1.24	1.64
<i>B9</i>	1.33	1.43	1.21	1.63
<i>C9</i>	1.24	1.21	1.25	1.26
<i>D12</i>	1.28	1.54	1.32	1.58
<i>E9</i>	1.31	1.44	1.41	1.62
<i>F9cm</i>	1.19	1.47	1.22	1.43
a) A-F	1.26 ± 0.05	1.41 ± 0.11	1.28 ± 0.08	1.53 ± 0.15
b) F03	1.25 ± 0.05	1.52 ± 0.06	1.33 ± 0.15	1.54 ± 0.15
c) H03	1.18 ± 0.13	1.38 ± 0.14	1.23 ± 0.17	1.50 ± 0.14
d) T03	1.50 ± 0.14	1.79 ± 0.07	—	1.56 ± 0.12
e) W03	1.11 ± 0.04	1.41 ± 0.13	—	1.35 ± 0.06
avg. (a-e)	1.26	1.50	—	1.49
avg. (a-c)	1.23	1.44	1.28	1.52
NFW			1.12	1.32
Moore et al.			1.54	1.65

JD, Moore, Stadel,
MNRAS, 2004, 353, 624

why are profiles nearly universal? what causes the scatter?

fitting functions

2 parameter functions (only two 'scaling' parameters):

NFW

$$\rho = \frac{\rho_s}{x(1+x)^2}$$

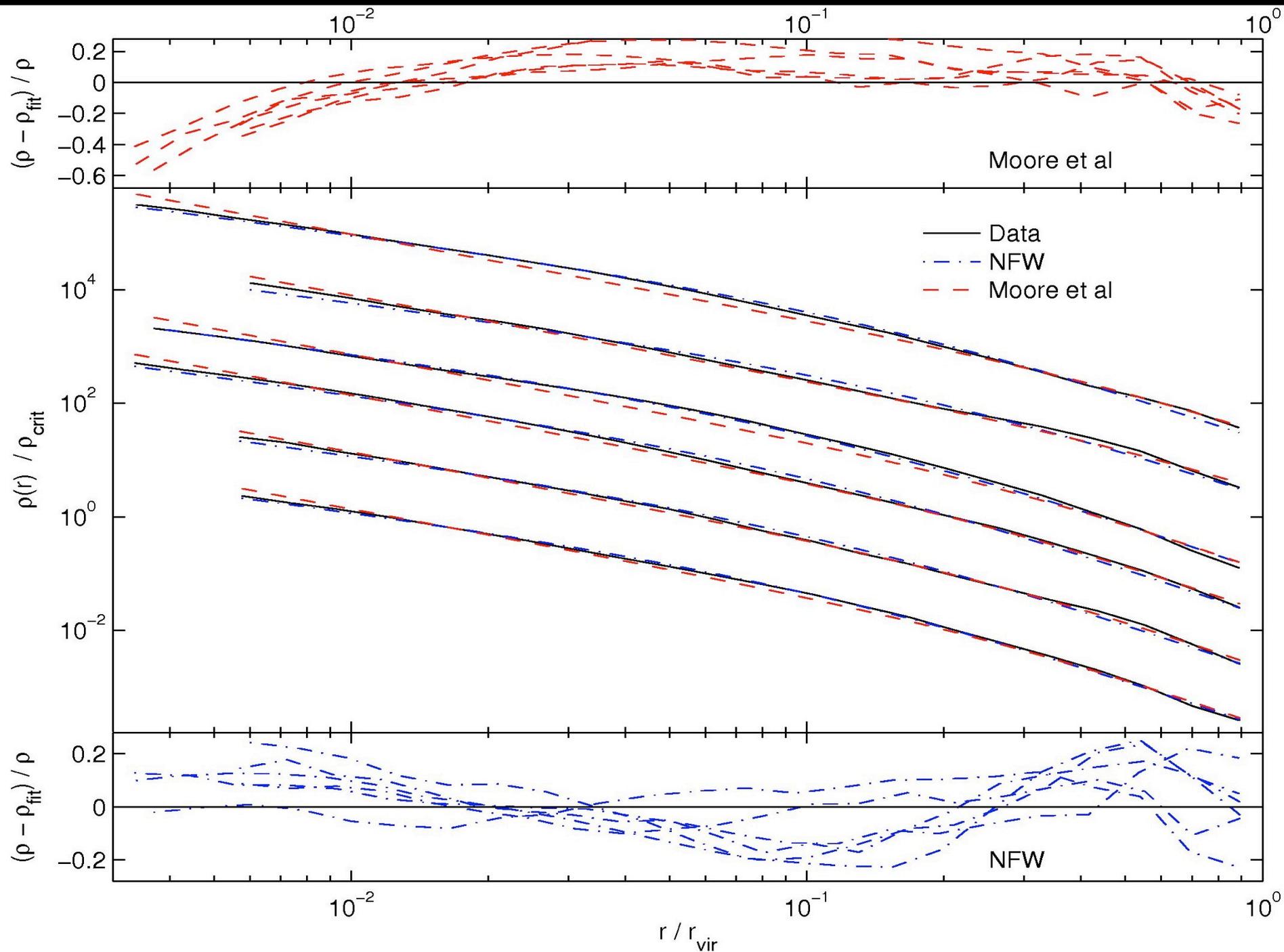
Moore et al 1999

$$\rho = \frac{\rho_s}{x^{1.5}(1+x)^{1.5}}$$

$$x = r/r_s$$

2 parameter functions (only two 'scaling' parameters):

JD, Moore, Stadel,
MNRAS, 2004



more fitting functions

2 parameter functions (only two 'scaling' parameters):

NFW

$$\rho = \frac{\rho_s}{x(1+x)^2}$$

$$x = r/r_s$$

Moore et al 1999

$$\rho = \frac{\rho_s}{x^{1.5}(1+x)^{1.5}}$$

3 parameter functions (one additional 'profile shape' parameter):

gamma model (cusp)

JD, Moore, Stadel, 2004

$$\rho_G(r) = \frac{\rho_s}{(r/r_s)^\gamma (1 + (r/r_s)^\alpha)^{(\beta-\gamma)/\alpha}}$$

$$\alpha = 1, \beta = 3$$

Sersic/Einasto (core)

Navarro etal 2004

Merrit etal 2005/2006

$$\rho(r) = \rho_e \exp \left\{ -d_n \left[(r/r_e)^{1/n} - 1 \right] \right\}$$

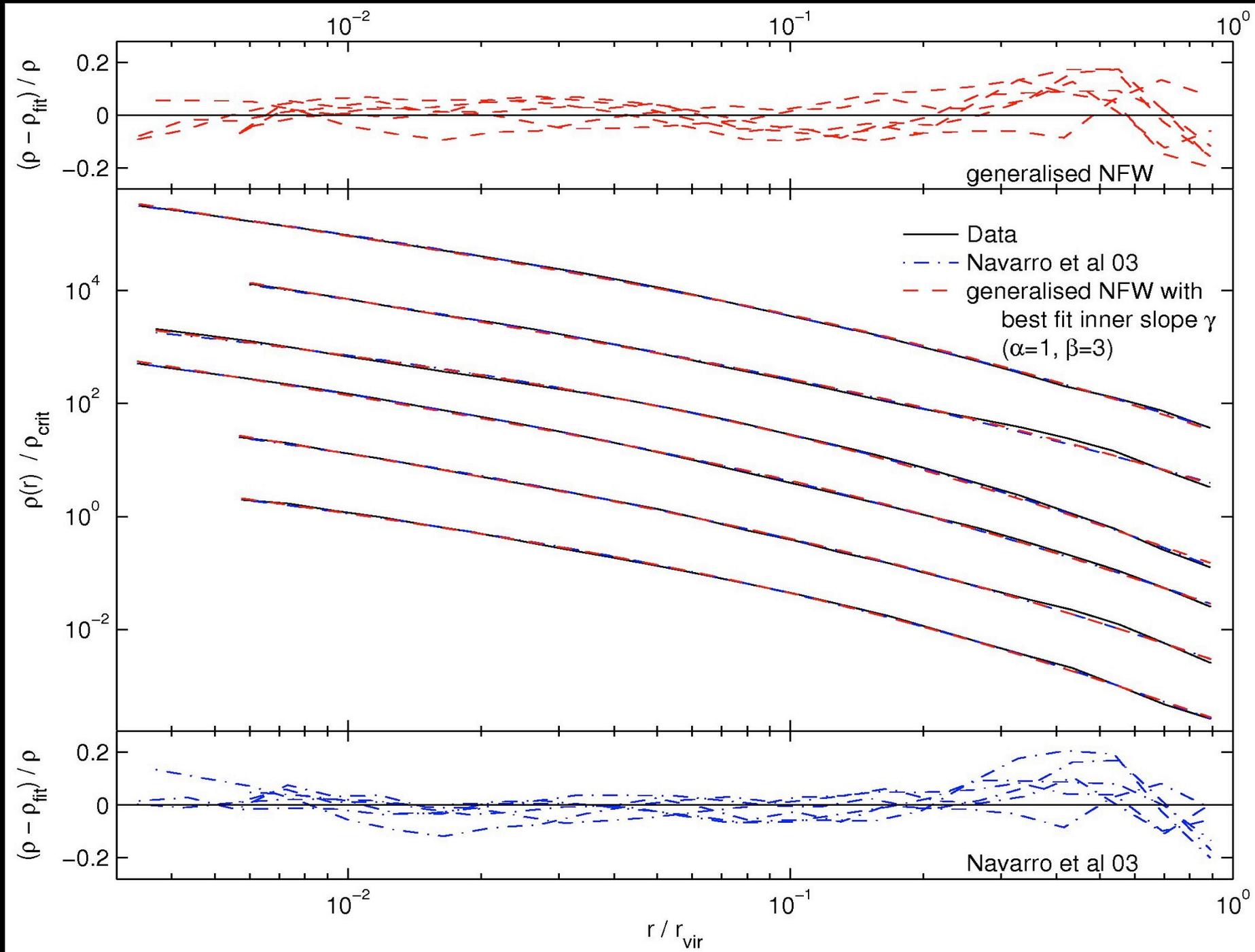
Prugniel-Simien (deprojected Sersic)

Merritt, Navarro, Ludlow, Jenkins, 2005

Merritt, Graham, Moore, JD, Terzic, 2006

Graham etal 2006

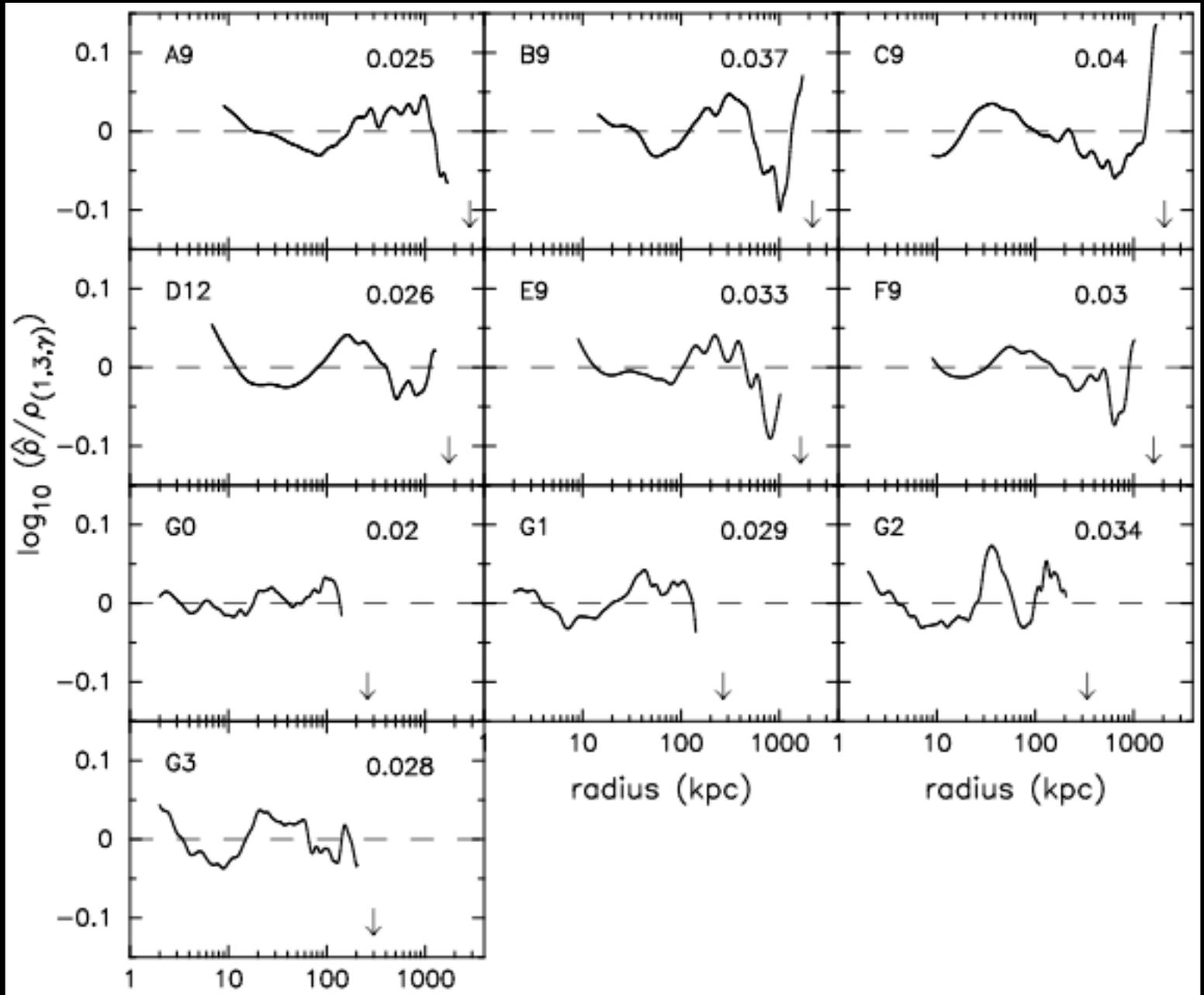
$$\rho(r) = \rho' \left(\frac{r}{R_e} \right)^{-p} \exp \left[-b (r/R_e)^{1/n} \right]$$



3 parameter functions (one additional 'profile shape' parameter):

gamma-model

fitted to
non-parametric
density profiles



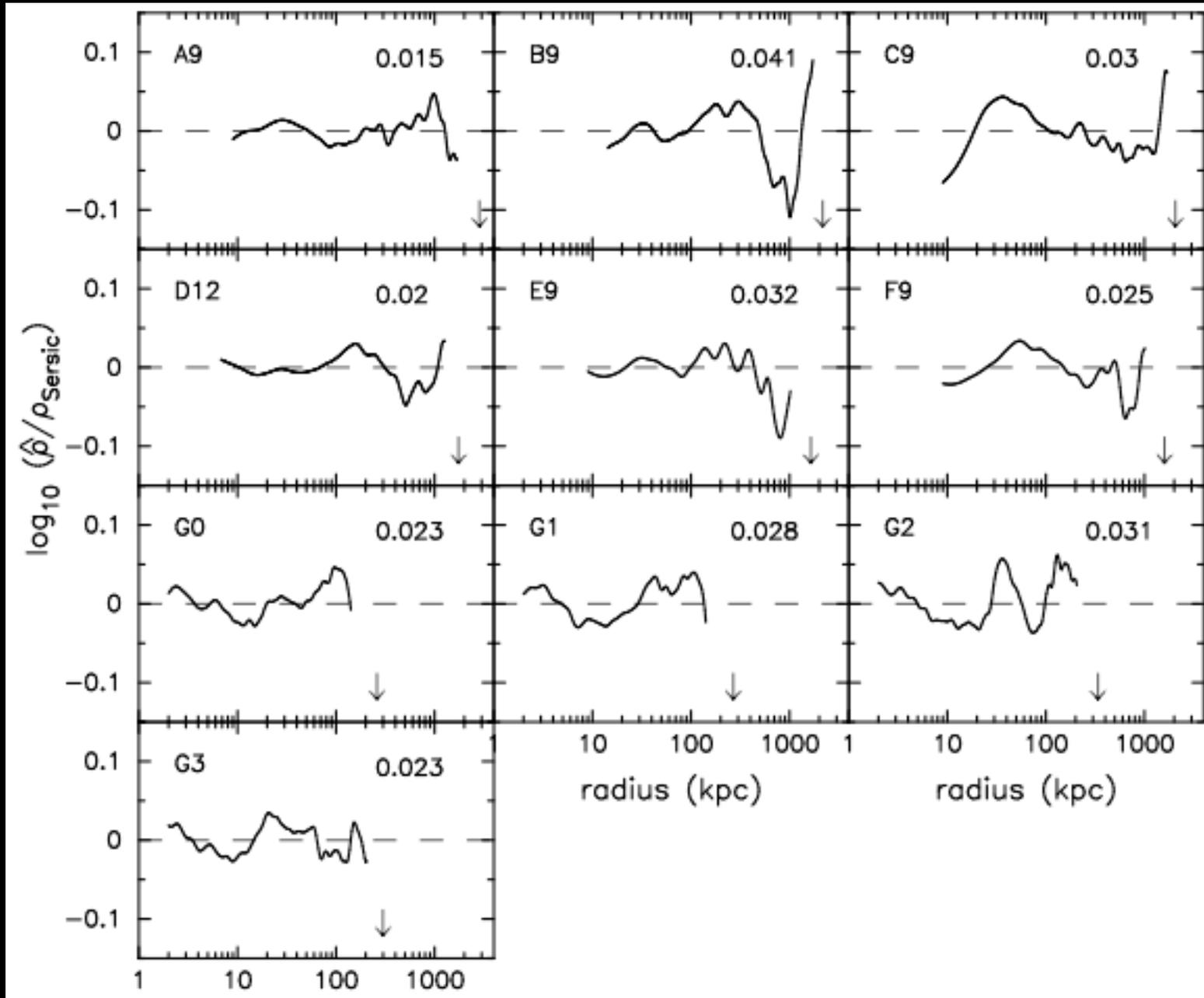
3 parameter functions (one additional 'profile shape' parameter):

Sersic-model

rms deviations
are often
smaller than
for the
gamma-model

both have largest
deviations in the
outer halo

which one fits the
inner halo better?



resolving the very inner profile

JD, Zemp, Moore, Stadel, Carollo,
MNRAS, 2005, 364, 665

physical time-steps:

the empirical $\Delta t_i < \eta \sqrt{\epsilon/a_i}$, $\eta=0.25$ is no longer sufficient

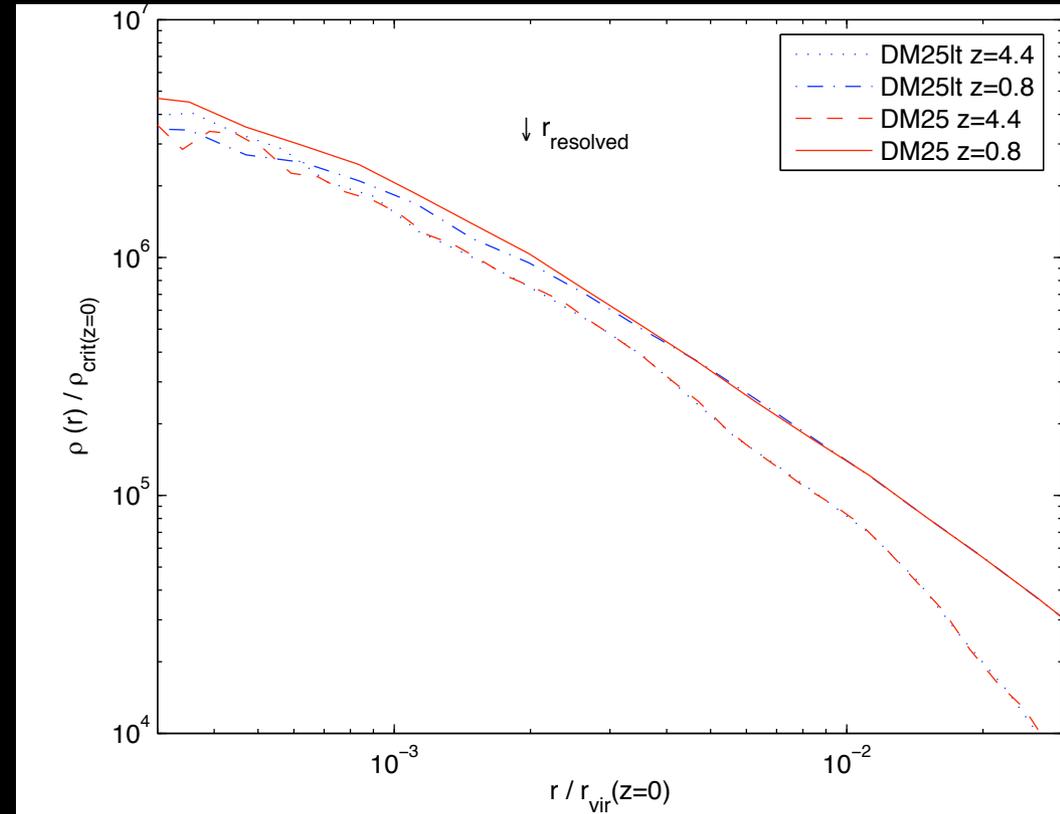
using $\Delta t < \min(\eta \sqrt{\epsilon/a_i}, \eta/4 \sqrt{G\rho_i})$ instead

this ensures step are at least 12 times smaller than the local dynamical time

$$1/\sqrt{G\rho(< r_i)}$$

but increases CPU time by a factor of two

recently Zemp, Stadel, Moore, Carollo (2006) have implemented a more efficient algorithm which scales with the local dynamical time everywhere.



summary : density profiles

CDM density profile shapes are not exactly universal:

inner slopes at a give fraction of the scale radius have about 0.2 rms halo to halo scatter

outer slopes (near R_{vir}) are very noisy

most CDM clusters are denser than NFW at $0.01 R_{\text{vir}}$, but not as dense as the Moore et al 1999 fit

CDM cluster profiles resolved with around 20 million particles can be fitted equally well with a cuspy gamma-model and with the cored Sersic function

the one halo resolved with substantially higher mass, force and time-resolution is consistent with a -1.2 cusp.

its inner halo is denser than the best fit Sersic-model