# **B**<sub>S</sub> Mixing Results at Tevatron

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### Outline

### Introduction

- B<sub>s</sub> mixing in the Standard Model
- Ingredients to perform a measurement
- CDF measurement
- DO analysis and result
- New Standard Model constraints

### Introduction

#### $B_s$ Mixing group

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 Decay channels selection using Tier 1 and data stored at CNAF

Casarsa (TS), Da Ronco, Pagan, Delli Paoli, Lucchesi

 Event by event Primary Vertex determination

Casarsa (TS), Da Ronco, Lucchesi

 B<sub>s</sub> lifetime measurement in hadronic decays: trigger efficiency determination used in mixing analysis Da Ronco, PhD thesis

## B<sub>s</sub> Mixing in The Standard Model



$$i\frac{d}{dt} \begin{pmatrix} |B(t)\rangle \\ |\overline{B}(t)\rangle \end{pmatrix} = \begin{pmatrix} M - \frac{i}{2}\Gamma \end{pmatrix} \begin{pmatrix} |B(t)\rangle \\ |\overline{B}(t)\rangle \end{pmatrix}$$
$$H = \begin{pmatrix} M & M_{12} \\ M_{12}^* & M \end{pmatrix} - \frac{i}{2} \begin{pmatrix} \Gamma & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma \end{pmatrix}$$
$$Eigenstates are:$$
$$|B_s^H\rangle = \frac{1}{\sqrt{2}} (|B_s\rangle + |\overline{B}_s\rangle)$$
$$|B_s^L\rangle = \frac{1}{\sqrt{2}} (|B_s\rangle - |\overline{B}_s\rangle)$$
$$\Gamma = \frac{1}{2} (\Gamma_L + \Gamma_H) \equiv \frac{1}{\tau} \qquad \Delta\Gamma = \Gamma_L - \Gamma_H$$

$$\Delta m/2$$

$$M_{H,L} = M \pm \operatorname{Re}(M_{12} - \frac{i}{2}\Gamma_{12})$$

$$\Gamma_{H,L} = \Gamma \pm 2\operatorname{Im}(M_{12} - \frac{i}{2}\Gamma_{12})$$

$$\Delta \Gamma/2$$

## B<sub>s</sub> Mixing in The Standard Model cont'd

$$\Delta m_{q} = \frac{G_{F}^{2} m_{W}^{2} \eta S(m_{t}^{2} / m_{W}^{2})}{6\pi^{2}} m_{Bq} \left( f_{Bq}^{2} B_{Bq} \middle| V_{tq}^{*} V_{tb} \middle|^{2} \right)$$

#### In the ratio uncertainties cancels:

#### Applying unitarity...

## B<sub>s</sub> Mixing constraints the Standard Model

Winter 2006  $\Delta m_s$ >16.6 at 95% C.L.  $\overline{\rho} = 0.217 \pm 0.032$  $\overline{\eta} = 0.344 \pm 0.021$ 

<mark>D0 results:</mark> 17<∆m<sub>s</sub><21 90% C.L.

CDF effect in about one hour...



### **Measurement Principle in a Perfect World**

$$P(t)_{B_{q}^{0} \to B_{q}^{0}} = \frac{1}{2\tau} e^{-\frac{t}{\tau}} (1 \pm \cos(\Delta m_{q} t)) \qquad A = \frac{N^{nomix} - N^{mix}}{N^{nomix} + N^{mix}} = \cos(\Delta m_{s} t)$$



**B** lifetime

Rather than fit for frequency perform a 'fourier transform'



### Road Map to $\Delta m_s$ Measurement



## Detector for the measurement



## Adding all the realistic effects



### Road Map to $\Delta m_s$ Measurement



### **Tevatron Luminosity**

![](_page_11_Figure_1.jpeg)

May 17, 2006

## Trigger on displaced tracks: SVT

![](_page_12_Figure_1.jpeg)

May 17, 2006

## B<sub>s</sub> Data sample

![](_page_13_Figure_1.jpeg)

## Hadronic B<sub>s</sub> yields summary

![](_page_14_Figure_1.jpeg)

May 17, 2006

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#### Semileptonic samples

![](_page_15_Figure_1.jpeg)

#### Road Map to $\Delta m_s$ Measurement

![](_page_16_Figure_1.jpeg)

### **B** Lifetime measurement

Lifetime Measurement: hadronic and semileptonic B decays Hadronic decays: well measured

ct = 
$$L_{xy}/\beta_t \gamma \beta_t \gamma = P_t(B)/M(B)$$

SVT trigger bias: P(t) =  $e^{-t'/\tau} \otimes R(t',t) \cdot \epsilon(t)$  Semileptonic decays: missing X need correction factor

![](_page_17_Figure_5.jpeg)

![](_page_17_Figure_6.jpeg)

## **B** Lifetime measurement

![](_page_18_Figure_1.jpeg)

## Proper time resolution, $\sigma_t$

- Lifetime measurement not very sensitive
- In the  $\Delta$ ms fit each event weighted by its resolution
- Dedicated calibration need

![](_page_19_Figure_4.jpeg)

![](_page_19_Figure_5.jpeg)

## Proper time resolution, $\sigma_t$

![](_page_20_Figure_1.jpeg)

Layer00 is a layer of silicon placed directly on beam pipe Additional impact parameter resolution, radiation hardness

### Road Map to $\Delta m_s$ Measurement

![](_page_21_Figure_1.jpeg)

## Flavor tagger calibration: OST

#### Opposite Side Tagger (OST):

- Use data to calibrate the tagger and to evaluate D
- Fit semileptonic and hadronic  $B_d$  sample to measure: D,  $\Delta m_d$

#### Hadronic:

 $\Delta m_d = 0.535 \pm 0.028(stat) \pm 0.006(sys) ps^{-1}$ 

#### Semileptonic:

 $\Delta m_d = 0.509 \pm 0.010(stat) \pm 0.016(sys) ps^{-1}$ 

#### W.A.:

 $\Delta m_d = 0.506 \pm 0.005 \text{ ps}^{-1}$ 

![](_page_22_Figure_12.jpeg)

## Flavor Tagger calibration: SSTK

![](_page_23_Figure_1.jpeg)

 $\begin{array}{c} & & & \\ &$ 

B<sup>0</sup>/B<sup>±</sup> likely to have  $\pi$  nearby B<sup>0</sup><sub>s</sub> likely to have K Use TOF and dE/dX to separate pion from kaon Tune Monte Carlo to reproduce B<sup>0</sup>,B<sup>-</sup> distributions then apply to B<sub>s</sub>

![](_page_23_Figure_4.jpeg)

![](_page_23_Figure_5.jpeg)

## Flavor Tagger performances

	εD² Hadronic (%)	εD <sup>2</sup> Semileptonic (%)
Muon	$0.48\pm0.06$ (stat)	$0.62\pm0.03$ (stat)
Electron	$0.09\pm0.03$ (stat)	$0.10\pm0.01$ (stat)
JQ/Vertex	$0.30\pm0.04$ (stat)	0.27 $\pm$ 0.02 (stat)
JQ/Prob.	$0.46\pm0.05$ (stat)	0.34 $\pm$ 0.02 (stat)
JQ/High p <sub>T</sub>	$0.14\pm0.03$ (stat)	0.11 $\pm$ 0.01 (stat)
Total OST	$1.47\pm0.10$ (stat)	1.44 $\pm$ 0.04 (stat)
SSKT	$3.42\pm0.49~(\text{syst})$	$4.00\pm0.56~\text{(syst)}$

- Exclusive combination of tags in OST
- SSTK-OST combination assumes independent tagging information

## **Amplitude Scan**

- A is introduced:  $P(t)_{B_q^0 \to B_q^0} = \frac{1}{2\tau} e^{-\frac{t}{\tau}} (1 \pm A\cos(\Delta m_q t))$
- A=1 when  $\Delta m_s^{\text{measured}} = \Delta m_s^{\text{true}}$
- Points:
   A±σ(A) from Likelihood
   fit for different Δm
- Yellow band: A±1.645σ(A)
- Δm where A±1.645σ(A)<1 excluded at 95% C.L.
- Dashed line: 1.645σ(A) vs Δm
- Measured sensitivity: 1.645σ(A)=1 May 17, 2006

#### B<sup>o</sup> mixing in hadronic decay

![](_page_25_Figure_9.jpeg)

## Choice of Procedure

- How does an evidence of a signal look like?
- What procedure if aiming at measurement?
- These questions must be asked before performing the Analysis! Otherwise lack of coverage is the punishment!
- Before un-blinding:

p-value: probability that observed effect is due background fluctuation. No search window.

![](_page_26_Figure_7.jpeg)

## p-value Estimation

![](_page_27_Figure_1.jpeg)

#### ∆(ln(L ))= ln[L (A=1)/ lnL (A=0)]

Probability of random tag fluctuation estimated on data (randomized tags) and checked with toy Monte Carlo May 17, 2006

## Systematic Uncertanties in Amplitude Scan

![](_page_28_Figure_1.jpeg)

Related to absolute value of A important when setting a limit Cancel out in  $A/\sigma_A$ Very small compared to statistical error May 17, 2006

## Amplitude Scan: Semileptonic decays

![](_page_29_Figure_1.jpeg)

### Amplitude Scan: Hadronic decays

![](_page_30_Figure_1.jpeg)

## **Amplitude Scan: Combined**

![](_page_31_Figure_1.jpeg)

### Combined Amplitude Scan: an other view

![](_page_32_Figure_1.jpeg)

## Likelihood Profile

How often random tags produce a likelihood deep this dip?

![](_page_33_Figure_3.jpeg)

## Likelihood significance

![](_page_34_Figure_1.jpeg)

Find maximum ∆(ln(L)) in data randomizing 50,000 times tags
In 228 experiments found ∆(ln(L))>6.06 Probability of fake, p-value=0.5%

![](_page_34_Picture_3.jpeg)

Measure  $\Delta m_s \parallel \parallel$ 

#### Systematic Uncertanties on $\Delta m_s$

	Syst. Unc
SVX Alignment	0.04 ps <sup>-1</sup>
Track Fit Bias	0.05 ps <sup>-1</sup>
PV bias from tagging	0.02 ps <sup>-1</sup>
All Other Sys	< 0.01ps <sup>-1</sup>
Total	0.07 ps <sup>-1</sup>

Fit Model: negligible

#### Relevant only lifetime scale

### Measurement of $\Delta m_s$

![](_page_36_Figure_1.jpeg)

17.00 < ∆m<sub>s</sub> <17.91 ps<sup>-1</sup> at 90% C.L. 16.94 < ∆m<sub>s</sub> <17.97 ps<sup>-1</sup> at 95% C.L. May 17, 2006

# $|V_{td}|/|V_{ts}|$ Determination

$$\frac{\Delta m_s}{\Delta m_d} = \frac{m_{Bs}}{m_{Bd}} \xi^2 \frac{\left|V_{ts}\right|^2}{\left|V_{td}\right|^2}$$

Used as inputs:

- $m_{Bs}/m_{Bd} = 0.9830 \text{ PDG } 2006$   $\xi^2 = 1.210_{-0.35}^{+0.47}$  (M. Okamoto, hep-lat/0510113)
- $\Delta m_d = 0.507 \pm 0.005 PDG 2006$

||V<sub>td</sub>|/|V<sub>ts</sub>|=0.208 <sup>+0.008</sup> (stat.+syst.)|

Latest Belle result  $b \rightarrow s\gamma$  (hep-ex/050679):

 $|V_{td}|/|V_{ts}| = 0.199 + 0.026 = (stat) + 0.018 = 0.015 (syst)$ 

## **DO** Analysis

![](_page_38_Figure_1.jpeg)

*М*<sub>(*кк*)π</sub> [GeV]

## **DO Analysis**

![](_page_39_Figure_1.jpeg)

Opposite Side Tagging: -lepton (electron or muon)  $Q_J^{\ell} = \sum_i q^i p_T^i / \sum_i p_T^i$ - Secondary Vertex  $Q_{SV} = \sum_i (q^i p_L^i)^{0.6} / \sum_i (p_L^i)^{0.6}$ 

- Event Charge  $Q_{\rm EV} = \sum_i q^i p_T^i / \sum_i p_T^i$ 

#### Tags combined:

$$d_{\text{tag}} = \frac{1-z}{1+z}$$

d>0 b tag

d<0 b tag

$$z = \prod_{i=1}^{n} \frac{f_i^{\overline{b}}(x_i)}{f_i^{\overline{b}}(x_i)}$$

### **DO Procedure**

![](_page_40_Figure_1.jpeg)

Correction factor due to missing neutrino

Several effects taken into account:

- Resolution scale factor for detector mismodeling
- Reconstruction efficiency as function of decay length
- Physical and combinatorial background contributions

### **DO Results**

![](_page_41_Figure_1.jpeg)

## Unitarity Triangle fit with $\Delta m_s$

Old:  $\overline{\rho} = 0.217 \pm 0.032$  $\overline{\eta} = 0.344 \pm 0.021$ 

New:

![](_page_42_Picture_3.jpeg)

![](_page_42_Figure_4.jpeg)

## **New Physics Limit UTfit**

#### Model independent approach $|\Delta F|=2$ Hamiltonian

![](_page_43_Figure_2.jpeg)

 $C_{Bs} = \Delta m_s^{SM+NP} / \Delta m_s^{SM} = 1.01 \pm 0.33$ [0.33,2.04] @ 95% C.L.

#### Conclusions

> CDF has an experimental signature for  $B_s - \overline{B}_s$  oscillations > Probability of random fluctuation is 0.5%

First direct measurement of:

$$\Delta m_s = 17.33^{+0.42}_{-0.21} \pm 0.07 \text{ ps}^{-1}$$

### BACKUP

#### The Accelerator

![](_page_46_Picture_1.jpeg)

#### Detectors

![](_page_47_Figure_1.jpeg)

#### Detectors

![](_page_48_Figure_1.jpeg)

### Introduction

#### Made Possible By the CDF Detector

- Trigger
  - high bandwidth & tremendous flexibility
  - XFT and SVT
- Exquisite charged particle tracking
  - excellent pattern recognition & mass resolution (COT, solenoid)
  - precise production & decay point reconstruction (L00) SVX)
- Particle identification
  - Time of Flight (TOF) and dE/dx in COT
- Extremely dedicated collaborators for operations
  - a lot of sleepless nights for analysis but many more for operations
  - many of the analyzers spent sleepless nights working on critical detector components too.

Designed by Padova group and detectors tests done in Padova

## Flavor tagger calibration

![](_page_50_Figure_1.jpeg)

## Parametrizing tag decision

![](_page_51_Figure_1.jpeg)

Opposite Side Taggers calibrated in our very high statistics  $\ell + SVT$  samples Dependence on several variables used to increase the tagging power

Overall scale factor measured on B<sup>0/+</sup> candidates to take care a possible overall (small) shift

Similar performace of semileptonic hadronic modes

## Calibrating SSTK

#### Systematic studies cover:

- + Fragmentation Model
- bb Production Mechanisms
- + B\*\* content
- Detector/PID resolution
- + Multiple interactions
- PID content around B
- Data/MC agreement

![](_page_52_Figure_9.jpeg)

Small discrepancies covered

Select the most likely kaon track (PID \*) as tagging track SS(K)T performance estimated from MC:  $\varepsilon D^2(B_s \rightarrow D_s(\phi \pi)\pi) = 4.0^{+0.8}_{-1.2}\%$  (1rst period of the data) \*) TOF & dE/dx are used for particle identification

## Calibrating SSTK

![](_page_53_Figure_1.jpeg)

Tune MC to reproduce  $\mathsf{B}^{0/\underline{+}}$  dilution and then measure it for SSTK

## Amplitude scan semileptonic

![](_page_54_Figure_1.jpeg)

## Amplitude scan hadronic

![](_page_55_Figure_1.jpeg)

#### Sequence of CDF Run II Results on B<sub>s</sub> Mixing

- 1<sup>st</sup> result March 2005 presented at Moriond QCD
  - hadronic modes from two-track trigger
  - semileptonic modes from lepton + SVT trigger
  - opposite-side flavor tags: muons, electrons, jet-charge
  - combined sensitivity  $\Delta m_s > 8.4 \text{ ps}^{-1}$
- 1<sup>st</sup> update: October 2005 presented at PANIC 2005
  - substantial increase in semileptonic signal from TTT
  - several analysis improvements, e.g.,
    - neural net based jet-charge opposite side flavor tag
    - improved opposite side flavor tag calibration
    - improved boost resolution on semileptonic decays
  - combined sensitivity ∆ m<sub>s</sub> ≥ 13.0 ps<sup>-1</sup>

#### These results based on 360 pb-1 (0d data)