
Z-peak Subtracted Representation of Bhabha Scattering and Search for New Physics Effects at the NLC

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Introduction and Outline

- Z -peak subtracted representation ($f \neq e$) of $e^+e^- \rightarrow f\bar{f}$ at LEP2 and NLC energies
- Universal (AGC, TC) and non Universal (CT, ED) New Physics models
- Z -peak representation of Bhabha scattering $e^+e^- \rightarrow e^+e^-$

General Features of New Physics Effects off the Z Peak

- **At** the Z peak
 - Peskin - Takeuchi (S, T) or Altarelli - Barbieri ϵ_1, ϵ_3
 - Conditions for universality
 - box diagrams can be neglected
 - s channel γ exchange can be neglected
- **Off** the Z peak (LEP2, NLC, $\mu^+ \mu^-$): Generic New Physics
 - Complicated dependence on the kinematical variables (s, θ)
 - box diagrams and s channel γ exchange are important
- **Off** the Z peak: Universal New Physics
 - **Only 3** functions $\delta_\gamma, \delta_s, \delta_Z$ of the energy (constants ?)

The Z-peak Subtracted Representation ($f \neq e$)
 F.M. Renard and C. Verzeqgnassi, PRD52, 1369 (1995), PRD53, 1290 (1996)

- The general $e^+e^- \rightarrow f\bar{f}$ ($f \neq e$) scattering amplitude at one loop is the sum of an **effective photon** and an **effective Z amplitude** with couplings $g_{Vj}^\gamma(q^2, \theta)$, $g_{Vj}^Z(q^2, \theta)$, $g_{Aj}^Z(q^2, \theta)$ (j is the initial electron $j = e$ or the final fermion $j = f \neq e$)

$$\mathcal{A}(q^2, \theta) = \frac{i}{q^2} \bar{v} \gamma^\mu g_{Ve}^{(\gamma)}(q^2, \theta) u \cdot \bar{u} \gamma_\mu g_{Vf}^{(\gamma)}(q^2, \theta) v + \frac{i}{q^2 - M_Z^2 + iM_Z \Gamma_Z} \cdot \bar{v} \gamma^\mu [g_{Ve}^{(Z)}(q^2, \theta) - g_{Ae}^{(Z)}(q^2, \theta) \gamma^5] u \cdot \bar{u} \gamma_\mu [g_{Vf}^{(Z)}(q^2, \theta) - g_{Af}^{(Z)}(q^2, \theta) \gamma^5] v$$

– Effective couplings ($\tilde{\Delta}_{\alpha,ef}$, R_{ef} and V_{ef} are finite and gauge invariant)

$$g_{V_e}^\gamma(q^2, \theta) = \sqrt{4\pi\alpha(0)} Q_e [1 + \frac{1}{2}\tilde{\Delta}_{\alpha,ef}(q^2, \theta)]$$

$$g_{V_f}^\gamma(q^2, \theta) = \sqrt{4\pi\alpha(0)} Q_f [1 + \frac{1}{2}\tilde{\Delta}_{\alpha,ef}(q^2, \theta)]$$

$$g_{A_e}^\gamma(q^2, \theta) = g_{A_f}^\gamma(q^2, \theta) = 0$$

$$g_{V_e}^Z = \gamma_e^{\frac{1}{2}} I_{3e} \tilde{v}_e [1 - \frac{1}{2}R_{ef}(q^2, \theta) - \frac{4\tilde{s}_e\tilde{c}_e}{\tilde{v}_e} |Q_f| V_{ef}^{\gamma Z}(q^2, \theta)]$$

$$g_{V_f}^Z(q^2, \theta) = \gamma_f^{\frac{1}{2}} I_{3f} \tilde{v}_f [1 - \frac{1}{2}R_{ef}(q^2, \theta) - \frac{4\tilde{s}_e\tilde{c}_e}{\tilde{v}_f} |Q_f| V_{ef}^{Z\gamma}(q^2, \theta)]$$

$$g_{A_e}^Z(q^2, \theta) = \gamma_e^{\frac{1}{2}} I_{3e} [1 - \frac{1}{2}R_{ef}(q^2, \theta)]$$

$$g_{A_f}^Z(q^2, \theta) = \gamma_f^{\frac{1}{2}} I_{3f} [1 - \frac{1}{2}R_{ef}(q^2, \theta)]$$

with the Z -peak inputs

$$\gamma_j^{\frac{1}{2}} = \left[\frac{48\pi\Gamma_j}{N_j M_Z (1 + \tilde{v}_j^2)} \right]^{\frac{1}{2}} = \frac{e}{2sc} + \dots$$

$$\tilde{v}_j = 1 - 4|Q_j| \tilde{s}_j^2$$

- $\tilde{s}_j^2 = 1 - \tilde{c}_j^2$ is the **weak effective angle** measured through the forward-backward or polarization asymmetries in the final channel j , $\tilde{s}_e \equiv \tilde{s}_\mu \equiv \tilde{s}_\tau$
- The quantities $\tilde{\Delta}_{\alpha,ef}(q^2, \theta)$, $R_{ef}(q^2, \theta)$, $V_{ef}^{\gamma Z}(q^2, \theta)$, $V_{ef}^{Z\gamma}(q^2, \theta)$ contain all the q^2 , θ dependent parts of the scattering amplitude due to SM or NP at one-loop.
 - They are **finite, gauge independent** combinations of self-energies, vertices and boxes

– For an additional four fermion amplitude with Lorentz structure

$$\bar{v}(e^+) \gamma^\mu [a(q^2, \theta) - b(q^2, \theta) \gamma^5] u(e^-) \cdot \bar{u}(f) \gamma_\mu [c(q^2, \theta) - d(q^2, \theta) \gamma^5] v(f)$$

and a, b, c, d representing $\mathcal{O}(\alpha)$ effects, we have

$$\tilde{\Delta}_{\alpha,ef}(q^2, \theta) = \mathbf{q}^2 \frac{[a(q^2, \theta) - b(q^2, \theta) \tilde{v}_e][c(q^2, \theta) - d(q^2, \theta) \tilde{v}_f]}{e^2 Q_e Q_f}$$

$$R_{ef}(q^2, \theta) = -(\mathbf{q}^2 - \mathbf{M}_Z^2) \frac{4\tilde{s}_e^2 \tilde{c}_e^2 b(q^2, \theta) d(q^2, \theta)}{e^2 I_{3e} I_{3f}}$$

$$V_{ef}^{\gamma Z}(q^2, \theta) = -(\mathbf{q}^2 - \mathbf{M}_Z^2) \frac{[a(q^2, \theta) - b(q^2, \theta) \tilde{v}_e] 2\tilde{s}_e \tilde{c}_e d(q^2, \theta)}{e^2 Q_e I_{3f}}$$

$$V_{ef}^{Z\gamma}(q^2, \theta) = -(\mathbf{q}^2 - \mathbf{M}_Z^2) \frac{[c(q^2, \theta) - d(q^2, \theta) \tilde{v}_f] 2\tilde{s}_e \tilde{c}_e b(q^2, \theta)}{e^2 Q_f I_{3e}}$$

Differential Unpolarized Cross Sections

$$\frac{d\sigma_{lf}}{d\cos\theta} = \frac{4\pi}{3} N_f q^2 \left\{ \frac{3}{8} (1 + \cos^2\theta) \mathbf{U}_{11} + \frac{3}{4} \cos\theta \mathbf{U}_{12} \right\}$$

where (apart from α redefinition)

$$U_{11} = \gamma\gamma + (\gamma Z + ZZ)(1 + \mathbf{A}_e \mathbf{A}_f + \mathbf{A}_e + \mathbf{A}_f)$$

$$U_{12} = \gamma Z(1 + \mathbf{A}_e \mathbf{A}_f) + ZZ(1 + \mathbf{A}_e \mathbf{A}_f + \mathbf{A}_e + \mathbf{A}_f)$$

$$\begin{aligned} U_{11} = & \frac{\alpha^2(0)Q_f^2}{q^4} [1 + 2\tilde{\Delta}_{\alpha,lf}(q^2, \theta)] \\ & + 2[\alpha(0)|Q_f|] \frac{q^2 - M_Z^2}{q^2((q^2 - M_Z^2)^2 + M_Z^2\Gamma_Z^2)} \left[\frac{3\Gamma_l}{M_Z} \right]^{1/2} \left[\frac{3\Gamma_f}{N_f M_Z} \right]^{1/2} \frac{\tilde{v}_l \tilde{v}_f}{(1 + \tilde{v}_l^2)^{1/2} (1 + \tilde{v}_f^2)^{1/2}} \\ & \times [1 + \tilde{\Delta}_{\alpha,lf}(q^2, \theta) - R_{lf}(q^2, \theta) - 4\tilde{s}_l \tilde{c}_l \left\{ \frac{1}{\tilde{v}_l} V_{lf}^{\gamma Z}(q^2, \theta) + \frac{|Q_f|}{\tilde{v}_f} V_{lf}^{Z\gamma}(q^2, \theta) \right\}] \end{aligned}$$

$$\begin{aligned}
& + \frac{[\frac{3\Gamma_l}{M_Z}][\frac{3\Gamma_f}{N_f M_Z}]}{(q^2 - M_Z^2)^2 + M_Z^2 \Gamma_Z^2} \\
& \times [1 - 2R_{lf}(q^2, \theta) - 8\tilde{s}_l \tilde{c}_l \{ \frac{\tilde{v}_l}{1 + \tilde{v}_l^2} V_{lf}^{\gamma Z}(q^2, \theta) + \frac{\tilde{v}_f |\mathcal{Q}_f|}{(1 + \tilde{v}_f^2)} V_{lf}^{Z\gamma}(q^2, \theta) \}] \\
U_{12} = & 2[\alpha(0)|\mathcal{Q}_f|] \frac{q^2 - M_Z^2}{q^2((q^2 - M_Z^2)^2 + M_Z^2 \Gamma_Z^2)} [\frac{3\Gamma_l}{M_Z}]^{1/2} [\frac{3\Gamma_f}{N_f M_Z}]^{1/2} \frac{1}{(1 + \tilde{v}_l^2)^{1/2} (1 + \tilde{v}_f^2)^{1/2}} \\
& \times [1 + \tilde{\Delta}_{\alpha, lf}(q^2, \theta) - R_{lf}(q^2, \theta)] \\
& + \frac{[\frac{3\Gamma_l}{M_Z}][\frac{3\Gamma_f}{N_f M_Z}]}{(q^2 - M_Z^2)^2 + M_Z^2 \Gamma_Z^2} \left[\frac{4\tilde{v}_l \tilde{v}_f}{(1 + \tilde{v}_l^2)(1 + \tilde{v}_f^2)} \right] \\
& \times [1 - 2R_{lf}(q^2, \theta) - 4\tilde{s}_l \tilde{c}_l \{ \frac{1}{\tilde{v}_l} V_{lf}^{\gamma Z}(q^2, \theta) + \frac{|\mathcal{Q}_f|}{\tilde{v}_f} V_{lf}^{Z\gamma}(q^2, \theta) \}]
\end{aligned}$$

New Physics Contributions

- For a general one loop New Physics effect the form factors $\tilde{\Delta}_{\alpha,l,f}$, $R_{l,f}$, $V_{l,f}^{\gamma Z}$ and $V_{l,f}^{Z\gamma}$ are shifted

$$\tilde{\Delta}_{\alpha,l,f}(q^2, \theta) \rightarrow \tilde{\Delta}_{\alpha,l,f}(q^2, \theta) + \tilde{\Delta}_{\alpha,l,f}^{NP}(q^2, \theta)$$

- Explicit θ dependent terms (e.g. from SUSY boxes) introduce **new** parameters (# of terms $\cos^N \theta$)
- Simplifications occur for **Universal New Physics**
 - independent on the final fermion family f
 - independent on θ

$$\tilde{\Delta}_{\alpha}^{UNP}(q^2) \quad R^{UNP}(q^2) \quad V^{UNP}(q^2)$$

- If the q^2 dependence is **factorized**, then measurements at different q^2 can be combined

Definition of the Three δ Parameters

- By construction
$$\tilde{\Delta}_\alpha^{UNP}(0) = R^{UNP}(M_Z^2) = V^{UNP}(M_Z^2) = 0$$
- We therefore introduce the three dimensionless functions $\delta_{z,s,\gamma}(q^2)$

$$R^{UNP}(q^2) = \frac{(q^2 - M_Z^2)}{M_Z^2} \delta_z \quad V^{UNP}(q^2) = \frac{(q^2 - M_Z^2)}{M_Z^2} \delta_s \quad \tilde{\Delta}_\alpha^{UNP}(q^2) = \frac{q^2}{M_Z^2} \delta_\gamma$$

- For large New Physics scales ($\Lambda^2 \gg q^2$), we find typically $\delta_i(q^2) = (q^2)^{m_i} \hat{\delta}_i(q^2)$ and, in some cases, $\hat{\delta}_i(q^2) \simeq \hat{\delta}_i(0)$
- Non Universality can occur by a θ dependence, a final flavour dependence, both.

Z-peak Representation of the Bhabha Process

- The scattering amplitude at one loop is the sum of two (s-channel and t-channel) components

$$\mathcal{A}_{ee} = \mathcal{A}_s(q^2, \theta) + \mathcal{A}_t(q^2, \theta)$$

- Definition of effective couplings in the t-channel component

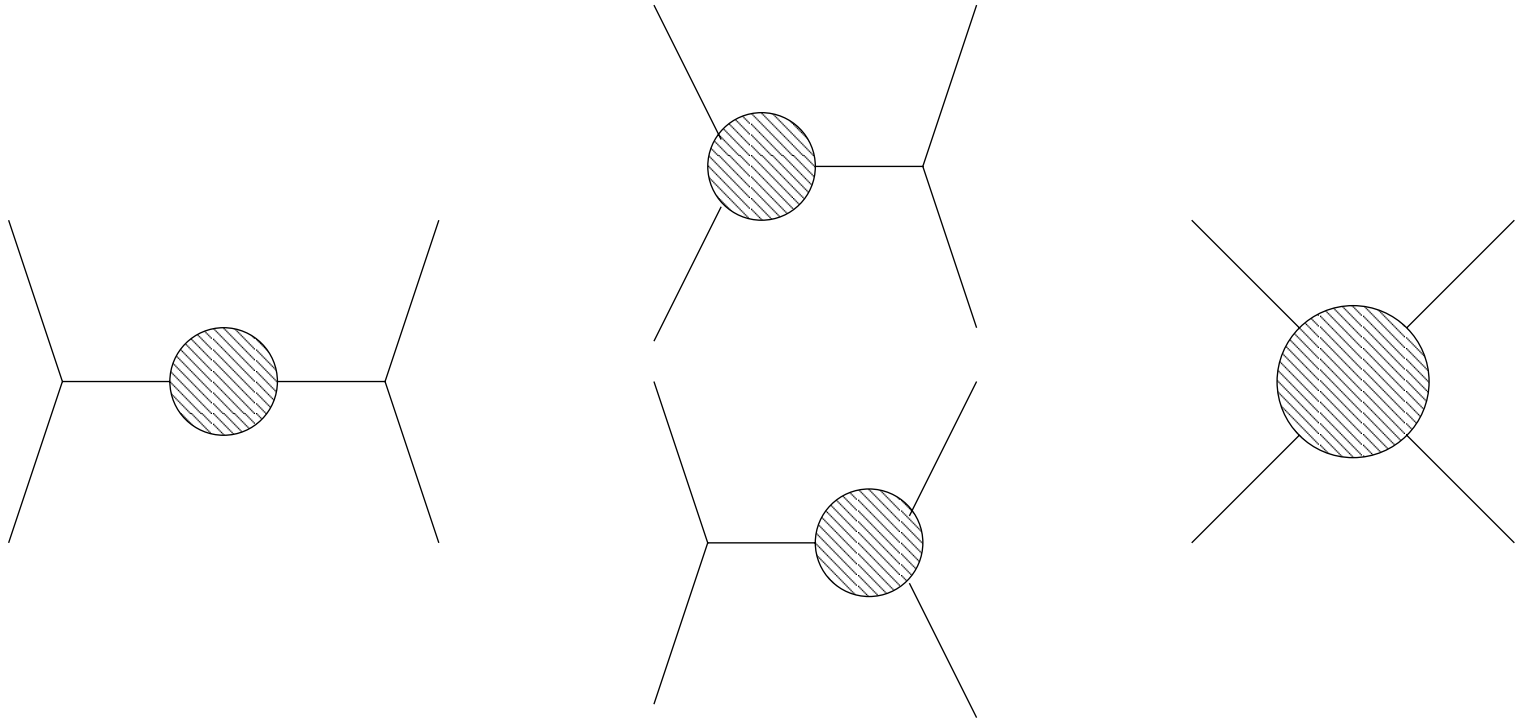
$$\begin{aligned} \mathcal{A}_t(q^2, \theta) &= \frac{i}{t} \bar{v} \gamma^\mu \bar{g}_{Ve}^{(\gamma)}(q^2, \theta) v \cdot \bar{u} \gamma_\mu \bar{g}_{Vf}^{(\gamma)}(q^2, \theta) + \frac{i}{t - M_Z^2} \cdot \\ &\bar{v} \gamma^\mu [\bar{g}_{Ve}^{(Z)}(q^2, \theta) - \bar{g}_{Ae}^{(Z)}(q^2, \theta) \gamma^5] \cdot \bar{u} \gamma_\mu [\bar{g}_{Vf}^{(Z)}(q^2, \theta) - \bar{g}_{Af}^{(Z)}(q^2, \theta) \gamma^5] u \end{aligned}$$

– t -channel effective couplings

$$\begin{aligned}
\bar{g}_{V_e}^\gamma(q^2, \theta) &= \sqrt{4\pi\alpha(0)} Q_e \left[1 + \frac{1}{2} \bar{\Delta}_\alpha(q^2, \theta) \right] \\
\bar{g}_{V_e}^Z(q^2, \theta) &= \gamma_e^{\frac{1}{2}} I_{3e} \tilde{v}_e \left[1 - \frac{1}{2} \bar{R}(q^2, \theta) - \frac{4\tilde{s}_e \tilde{c}_e}{\tilde{v}_e} |Q_f| \bar{V}(q^2, \theta) \right] \\
\bar{g}_{A_e}^Z(q^2, \theta) &= \gamma_e^{\frac{1}{2}} I_{3e} \left[1 - \frac{1}{2} \bar{R}(q^2, \theta) \right]
\end{aligned} \tag{1}$$

– The new functions $\bar{\Delta}_\alpha(q^2, \theta)$, $\bar{R}(q^2, \theta)$ and $\bar{V}(q^2, \theta)$ are obtained from the s -channel by crossing $s \longleftrightarrow t$

$$q^2 \longrightarrow t = -\frac{q^2}{2}(1 - \cos\theta) \quad \cos\theta \longrightarrow 1 + \frac{2q^2}{t}$$



A rotated copy of the same diagrams occur in $e^+e^- \rightarrow e^+e^-$

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- General expression of the polarized Bhabha differential cross section (P and P' are the initial e^- , e^+ polarizations)

$$\frac{d\sigma}{d\cos\theta} = (1 - PP') \frac{d\sigma^1}{d\cos\theta} + \underbrace{(1 + PP') \frac{d\sigma^2}{d\cos\theta} + (P' - P) \frac{d\sigma^P}{d\cos\theta}}_{\text{t channel only}}$$

- unpolarized angular distribution: the only one relevant at LEP2

$$\frac{d\sigma}{d\cos\theta} \equiv \frac{d\sigma^1}{d\cos\theta} + \frac{d\sigma^2}{d\cos\theta}$$

- LL-RR and LL+RR polarization asymmetries: specific of NLC

$$A_{LR}(q^2, \theta) = \left[\frac{d\sigma^P}{d\cos\theta} \right] / \left[\frac{d\sigma}{d\cos\theta} \right] \quad A_{\parallel}(q^2, \theta) = \left[\frac{d\sigma^2}{d\cos\theta} \right] / \left[\frac{d\sigma}{d\cos\theta} \right]$$

Parametrization of New Physics Effects in the Bhabha Observables

- General New Physics \implies duplication of the parameters
- Universal New Physics \implies the same set of three numbers
- General definition of δ , including contributions to Bhabha

$$R^{UNP}(z) = \frac{(z - M_Z^2)}{M_Z^2} \delta_Z$$

$$V^{UNP}(z) = \frac{(z - M_Z^2)}{M_Z^2} \delta_s$$

$$\tilde{\Delta}_\alpha^{UNP}(z) = \frac{z}{M_Z^2} \delta_\gamma$$

where $z = s, t$

Summary Table of Some Common New Physics Models

- AGC and TC are Universal
- CT are Universal in each flavour (e.g. $e^+e^- \rightarrow l\bar{l}$)
- For ED and SUSY, δ are functions of θ , not constants
- For SUSY, the condition $\Lambda^2 \gg q^2$ is not interesting.

Model	Universal	θ	f	m
AGC	X			
TC	X			
CT			X	
ED		X	X	1
(SUSY)		X	X	?

Universal New Physics I: Anomalous gauge couplings

A. Blondel, F. M. Renard, L. Trentadue and C. Verzegnassi PRD 54 (1996)

dim=6, $SU(2) \times U(1)$ and CP conserving operators, linear Higgs (Hagiwara et al., PRD 48 (1993))

	W^2	Z^2	AZ	A^2	$W^2 Z$	$W^2 A$	W^4	$W^2 Z^2$	$W^2 ZA$	$W^2 A^2$	Z^4
DW	x	x	x	x	x	x	x	x	x	x	
DB		x	x	x							
BW		x	x	x	x	x					
$\Phi, 1$		x									
WWW					x	x	x	x	x	x	
W					x	x	x	x	x		
B					x	x					

$e^+ e^- \rightarrow f \bar{f}$ versus $e^+ e^- \rightarrow W^+ W^-$ at LEP2

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- The effect of the “tree level” operators parametrized by f_{DW} , f_{DB} , f_{BW} and $f_{\Phi,1}$ receives contributions from the “one loop” operators, e.g.

$$f_{DW}^r = f_{DW} - \frac{1}{192\pi^2} \left(f_W \log \frac{\Lambda^2}{M_W^2} + \frac{f_B - f_W}{4} \log \frac{M_H^2}{M_W^2} \right)$$

$$f_{DB}^r = f_{DB} - \frac{1}{192\pi^2} \left(f_B \log \frac{\Lambda^2}{M_W^2} - \frac{f_B - f_W}{4} \log \frac{M_H^2}{M_W^2} \right)$$

- The couplings f_{DW} , f_{DB} , f_{BW} and $f_{\Phi,1}$ are well constrained by amplitudes with external fermions at LEP1 and LEP2. Results from a 500 pb^{-1} @ 175 GeV conventional 4 parameters fit

	DW	DB	BW	$\Phi,1$	WWW	W	B
$f\bar{f}$	0.22	1.9	0.46	0.042			
W^+W^-	2.1	12	1.5	0.19	10	7.1	46

– If they are excluded from $e^+e^- \rightarrow f\bar{f}$ then we can study

$$\frac{i\mathcal{L}}{g_{WWV}} = g_1^V V_\mu (W^{-\mu\nu} W_\nu^+ - W^{+\mu\nu} W_\nu^-) + \kappa_V V^{\mu\nu} W_\mu^- W_\nu^+ + \frac{\lambda_V}{M_W^2} V^{\mu\nu} W_\nu^+ W_{\rho\mu}^-$$

with $(SU(2) \times U(1))$ gives $g_1^\gamma = 1$, $\lambda_Z = \lambda_\gamma = \lambda$ and trades κ_Z)

$$\Delta\kappa_\gamma = (f_B + f_W) \frac{M_W^2}{2\Lambda^2}$$

$$\Delta g_1^Z = f_W \frac{M_Z^2}{2\Lambda^2}$$

$$\lambda = f_{WWW} \frac{3M_W^2 g^2}{2\Lambda^2}$$

LEP2 experimental results (C. Sbarra, Moriond 2000)

$$\Delta\kappa_\gamma = 0.021_{-0.059}^{+0.063}, \quad \Delta g_1^Z = -0.024_{-0.024}^{+0.024}, \quad \lambda_\gamma = -0.016_{-0.026}^{+0.026}$$

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- Z-peak subtracted analysis: 2 parameters, f_{DW} and f_{DB} ; they give q^2 dependent contributions.
 - Expression of the δ parameters in terms of f_{DW} and f_{DB}

$$\delta_z = 8\pi\alpha \frac{M_Z^2}{\Lambda^2} \left(\frac{\tilde{c}_l^2}{\tilde{s}_l^2} f_{DW} + \frac{\tilde{s}_l^2}{\tilde{c}_l^2} f_{DB} \right), \quad \delta_s = 8\pi\alpha \frac{M_Z^2}{\Lambda^2} \left(\frac{\tilde{c}_l}{\tilde{s}_l} f_{DW} - \frac{\tilde{s}_l}{\tilde{c}_l} f_{DB} \right),$$

$$\delta_\gamma = -8\pi\alpha \frac{M_Z^2}{\Lambda^2} (f_{DW} + f_{DB}),$$

They satisfy the linear constraint:

$$\delta_z - \frac{1-2\tilde{s}_l^2}{\tilde{s}_l\tilde{c}_l} \delta_s + \delta_\gamma = 0$$

Universal New Physics II: Models of Technicolor type

R. S. Chivukula, F. M. Renard and C. Verzegnassi PRD 547 (1998)

- Strongly coupled Vector and Axial resonances. 2 parameters (ratios F/M^2)
- The Z-peak scheme leads naturally to the use of non perturbative dispersion relations
- δ parameters

$$\delta_z = M_Z^2 \frac{\pi\alpha}{\tilde{s}_l^2 \tilde{c}_l} \left((1 - 2\tilde{s}_l^2)^2 \frac{F_V^2}{M_V^4} + \frac{F_A^2}{M_A^4} \right),$$

$$\delta_s = M_Z^2 \frac{2\pi\alpha}{\tilde{s}_l \tilde{c}_l} (1 - 2\tilde{s}_l^2) \frac{F_V^2}{M_V^4}, \quad \delta_\gamma = -4\pi\alpha M_Z^2 \frac{F_V^2}{M_V^4}.$$

Again, we have a linear constraint in the $(\delta_z, \delta_s, \delta_\gamma)$ space:

$$\delta_s = - \left(\frac{1 - 2\tilde{s}_l^2}{2\tilde{s}_l \tilde{c}_l} \right) \delta_\gamma$$

$$\delta_{z,s} > 0 \quad \delta_\gamma < 0$$

Non Universal New Physics I: Contact Interactions

E. Eichten, K. Lane, M. Peskin, PRL 50 (1983)

- Composite models or any generic virtual NP effect with a high intrinsic scale (e.g., higher vector boson exchanges, satisfying chirality conservation)
- Interaction Lagrangian for ($i\bar{i} \rightarrow f\bar{f}$)

$$\begin{aligned}\mathcal{L} = & k_{if} \frac{4\pi}{\Lambda^2} \{ \eta_{LL} (\bar{\Psi}_L^i \gamma^\mu \Psi_L^i) (\bar{\Psi}_L^f \gamma_\mu \Psi_L^f) + \eta_{RR} (\bar{\Psi}_R^i \gamma^\mu \Psi_R^i) (\bar{\Psi}_R^f \gamma_\mu \Psi_R^f) \\ & + \eta_{RL} (\bar{\Psi}_R^i \gamma^\mu \Psi_R^i) (\bar{\Psi}_L^f \gamma_\mu \Psi_L^f) + \eta_{LR} (\bar{\Psi}_L^i \gamma^\mu \Psi_L^i) (\bar{\Psi}_R^f \gamma_\mu \Psi_R^f) \}\end{aligned}$$

where

$k_{if} = \frac{1}{2}$ for $i \equiv f$, $k_{if} = 1$ otherwise; $\Psi_L = (1 - \gamma^5)/2 \Psi$, $\Psi_R = (1 + \gamma^5)/2 \Psi$; η_{ab} are phase factors defining the chirality structure of the interaction.

- Specific applications can be considered for pure chiral cases (ij) = LL or RR or LR or RL (keeping only one $\eta_{ij} = \pm 1$), as well as for mixed cases like VV ($\eta_{LL} = \eta_{RR} = \eta_{RL} = \eta_{LR} = \pm 1$), AA ($\eta_{LL} = \eta_{RR} = -\eta_{RL} = -\eta_{LR} = \pm 1$), VA ($\eta_{LL} = -\eta_{RR} = \eta_{RL} = -\eta_{LR} = \pm 1$), AV ($\eta_{LL} = -\eta_{RR} = -\eta_{RL} = \eta_{LR} = \pm 1$);

– δ parameters

$$\delta_{\gamma,ef} = \frac{\pi M_Z^2}{e^2 Q_e Q_f \Lambda^2} [\eta_{LL}(1 - v_e)(1 - v_f) + \eta_{RR}(1 + v_e)(1 + v_f)$$

$$+ \eta_{RL}(1 + v_e)(1 - v_f) + \eta_{LR}(1 - v_e)(1 + v_f)]$$

$$\delta_{Z,ef} = -\frac{4\tilde{s}_e^2 \tilde{c}_e^2 \pi M_Z^2}{e^2 I_{3e} I_{3f} \Lambda^2} [\eta_{LL} + \eta_{RR} - \eta_{RL} - \eta_{LR}]$$

$$\delta_{s,ef}^{Z\gamma} = -\frac{2\tilde{s}_e \tilde{c}_e \pi M_Z^2}{e^2 Q_e I_{3f} \Lambda^2} [\eta_{LL}(1 - v_e) - \eta_{RR}(1 + v_e) + \eta_{RL}(1 + v_e) - \eta_{LR}(1 - v_e)]$$

$$\delta_{s,ef}^{Z\gamma} = -\frac{2\tilde{s}_e \tilde{c}_e \pi M_Z^2}{e^2 Q_f I_{3e} \Lambda^2} [\eta_{LL}(1 - v_f) - \eta_{RR}(1 + v_f) - \eta_{RL}(1 - v_f) + \eta_{LR}(1 + v_f)]$$

– Since there is a single parameter, the bounds on $\delta_{Z,s,\gamma}$ translates into a bound on the New Physics coupling

Non Universal New Physics II: Extra Dimensions

N. Arkani-Hamed, S. Dimopoulos, G. Dvali, PLB 429 (1998), PLB 436 (1998)

– Arkani-Hamed, Dimopoulos, Dvali model ($M_{Pl} \sim 10^{19}$ GeV, $M_S \sim 10^2$ GeV)

$$M_{Pl}^2 \sim M_S^{n+2} R^n$$

– $n = 1$, $R \sim$ solar system;

$n = 2$, $R = 0.1 - 1$ mm

– Coupling to KK modes

$$\frac{1}{M_{Pl}} \times \# \text{ modes} \sim \frac{1}{M_S}$$

– Lorentz structure of the matrix element

$$\frac{\lambda}{\Lambda^4} [\bar{e} \gamma^\mu e \bar{f} \gamma_\mu f (p_2 - p_1) \cdot (p_4 - p_3) - \bar{e} \gamma^\mu e \bar{f} \gamma^\nu f (p_2 - p_1)_\nu (p_4 - p_3)_\mu]$$

– δ parameters

$$\delta_{z,ef} = -\left(\frac{\lambda M_Z^2 q^2}{\Lambda^4}\right) \frac{4\tilde{s}_l^2 \tilde{c}_l^2}{e^2 I_{3e} I_{3f}}$$

$$\delta_{s,ef}^{Z\gamma} = \left(\frac{\lambda M_Z^2 q^2}{\Lambda^4}\right) \frac{2\tilde{s}_l \tilde{c}_l \tilde{v}_l}{e^2 Q_e I_{3f}}$$

$$\delta_{s,ef}^{Z\gamma} = \left(\frac{\lambda M_Z^2 q^2}{\Lambda^4}\right) \frac{2\tilde{s}_l \tilde{c}_l \tilde{v}_f}{e^2 Q_f I_{3e}}$$

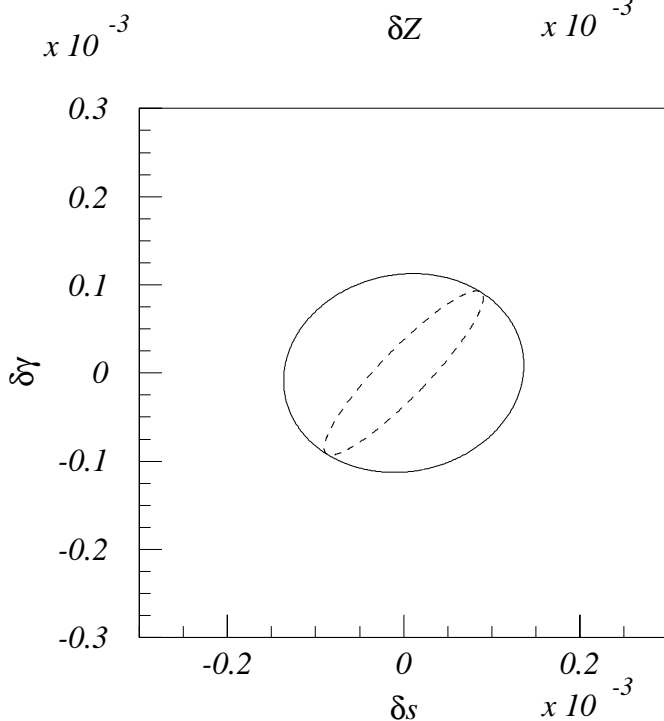
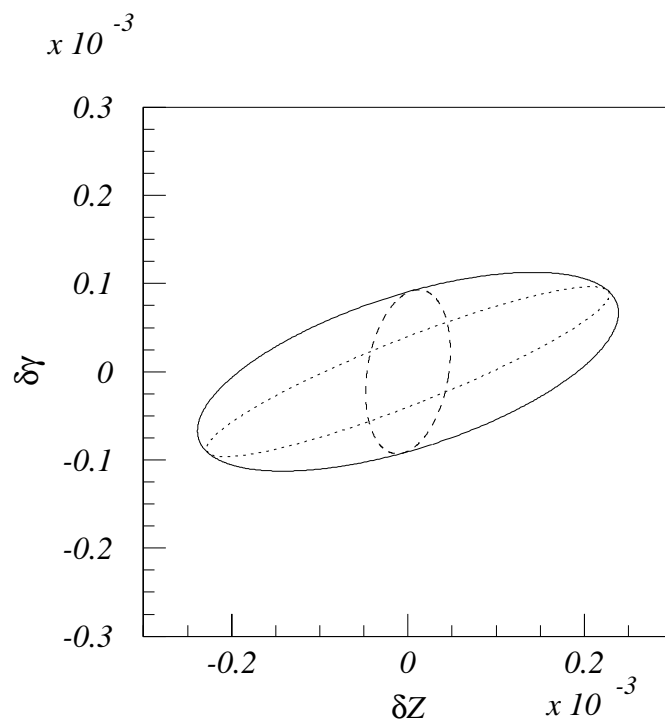
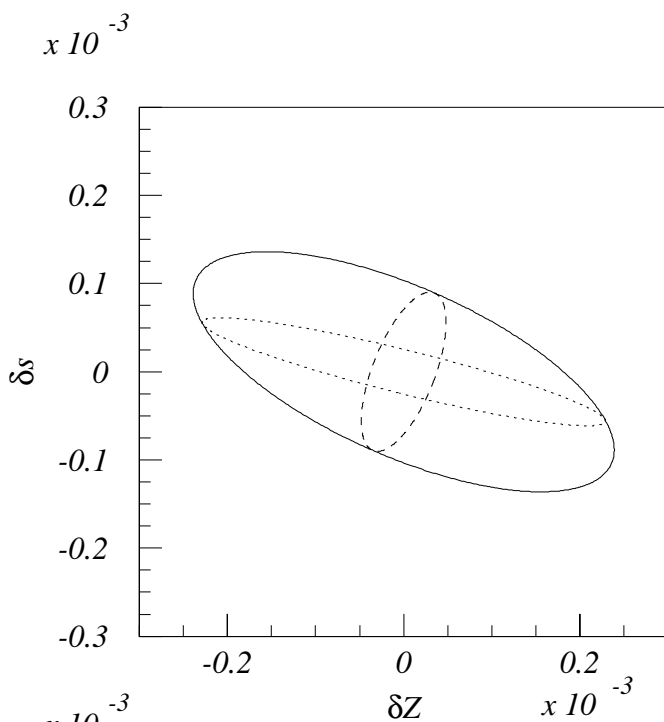
$$\delta_{\gamma,ef} = \left(\frac{\lambda M_Z^2 q^2}{\Lambda^4}\right) \frac{(\tilde{v}_l \tilde{v}_f - 2\cos\theta)}{e^2 Q_e Q_f}$$

- The q^2 factor is purely kinematical and a consequence of the higher dimension of the interaction Lagrangian
- The term proportional to $\cos\theta$ gives a contribution in the t -channel with **large interference** effects with the standard **photon exchange** amplitude.

Definition of the Observables

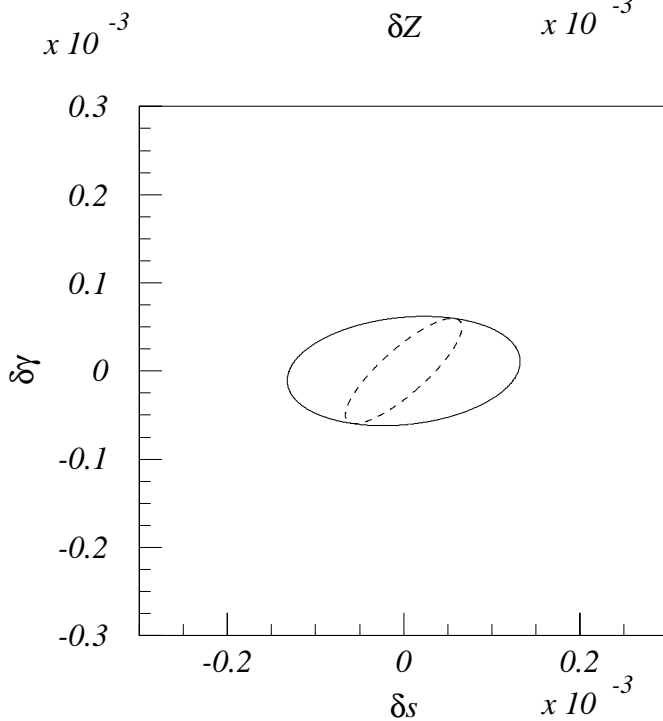
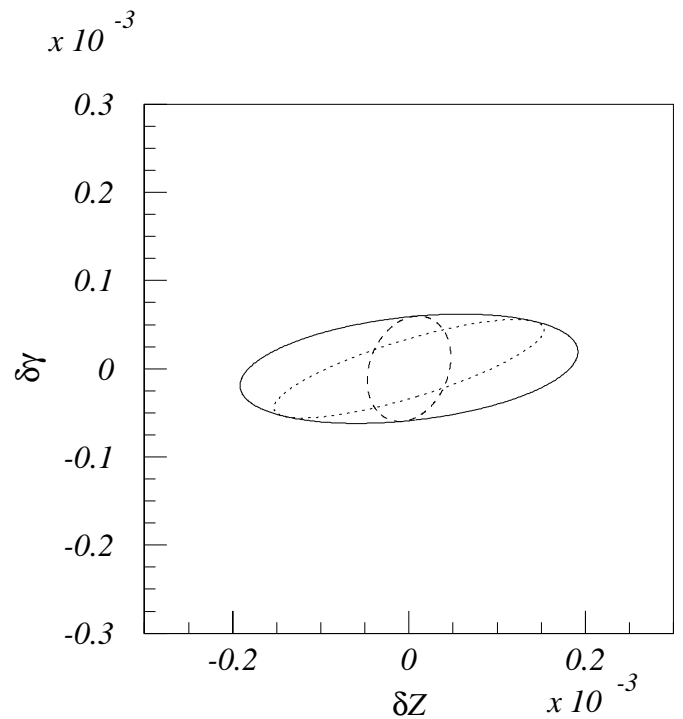
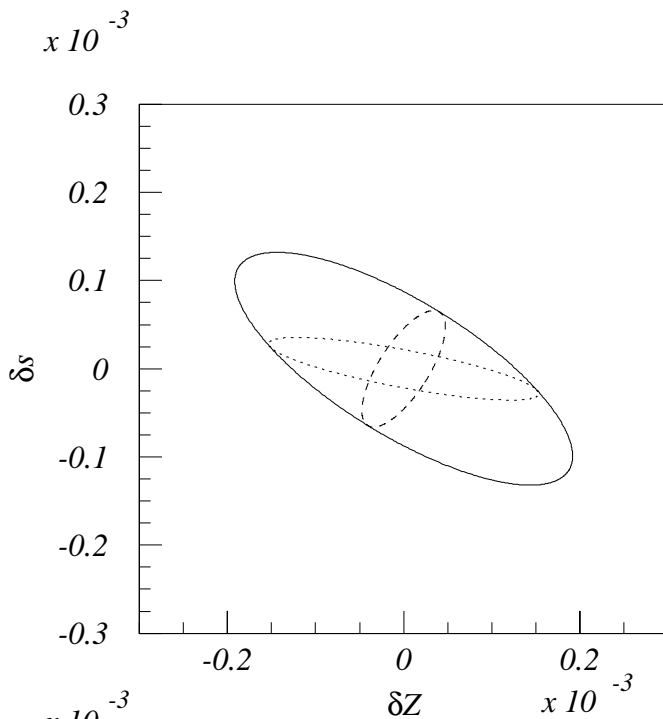
- Non Bhabha: $\sigma_l, \sigma_5, A_{FB,l}, A_{LR,l}$ @ $\sqrt{s} = 500$ GeV, $\mathcal{L} = 500 \text{ fb}^{-1}$
- Bhabha: $\sigma, A_{LR}, A_{||}$ in 9 angular bins $-0.9 < \cos\theta_{e^-} < 0.9$
- The theoretical error: situation at LEP2
 - For the non Bhabha observables, $\varepsilon_{th} < \varepsilon_{exp}$ is $< 1\%$, dominated by large QED corrections.
 - For the Bhabha cross section, $\varepsilon_{th} \simeq 2\%$ larger than the experimental error in the very forward cone.

Bounds on δ without Bhabha



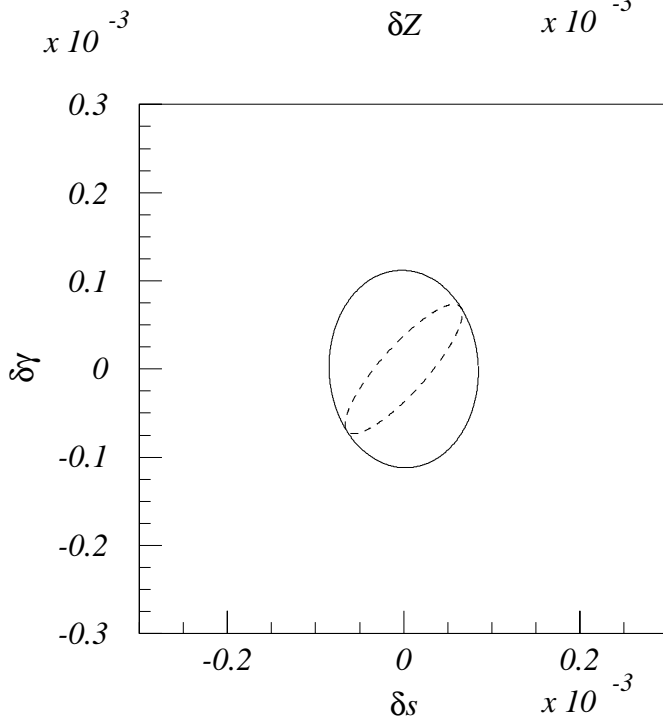
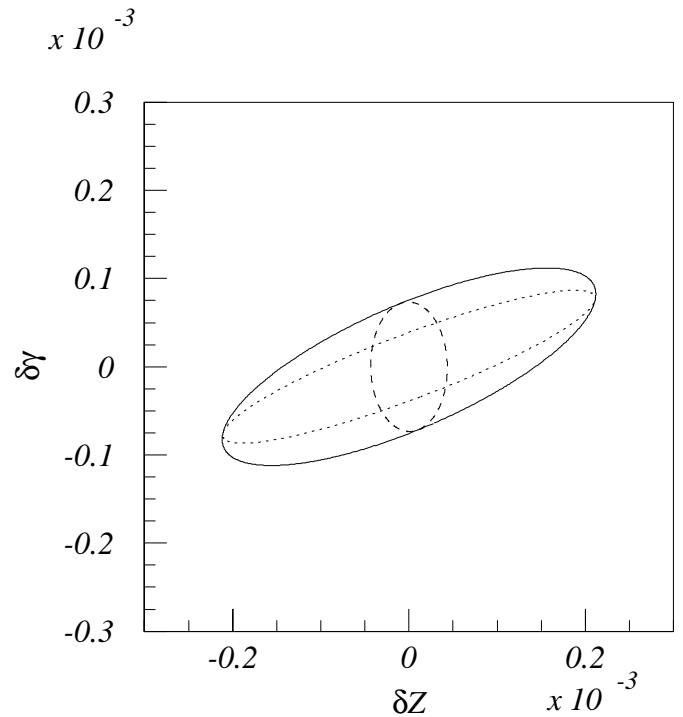
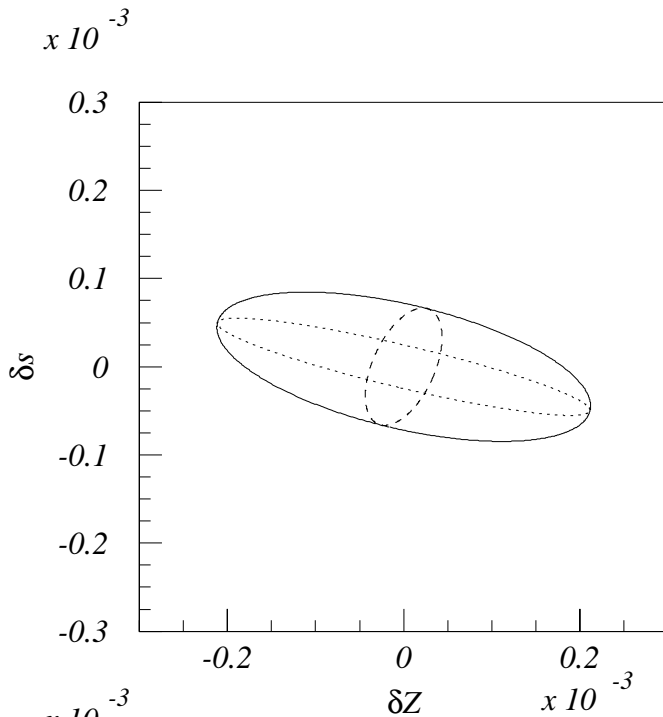
Bounds on δ

with unpolarized Bhabha σ



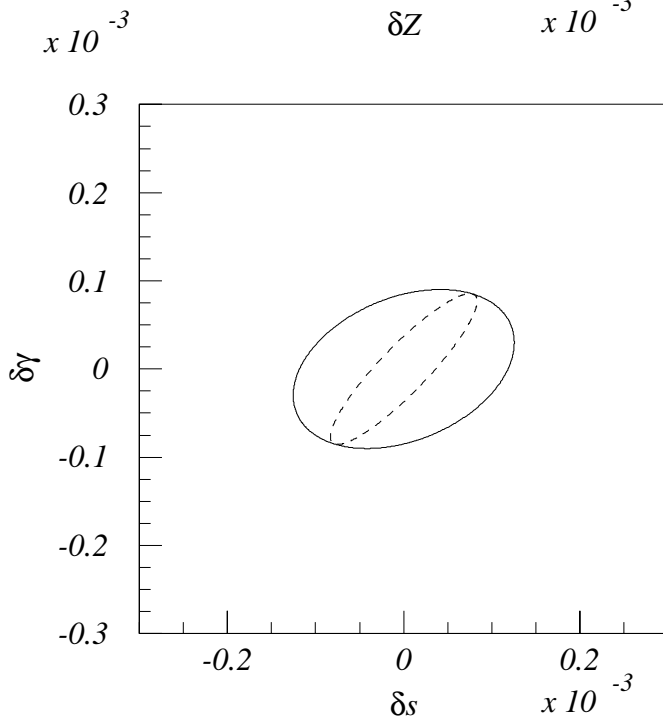
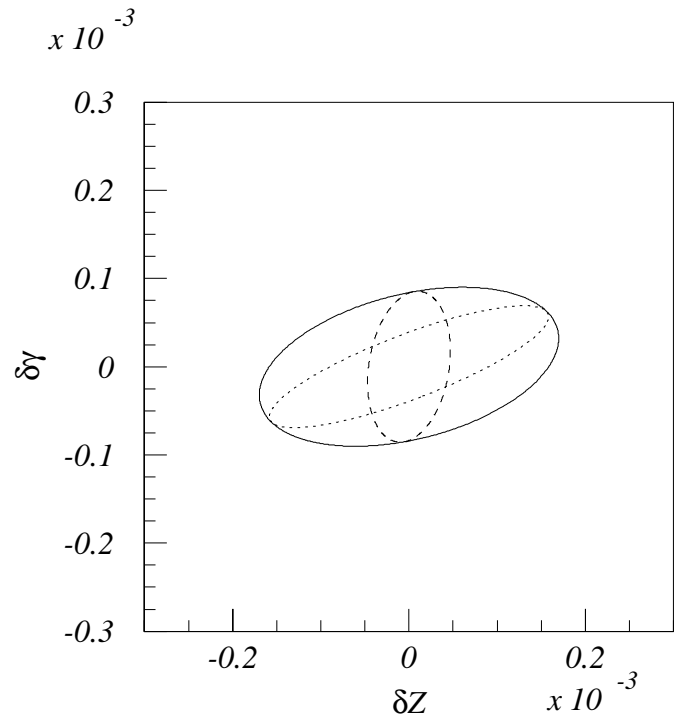
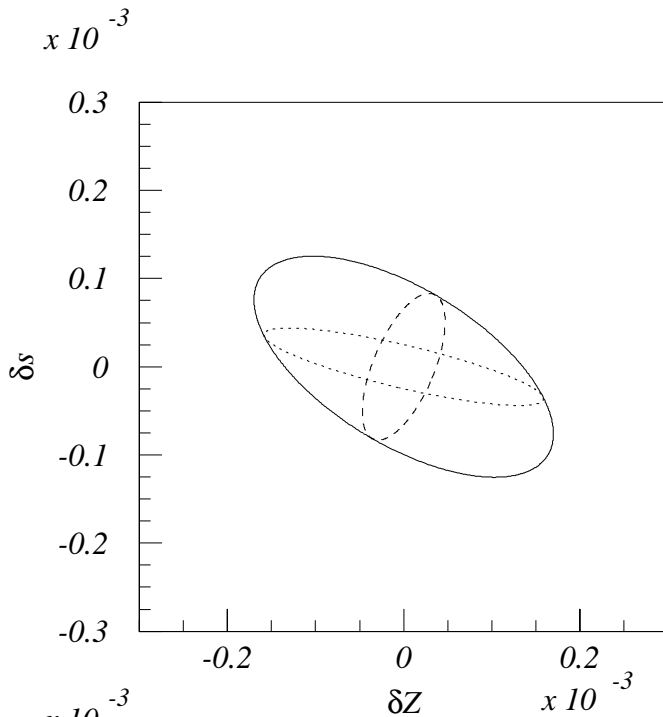
Bounds on δ

with Bhabha A_{LR}



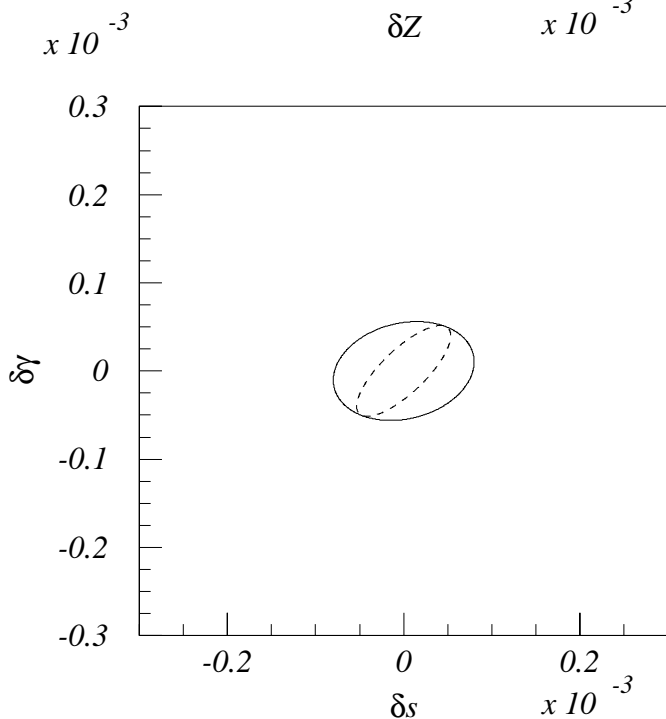
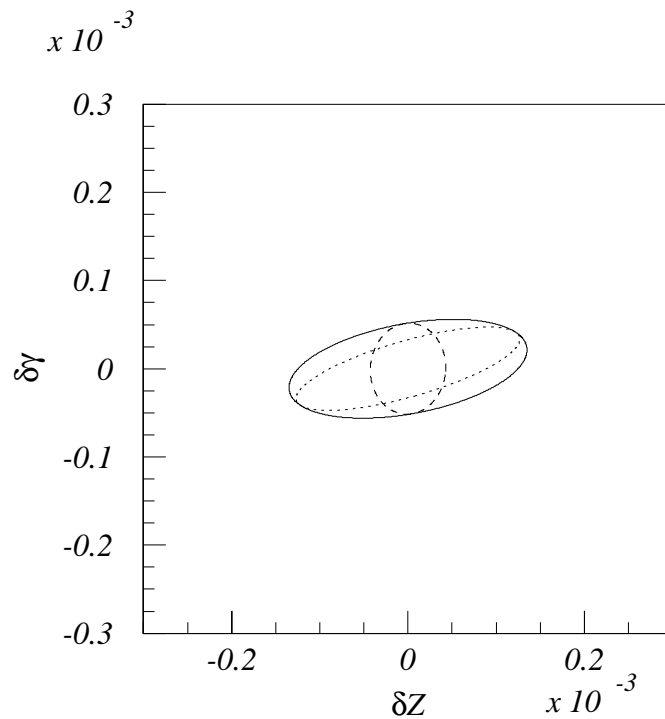
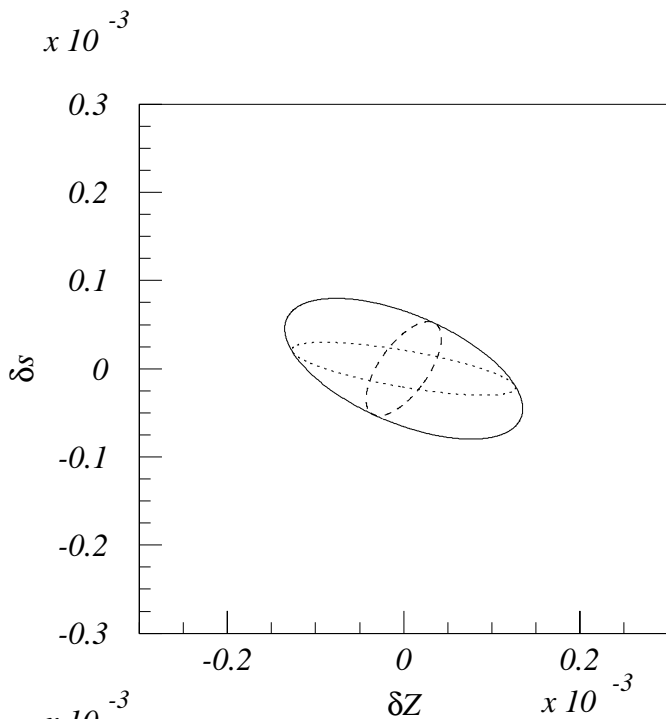
Bounds on δ

with Bhabha || asymmetry



Bounds on δ

with all Bhabha observables



Bounds on δ

Present Data

	without Bhabha	with all Bhabha	σ	A_{LR}	$A_{ }$	forw.	back.
$10^4 \delta_Z$	2.4	1.3	1.9	2.1	1.7	1.6	1.7
$10^4 \delta_s$	1.4	0.8	1.3	0.85	1.3	0.82	1.3
$10^4 \delta_\gamma$	1.1	0.56	0.62	1.1	0.9	0.65	0.82

Bounds on Non Universal New Physics

	without Bhabha	with all Bhabha	σ	A_{LR}	A_{\parallel}	forw.	back.
Λ_{LL}	85	94	89	89	87	93	85
Λ_{RR}	84	92	87	88	85	92	84
Λ_{LR}	66	120	120	66	87	110	110
Λ_{RL}	81	130	120	81	94	110	110
Λ_{VV}	120	150	150	120	120	150	140
Λ_{AA}	110	140	130	110	120	120	130
Λ_{AV}	130	130	130	130	130	130	130
Λ_{VA}	71	90	71	90	71	90	71
Λ_{ED}	3.3	5.7	5.7	3.3	3.6	5.6	4.5

Conclusions

- Simple parametrization of New Physics Effects in $e^+e^- \rightarrow f\bar{f}$ at present and future energies
- Exploitation of the Z-peak inputs in an automatic fashion for conventional observables and also for Bhabha
- Important Role of Bhabha scattering as a complementary measurement (such as A_{LR} available at NLC) and as a probe for certain New Physics models