

Status of the Analysis on CPV in mixing using P.R. D^*lv and K-tag

•Alessandro Gaz PHD thesis results:

Martino, 6/30/2008

$$|q/p|-1 = xxx \pm 0.0025(\text{stat}) \pm 0.0018(\text{syst}) \pm 0.0023(\text{bias})$$

(2nd best meas. @ B factories)

A good result but:

- $|q/p|$ bias ~ 0.004 from MC, bigger than statistical error;
- Bias reflects in the largest systematic error...

Large bias on τ_{B_0} , Δm_d :

PDG:

$$\bullet \tau_{B_0} = 1.490 \pm 0.004 \text{ ps}$$

$$1.530 \pm 0.009 \text{ ps}$$

$$\bullet \Delta m_d = 0.5699 \pm 0.0022 \text{ ps}^{-1}$$

$$0.507 \pm 0.005 \text{ ps}^{-1}$$



Bias to be understood before publication!

Problems of the Unbinned Fit

A) Slowness:

- Fit of the full Run1-Run5 data statistics too long (~ 100 free parameters);
- Split of data set (takes ~ 24 h to fit 5% of the real data statistics);
- Result from the average of the different subsample: systematic due to sampling criterion;

B) Convergence difficulty:

- $\log(\text{Likelihood})$ shows a structure with secondary minima;
- **Measured Bias is actually a true effect or is it a feature of the fit instability?**
- Same question about the evaluation of systematic uncertainties;



A) and B) effects interfere:

Slowness precludes studies on convergence & stability of the fit.

Solution: Binned Fit

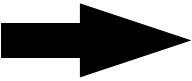
- Binning extended to all the relevant variables:

Δt , $\sigma(\Delta t)$, P_K , $m^2 v$, $\Theta(1-K) = 50K$ bins

8 event categories: (e/μ) X (Mixed/Unmixed) X (K^+/K^-)

→ Convergence takes ~ 24 h on the full R1-R5 data statistics by floating all the parameters!

→ Result on data compatible with the “Old-Unbinned” fit!

- 
- Go back to the MC in order to:
 - Define a strategy to reach the fit convergence;
 - Understand at which level of fit complexity the bias does appear (perfect/measured resolution and tagging; only signal/full sample composition);
 - Re-blind the fit on real data;

Bias w.r.t. MC truth vs number of Δt bins

B^0 Btag Signal Fit with Perfect Resolution & tagging:

Δt Bins	:	20	50	100
τ_{B^0}		0.0183 ± 0.0007	-0.0062 ± 0.0006	-0.0095 ± 0.0006
Δm		-0.0159 ± 0.0002	-0.0049 ± 0.0002	-0.0033 ± 0.0002
b		0.0019 ± 0.0004	0.0021 ± 0.0005	0.0021 ± 0.0005
c		0.0000 ± 0.0005	-0.0003 ± 0.0004	-0.0002 ± 0.0004

➔ Use at least 50 Δt bins; 100 Δt bins in the following

$$\text{Fitted } \chi_d = 0.176 \pm 0.0001 \quad 0.1778 \pm 0.0001 \quad 0.1780 \pm 0.0001$$

(in good agreement with $F(\text{mixed}) = 0.1786 \pm 0.0002$)

➔ -0.2% selection bias on $F(\text{mixed})$ (MC truth: $\chi_\delta = 0.1809$)
Bias of several Statistical Sigmas on τ_{B^0} & Δm , but <1%.

• $|q/p|$ measured from semilept charge asymmetry with no time dependence
➔ not sensitive to Δt binning

Study of Fit Convergence

- **Study the $\Delta\log(L)$ profile around the minimum** by performing a set of several fits with a fixed value of a relevant variable x (i.e. $|q/p|-1$, Δm_d , ...) and floating all the other parameters;

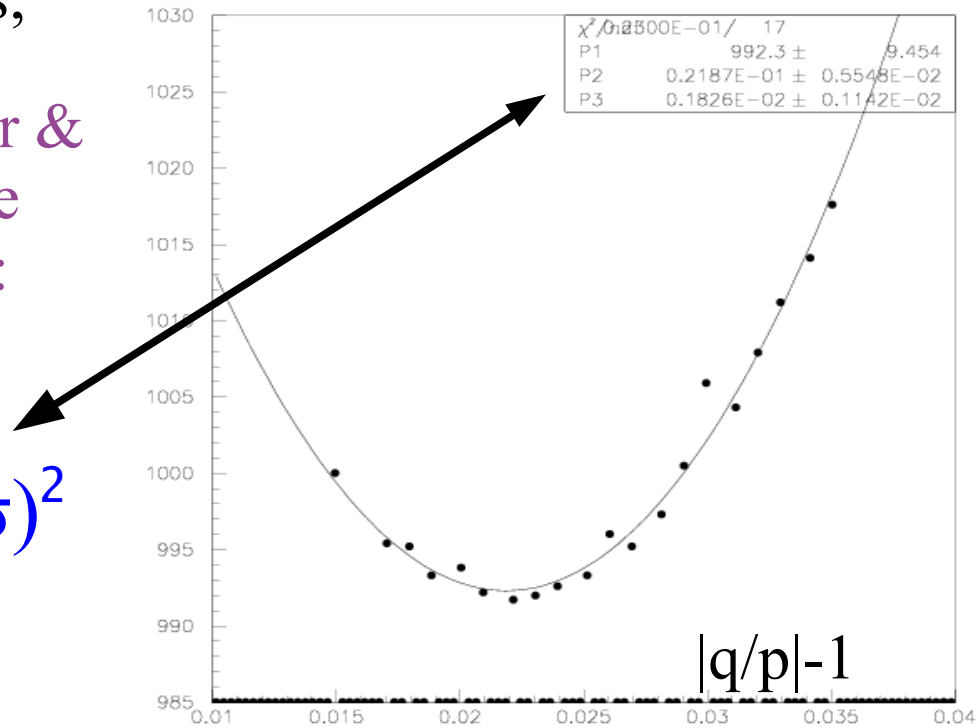
- **Determination of the parameter & statistical error directly from the plot by means of a parabolic fit:**

$$\log(L) = \log(L_{\min}) + \frac{1}{2} \left(\frac{x - x_{\min}}{\sigma} \right)^2$$

x_{\min} = Best Value

σ = Statistical Error

To be compared with the nominal fit results



Blind fit on data:

$$|q/p|-1 = 0.022 \pm 0.002$$

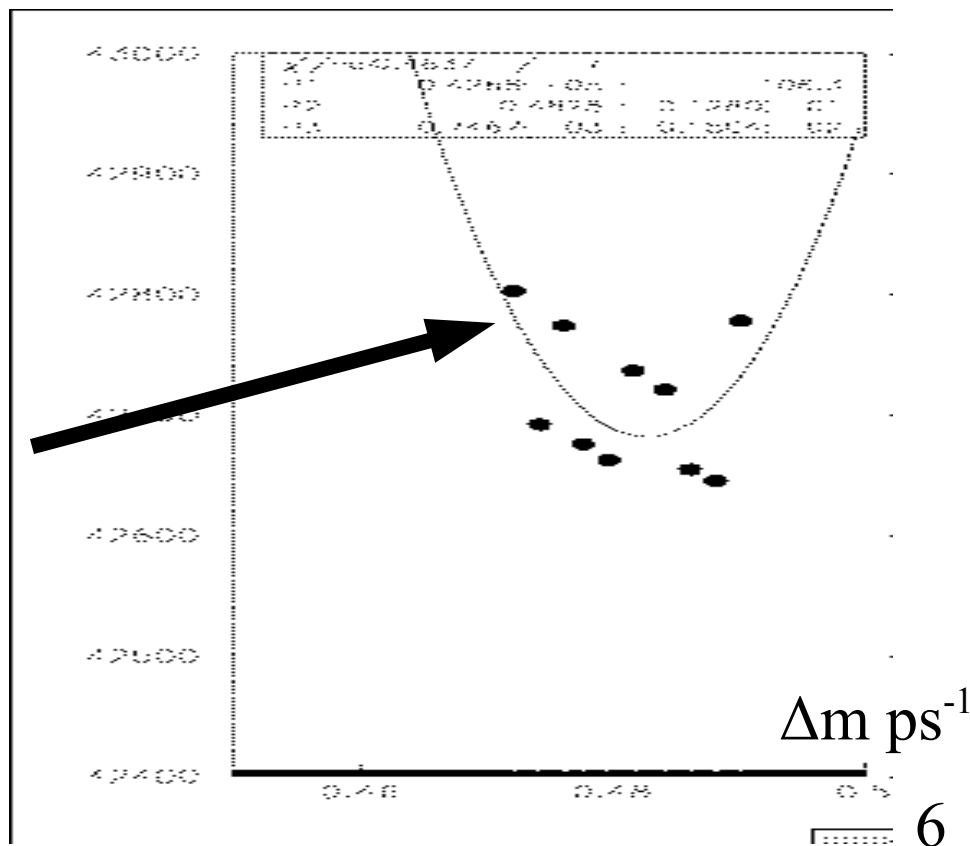
in agreement with Alessandro thesis result

Study of Fit Convergence

- $\log(L)$ shows multiple minima: often the fit does not converge to the absolute minimum (minuit status= FAILED, usually Covariance Matrix not positive defined);
- **$\log(L)$ scan is the solution!**

Scan vs Δm of B^0 MC Signal with measured Δt & tag

In case of problem in the fit convergence, the parabolic fit to the $\log(L)$ profile is BAD.



Definition of Fit Strategy

Recipe to reach the convergence:

- 1) Perform the nominal fit;
in case of convergence problems (often using experimental resolution or Signal+BKG sample):
- 2) **Launch a scan on Gridka** (~10 fits need a few hours \rightarrow a couple of days depending on sample statistics & fit complexity)
- 3) Check if the parabolic fit is good & it gives x_{\min} and σ in good agreement with the nominal fit;
- 4) Otherwise: Launch another scan starting from the parameters corresponding to the lowest minimum of the $\log(L)$ in the previous one;
- 5) **Iteratively reach a good $\log(L)$ profile;**
- 6) Perform the nominal fit starting from the parameters of the best fit of the set;



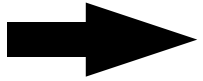
The nominal fit converges!

Fit Strategy

- To reach the absolute minimum usually is very useful to perform likelihood scans over different relevant variables (Δm , q/p , τ , Detector Asymmetries, dilutions)

The Log(L) scan strategy allow us to:

- 1) Reach the convergence at the “true” Log(L) minimum;
- 2) Check the statistical error of the nominal fit.



MC Validation: Fit Bias

- Study the bias on τ , Δm , $|q/p|$ step by step, from MC truth to experimental Δt and tagging. Add one component at a time from pure B^0 signal to full sample composition to see at which level of fit complexity the bias becomes dangerous (if it is the case...).
- Use only CONVERGED fits, obtained by means of the “log(L) Scan” recipe to avoid fit instability effects;

MC-Reference parameters:

$$\tau_{B^0} = 1.540 \text{ ps}$$

$$\chi_d = 0.1809$$

$$\Delta m = 0.489 \text{ ps}^{-1}$$

$$|q/p| - 1 = 0$$

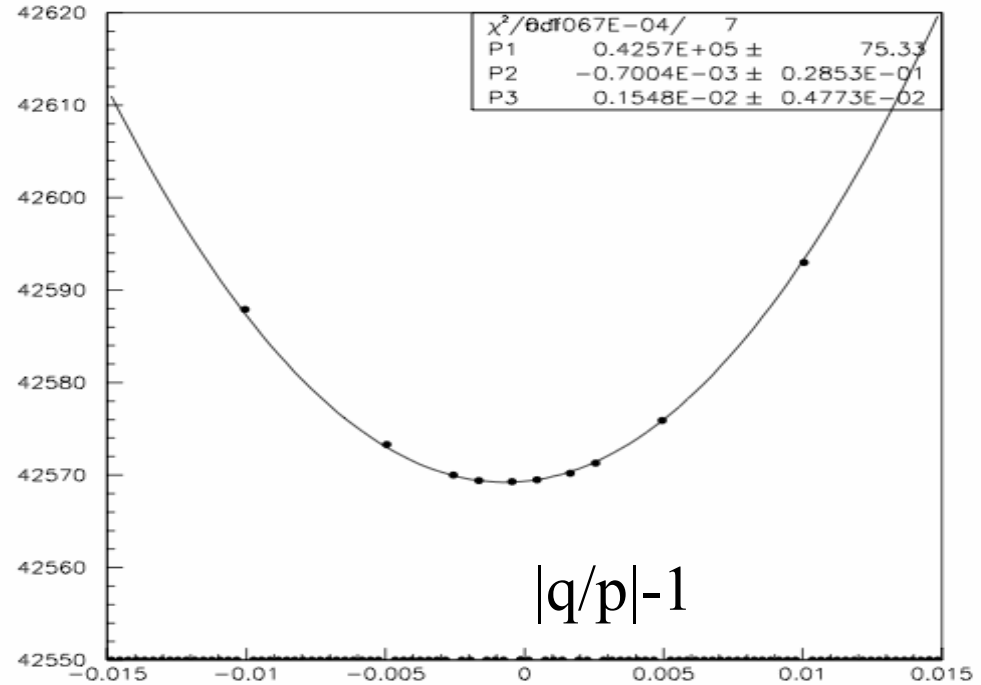
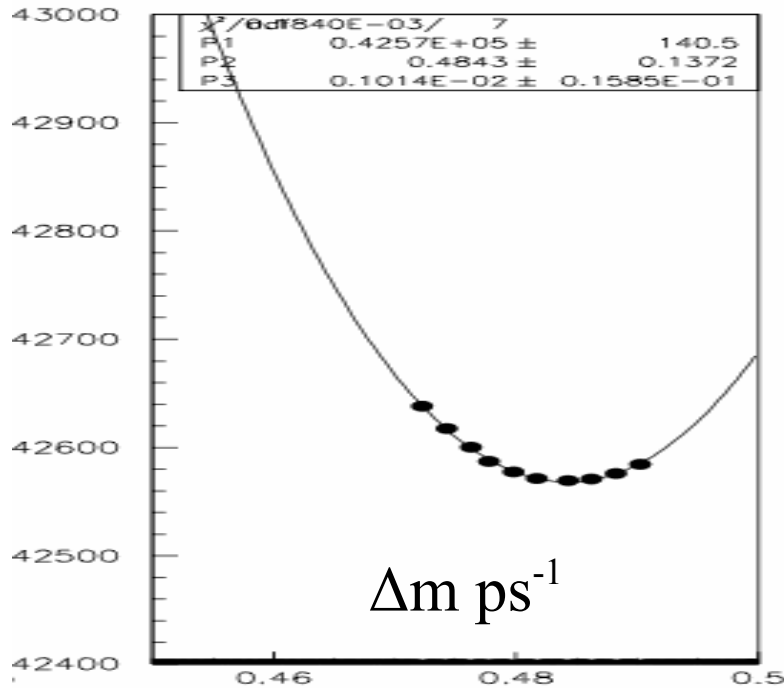
$$b = 0$$

$$c = 0$$

Doubly Cabibbo Suppressed

Pure B⁰ SIGNAL Results

Btag+Dtag Signal Fit with Measured Δt & tagging:



$$\tau_{B^0} = 1.5232 \pm 0.0018 \quad \delta\tau = -0.0168 \pm 0.0018$$

$$\Delta m = 0.4842 \pm 0.0011 \quad \delta\Delta m = -0.0048 \pm 0.0011 \quad \rightarrow \quad \text{1\% bias on both!}$$

$$|q/p|-1 = -0.0006 \pm 0.0015$$

$$A_{\text{tag}} = 0.0134 \pm 0.0010$$

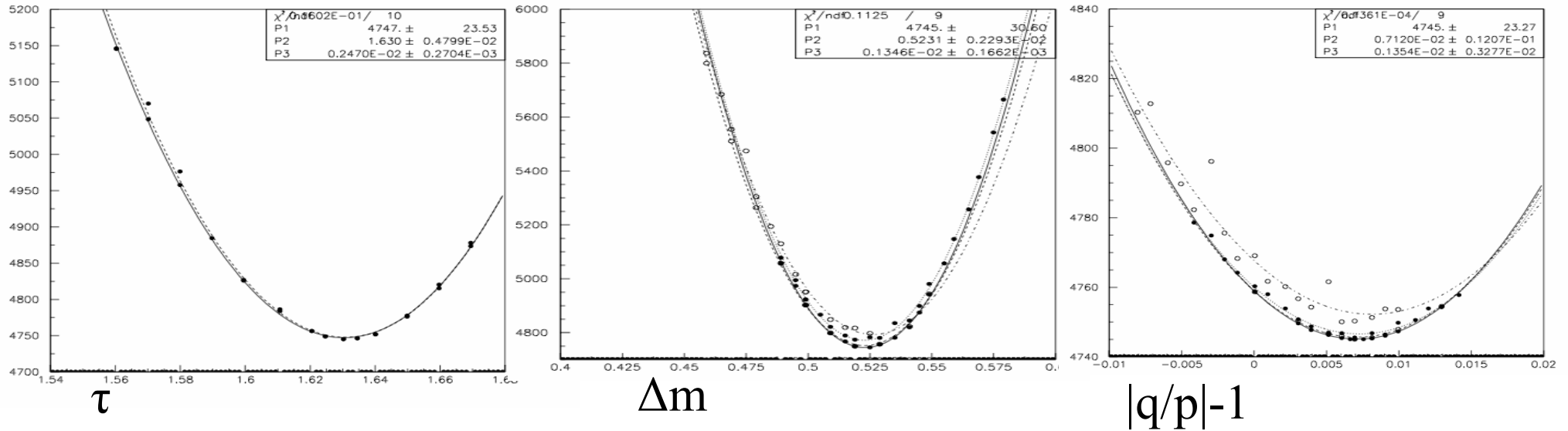
$$A_{\text{rec}(e)} = 0.0001 \pm 0.0007$$

$$A_{\text{rec}(\mu)} = 0.0059 \pm 0.0007$$

NO BIAS on $|q/p|$ (with the “old unbinned” procedure we had already a 0.004 bias on q/p at this level)

B⁰ Combinatorial BKG Study

B-tag+D-tag, measured Δt and tag



$$\tau = 1.630 \pm 0.0025 \text{ ps}; \quad \Delta m = 0.5231 \pm 0.0013 \text{ ps}^{-1}; \quad |q/p|-1 = 0.0071 \pm 0.0014$$

• $\chi_d(\text{BKG}) > \chi_d(\text{SIG})$ (if two $B^0 \rightarrow D^* l \nu$ decays in the event, it's possible to pick up lepton & π^* from the two different sides with the right charge correlation):

→ $\tau_{\text{BKG}}, \Delta m_{\text{BKG}}$ just effective parameters;

• $|q/p|-1$ shows a strong bias... PROBLEM?
 • Is the assumption to share the same charge asymmetries between SIG and BKG wrong?

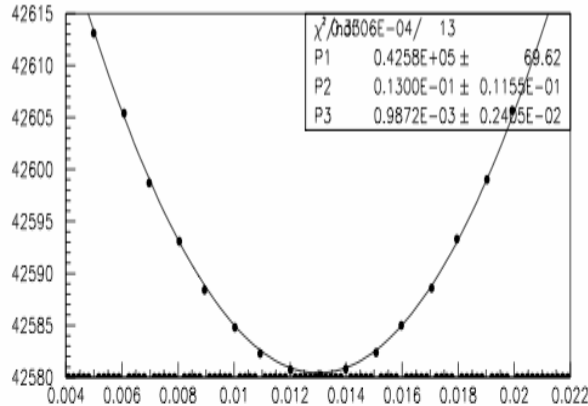
$A_{\text{tag}} \sim 0.0125$
 $A_{\text{rec}(e)} \sim 0.0040$
 $A_{\text{rec}(\mu)} \sim 0.0130$

• Look at the detector asymmetries to compare SIGNAL vs BKG...

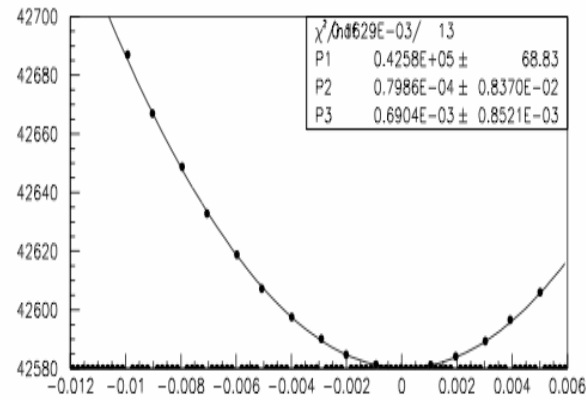
Detector Asymmetries SIG vs BKG

S
I
G
N
A
L

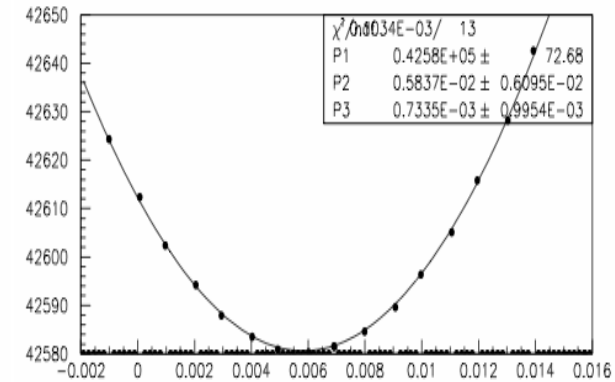
ATAG



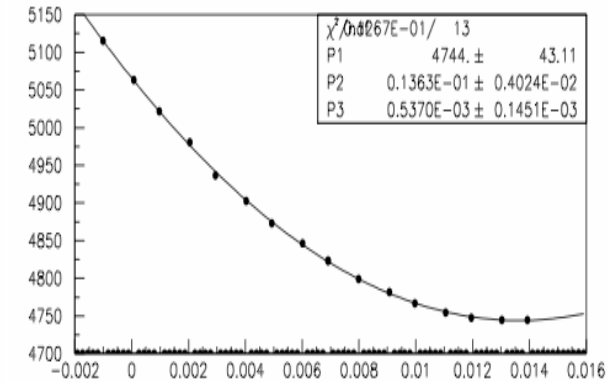
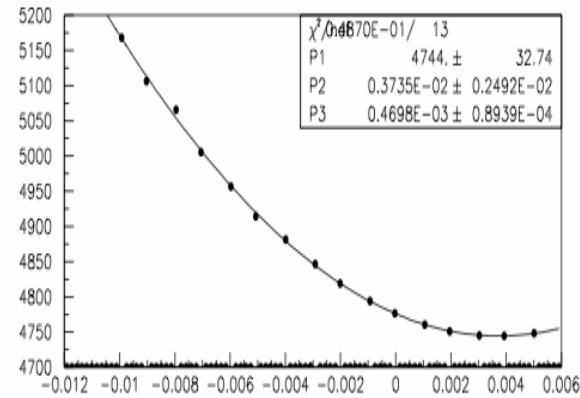
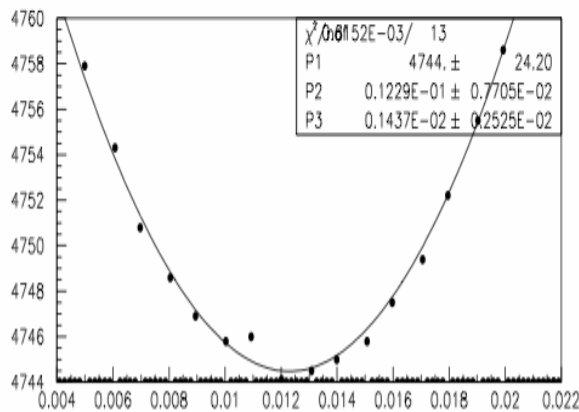
AREC(e)



AREC(μ)

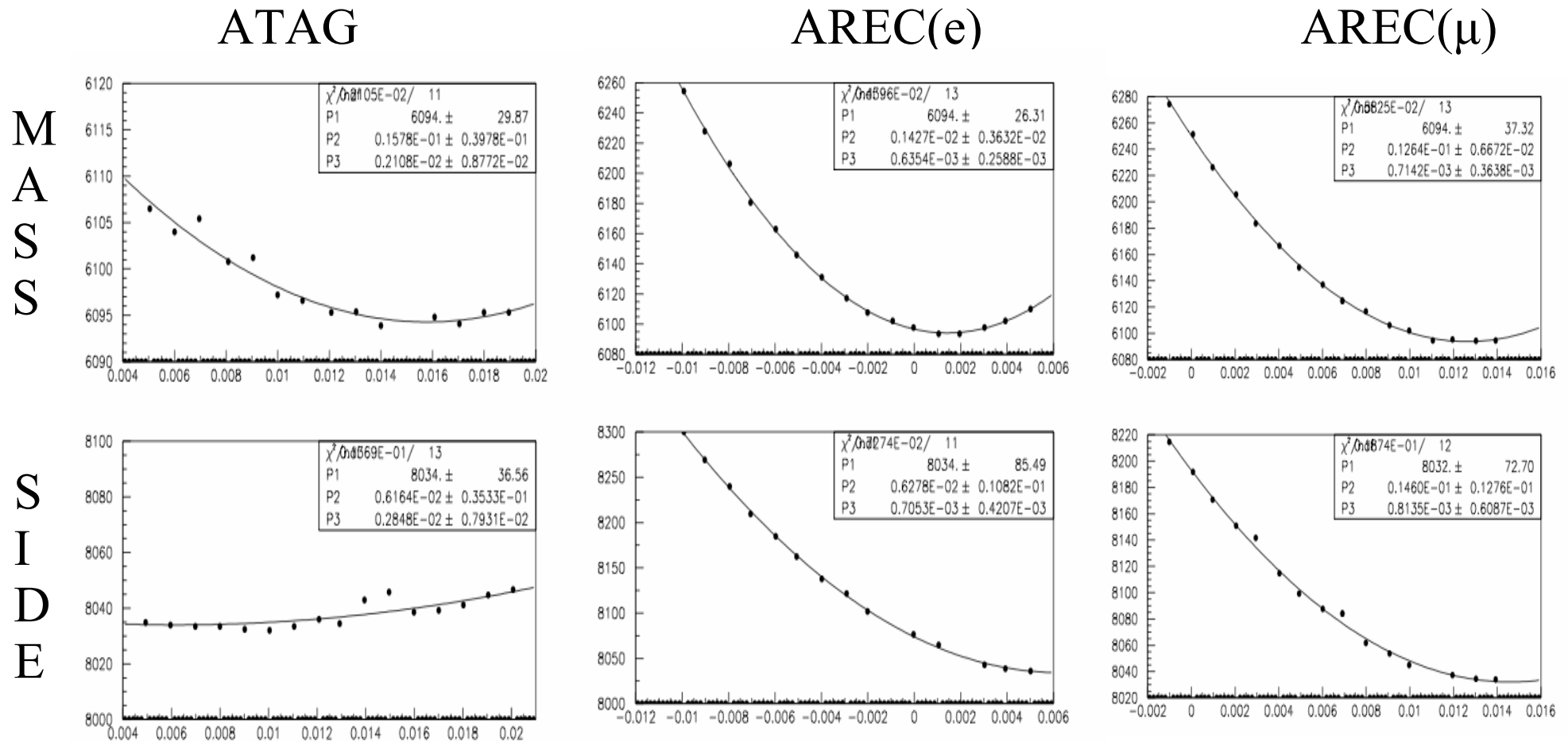


B
K
G



- Atag in good agreement between SIG & BKG;
- Arec(BKG) higher than Arec(SIG)... contradiction w.r.t. our “old fit” results?

BKG Detector Asymmetries: MB vs SB



- Atag(SB) lower than Arec(MB)...
- Arec(SB) higher than Arec(MB)...
- **Is it a true effect or a feature of the fit?**

Arec BKG vs SIGNAL from MC truth

From the comparison of selected # \overline{B}^0 vs # B^0

SIGNAL

BKG

Electron Sample

A Unm -0.0833229+-0.0384739(%)

A Mix 0.0453182+-0.0820595(%)

A all -0.0601405+-0.0348352(%)

Chi_d 0.1804+-0.000189488

0.18002+-0.000189219

B^0

\overline{B}^0

A Unm -0.113381+-0.0410147(%)

A Mix -0.0121102+-0.0743625(%)

A all -0.0897592+-0.0359142(%)

Chi_d 0.233433+-0.000214947

0.233071+-0.000214639

B^0

\overline{B}^0

Muon Sample

A Unm 0.749731+-0.0463026(%)

A Mix 0.678318+-0.0990136(%)

A all 0.736917+-0.041943(%)

Chi_d 0.179339+-0.000226725

0.17955+-0.000228507

B^0

\overline{B}^0

A Unm 0.768166+-0.0481464(%)

A Mix 0.991979+-0.0882264(%)

A all 0.819524+-0.0422629(%)

Chi_d 0.229861+-0.000250449

0.229069+-0.000252204

B^0

\overline{B}^0

- Good agreement found between SIGNAL and BKG!
- Results in agreement with previous page plots for the SIGNAL FIT!
- Selection does not introduce any relevant difference between SIG & BKG.

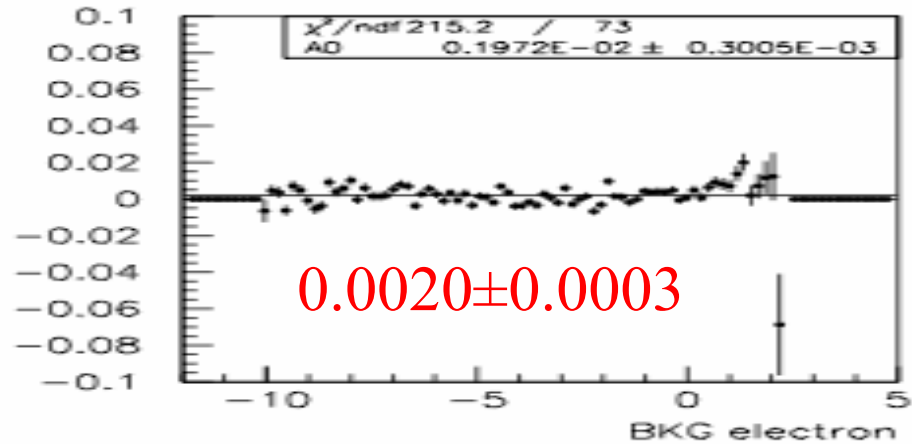
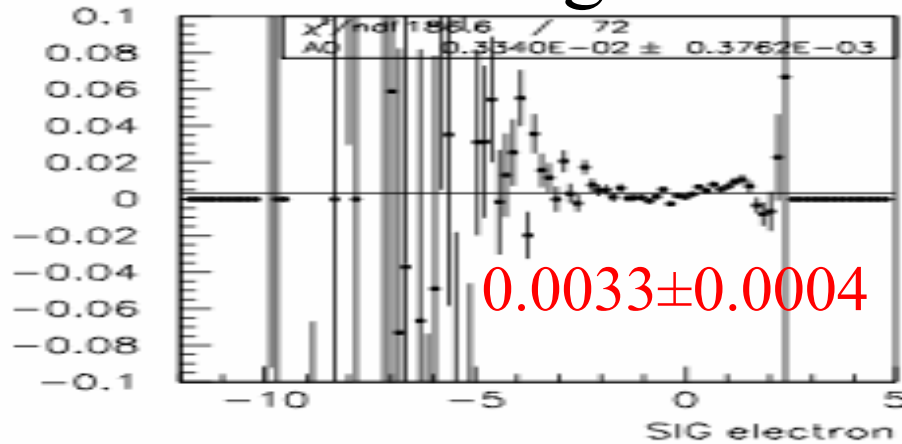
Arec BKG vs SIGNAL from MC counting

From the comparison of # 1^+ vs # 1^- (fakes included)

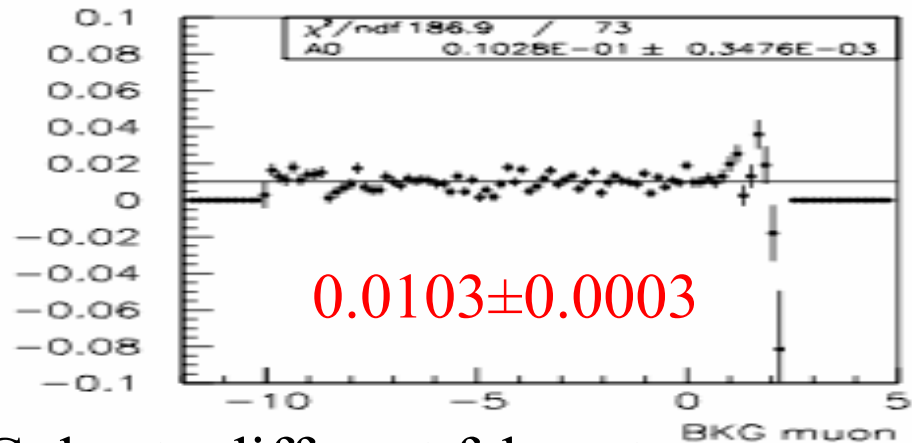
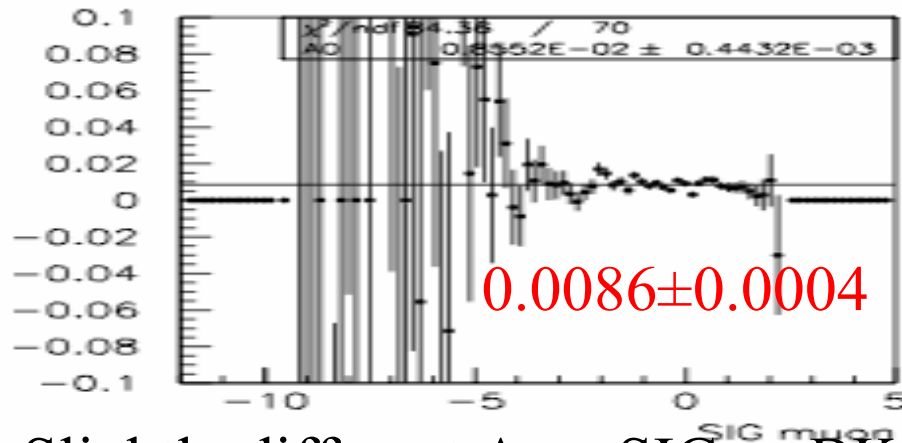
Arec vs mv^2

Signal

BKG



e



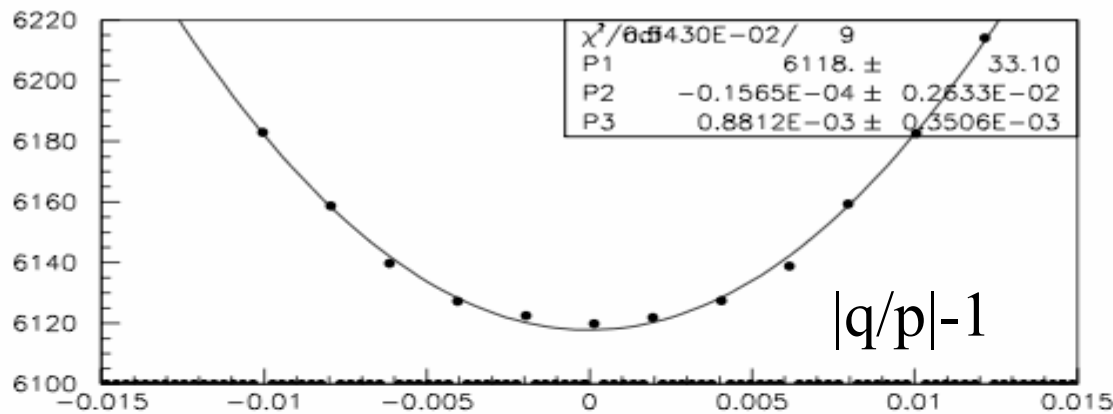
μ

- Slightly different Arec SIG vs BKG due to different fake rate;
- No mv^2 dependence found in the BKG detector asymmetries...
- **Arec & $|q/p|$ are strongly correlated: maybe the $|q/p|$ bias in the BKG fit would be reabsorbed by using common detector asymmetries for SIG & BKG?**

B⁰ Combinatorial BKG: MB vs SB

➔ CHECK:

Perform a scan on $q/p(\text{BKG})$ by fixing A_{tag} , A_{rec} to the SIGNAL ones:

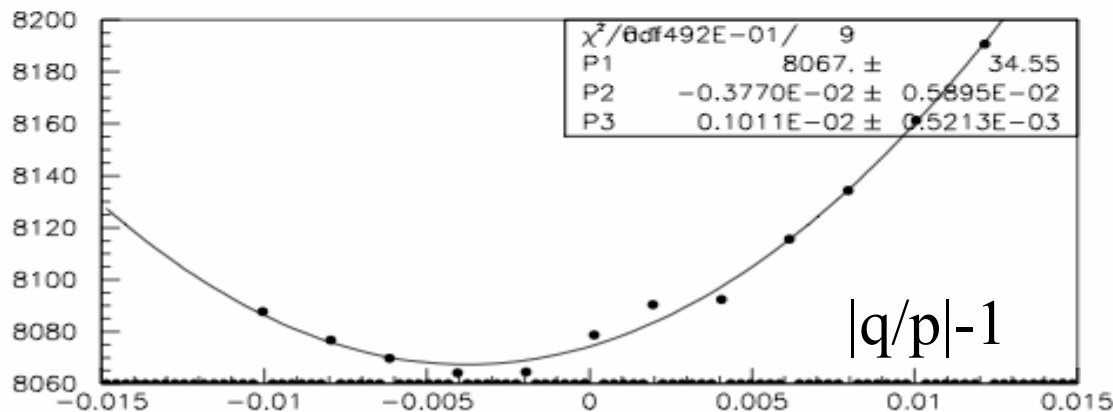


Mass Band:

$$|q/p|-1 = -0.00002 \pm 0.00088$$

No Bias!

- Compensation between the A_{rec} & $|q/p|-1$ differences in SIGNAL vs BKG !



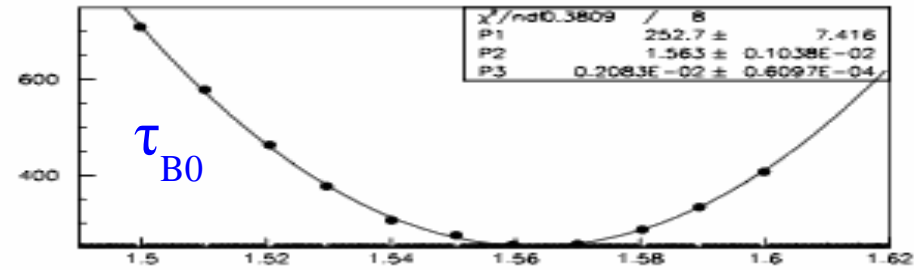
Side Band:

$$|q/p|-1 = -0.0037 \pm 0.0010$$

Strong Bias!

- MB B⁰ BKG in good agreement with signal B⁰
- ...try to use just the MB?...

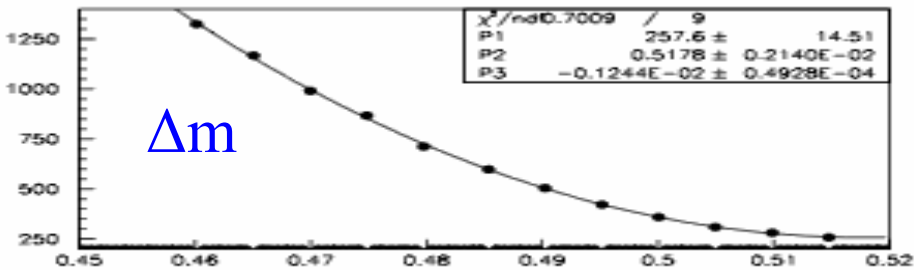
B^0 SIGNAL+BKG Mass Band Results



$$\tau_{B^0} = 1.563 \pm 0.0021 \quad \delta\tau = 0.023 \pm 0.002$$

$$\Delta m = 0.517 \pm 0.0012 \quad \delta\Delta m = 0.028 \pm 0.001$$

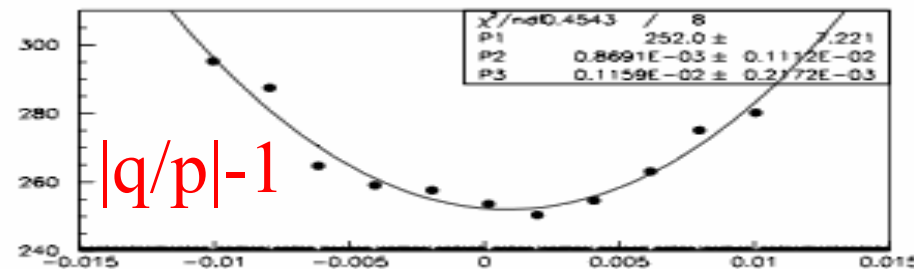
$$|q/p|-1 = 0.0009 \pm 0.0012$$



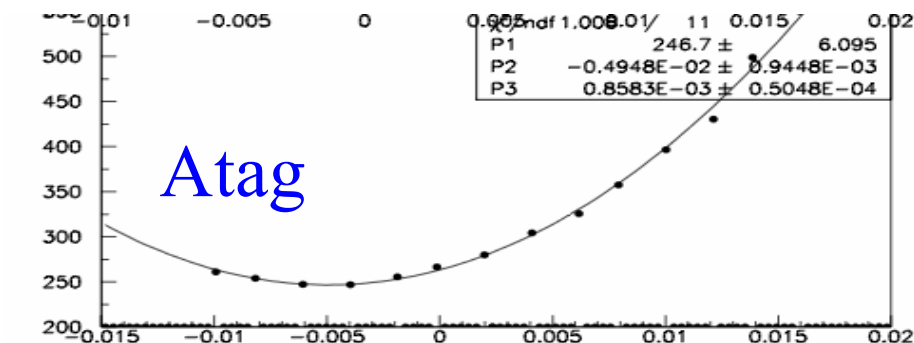
$$A_{tag} = -0.0049 \pm 0.0009$$

$$A_{rec}(e) \sim 0.0030$$

$$A_{rec}(\mu) \sim 0.0090$$



- **No Bias on $|q/p|$... BUT:**
- A_{tag} changes sign... (it was 0.0134 ± 0.0010 on Pure Signal);
- A_{rec} between SIG & BKG results;
- Strong bias on τ_{B^0} & Δm



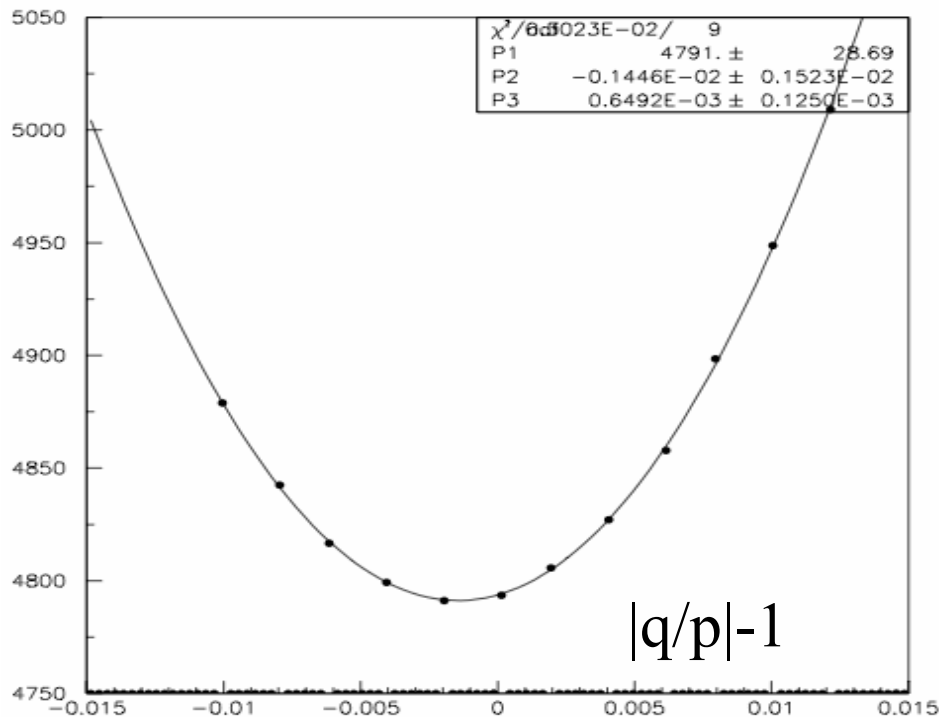
Due to the strong correlation between SIG & BKG lifetimes, Side Band are needed to fit the BKG effective parameters τ_{B^0} & Δm .

➡ **Go back to MB + SB...**

B^0 Combinatorial BKG: MB+SB

→ CHECK:

Perform a scan on $q/p(\text{BKG})$ by fixing A_{tag} , A_{rec} to the SIGNAL ones:

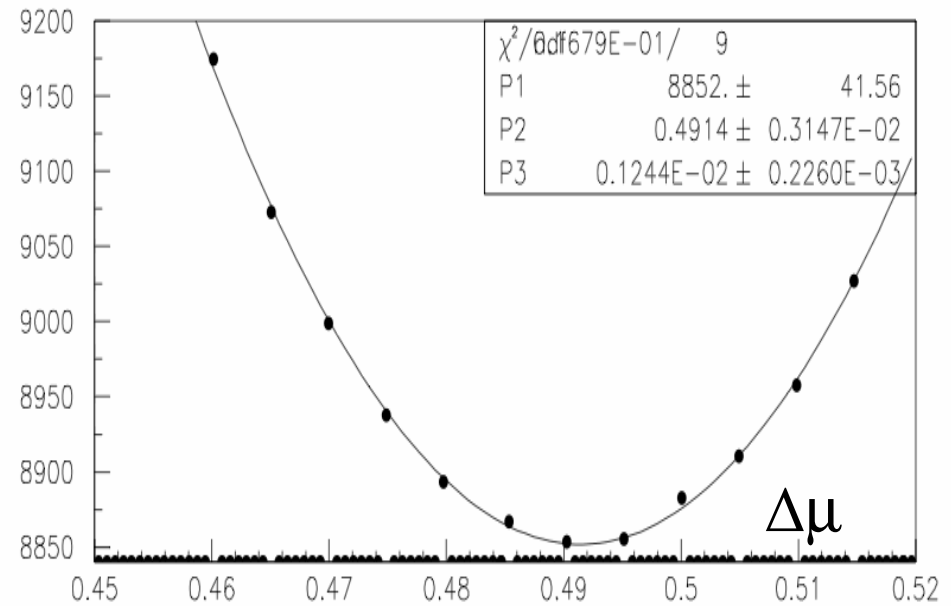
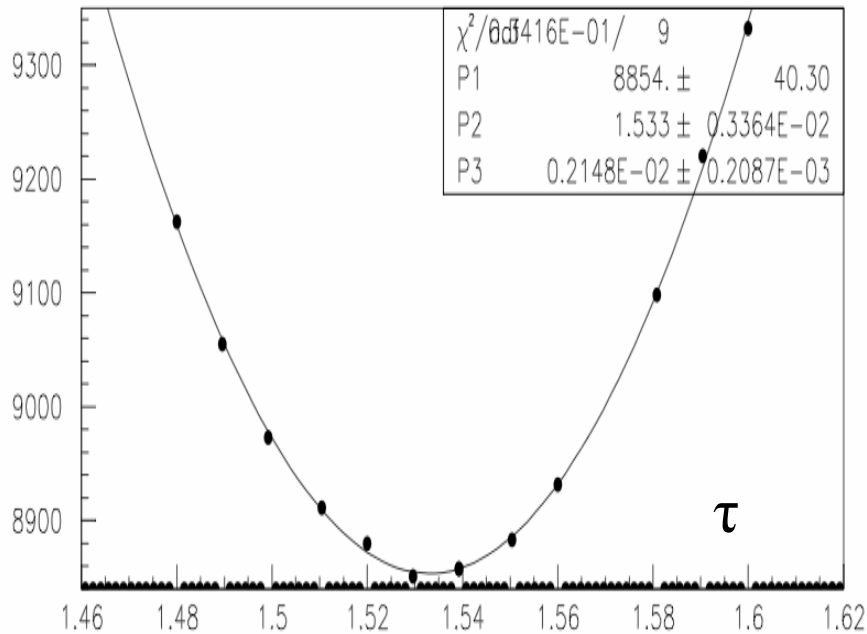


$|q/p|-1 = -0.0014 \pm 0.0006$
in agreement with MB+SB average

- Result compatible with sharing common A_{tag} , A_{rec} between SIGNAL & BKG and $\sim 2\sigma$ $|q/p|$ bias... due to the SB component.

B⁰ SIGNAL+BKG: MB+SB Results

- Scan performed by using common Atag & Arec for SIGNAL & BKG



Results on B⁰ Monte Carlo:

$$\tau_{B^0} = 1.5330 \pm 0.0021$$

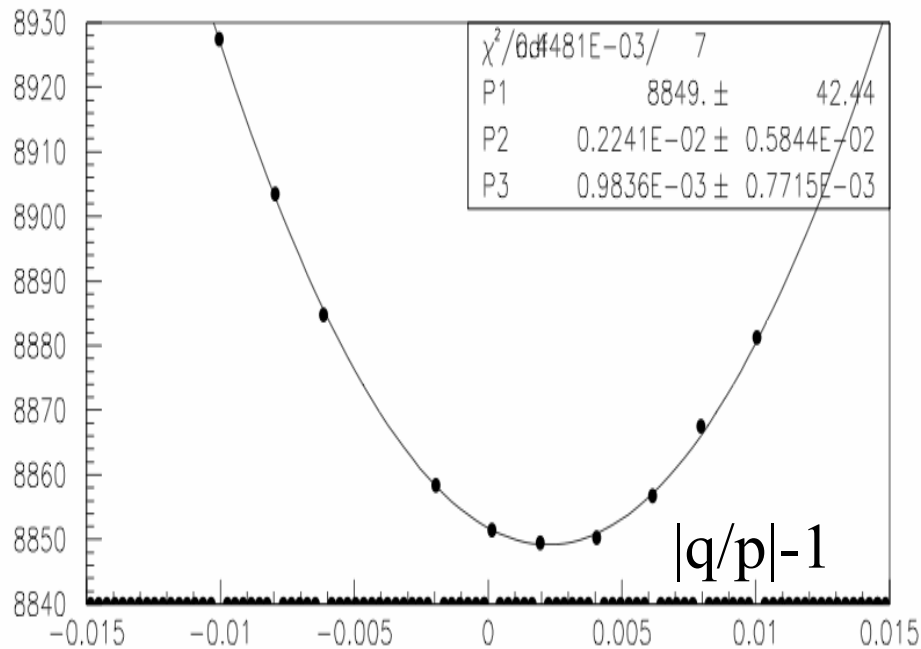
$$\Delta m = 0.4914 \pm 0.0012$$

$$\delta\tau = -0.0070 \pm 0.0021$$

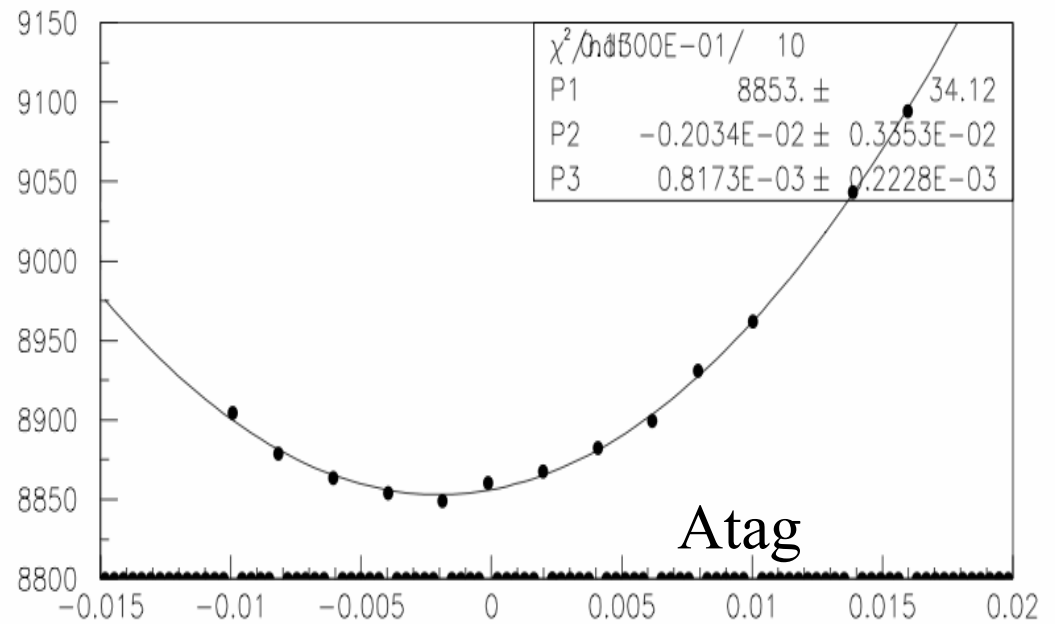
$$\delta\Delta m = 0.0024 \pm 0.0012$$

**0.5% bias
on both!**

B⁰ SIGNAL+BKG Results



$$|q/p|-1 = 0.0022 \pm 0.0010$$



$$A_{\text{tag}} = -0.0020 \pm 0.0008$$

$$A_{\text{rec}}(e) \sim 0.0030$$

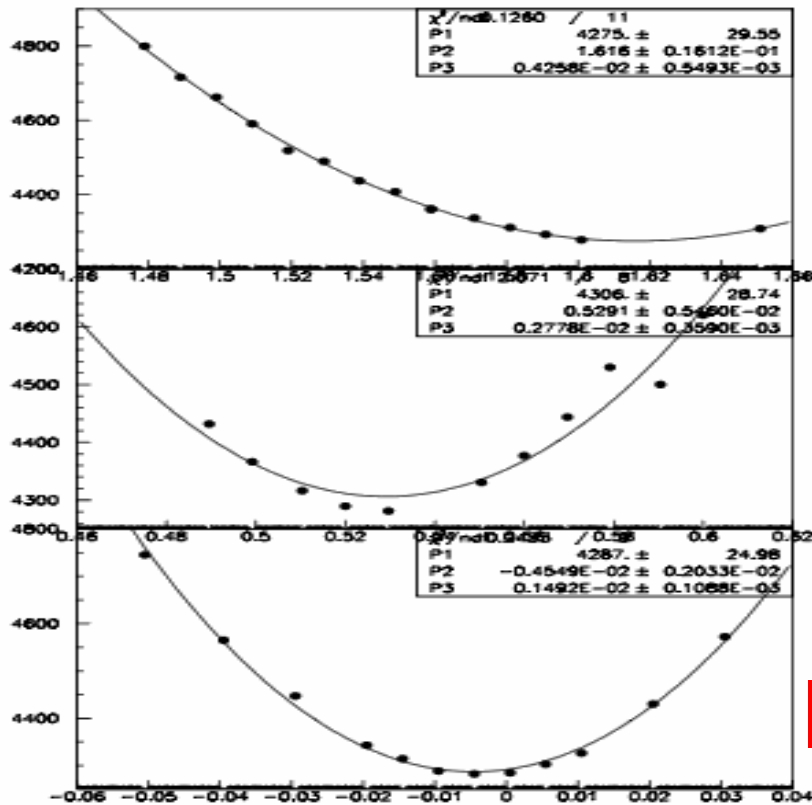
$$A_{\text{rec}}(\mu) \sim 0.0090$$

- $|q/p|$ bias still at the level of one statistical sigma of real data RUN1-RUN5 result... but it is however stretched in the $|q/p|_{\text{BKG}}$ direction...
- $A_{\text{tag}} < 0$ as before; A_{rec} remain stable between SIG & BKG results;
- Feeling that it is not completely right to share the same charge asymmetry between SIG & BKG...

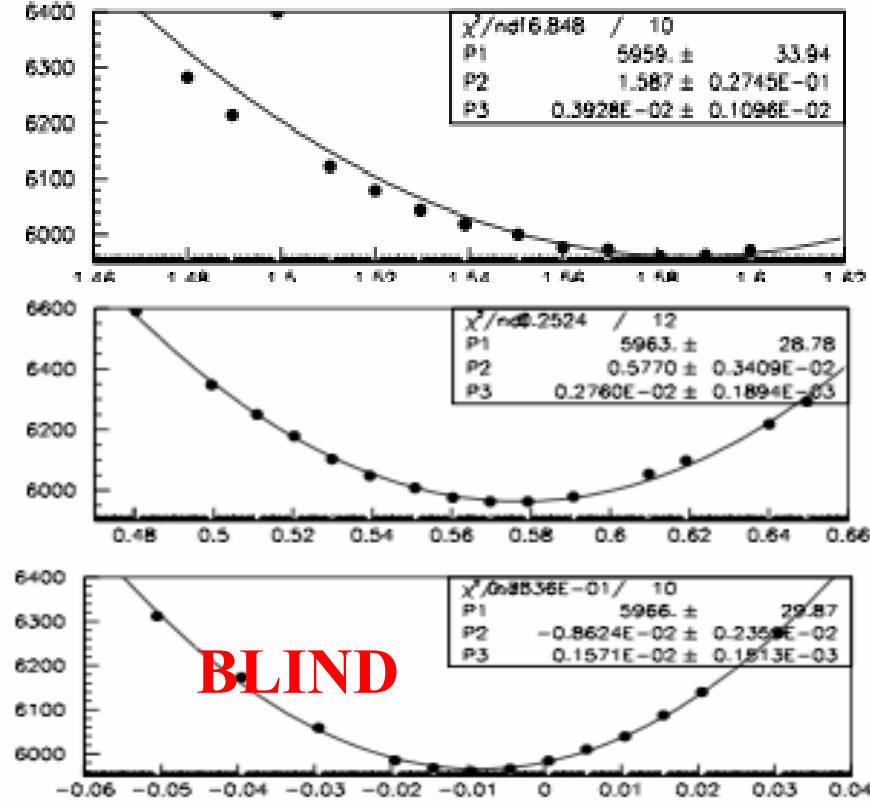
Very Preliminary Full Fit Results

B⁺ BKG & continuum added to the MC sample

MC



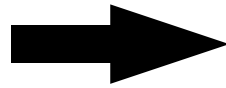
DATA



$$\delta\tau = 0.076 \pm 0.004$$

$$\delta\Delta m = 0.040 \pm 0.003$$

$$|q/p| - 1 = -0.0045 \pm 0.0015$$



• τ_{B0} & Δm out of control... what's happening?

- **Data show the same behavior**
- **Again the 0.004 bias on $|q/p|$...**

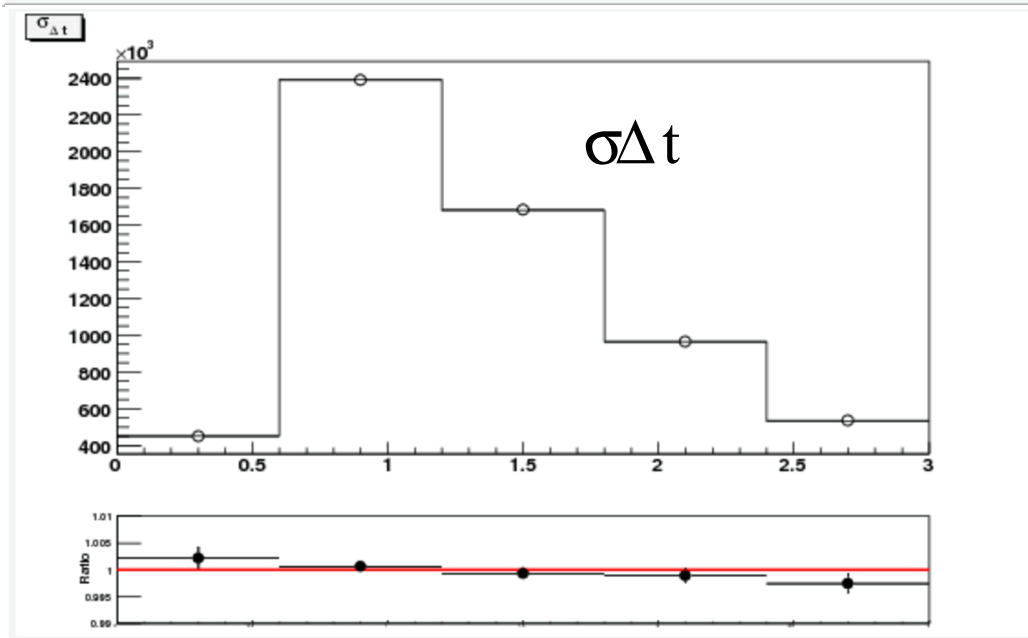
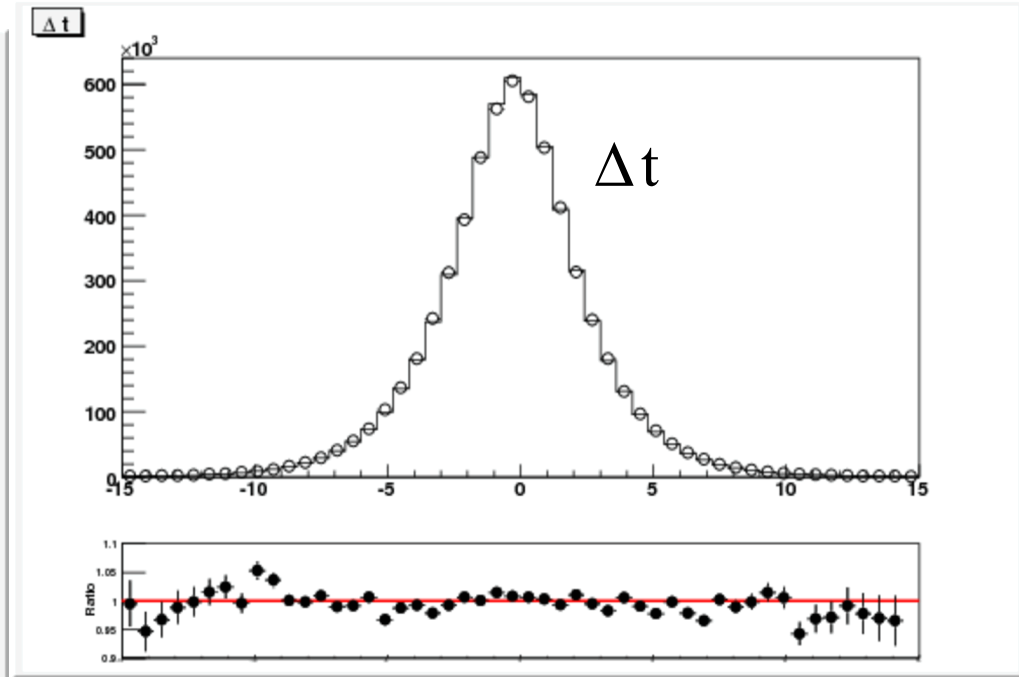
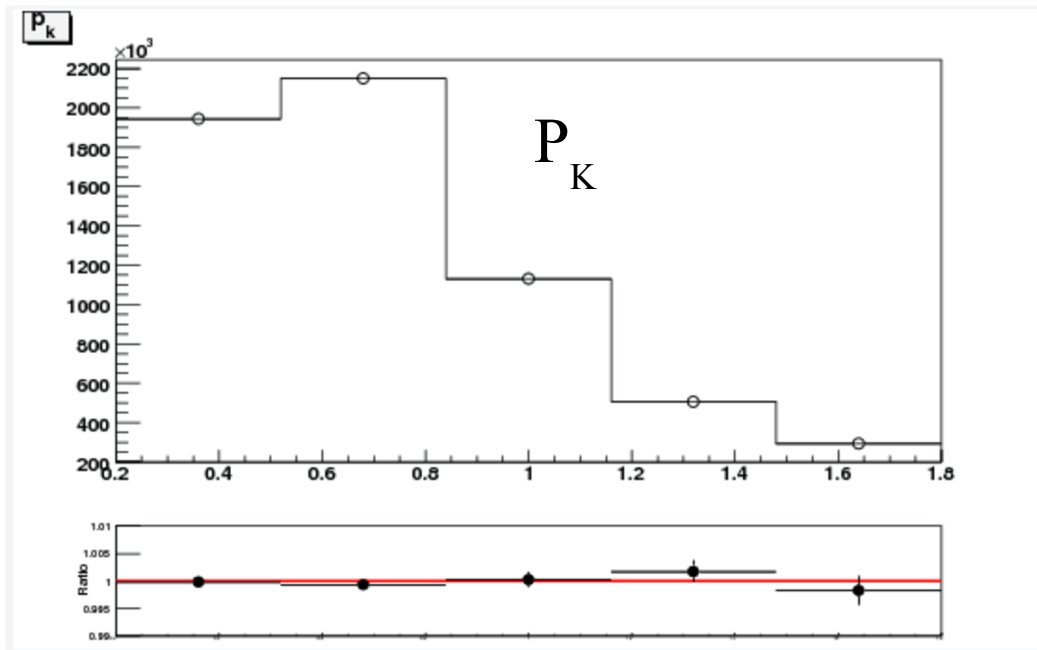
- Different A_{tag} , A_{rec} , $|q/p|$ for Signal & BKG?
- Launched scans to check this guess (work in progress)

Toy MC

Enrico Feltresi

- Generate several experiment starting from the **fitted PDF**($P_K, \Delta t, \sigma \Delta t$) for the various sample categories (B^0/B^+ /continuum; peaking/BKG; Btag/Dtag) both for **MC and Real Data**;
- **Fit separately every generated data set**;
- **MC fit validation**: study the pull of the various fits result vs MC truth/(vs nominal fit result) to check the nominal statistical error & to look for a possible analysis bias (to be done, waiting for the nominal fit result);
- **DATA fit validation**: study the pull of the various fits result vs the nominal fit one (to be done, waiting for the nominal fit result);

Comparison between nominal/generated distributions



MC B^0 SIG Btag
(E. Feltresi)

Strategy for full fit validation under debugging.

Conclusion & Next Steps

- Strategy to reach the fit convergence & evaluate the analysis bias finalized;
- No bias found on $|q/p|$, τ_{B^0} and Δm on MC Pure Signal;
- Some hints of different detector charge asymmetry between Signal & BKG which could be the cause of :
 - $|q/p|$ bias = 0.0022 ± 0.0010 on MC B^0 (Signal+BKG);
 - $|q/p|$ bias = -0.0045 ± 0.0015 on Full MC;
- No bias on τ_{B^0} and Δm on MC B^0 (Signal+BKG);
- Strong bias on τ_{B^0} and Δm after the addition of B^+ & continuum BKG
- Toy MC for full fit validation almost finalized;
- Full MC & Data scans using different charge asymmetries between Signal & BKG are going on...

Publication Strategy (to be chosen)

A) Benefit from the binned fit & likelihood scan in order to fully understand the origin of analysis bias before the publication;

B) Send a preliminary result to ICHEP with a bias correction of ~ 0.004 on $|q/p|$ without measuring τ & Δm ;

C) Let's wait for the results of the scans using different charge asymmetries for Signal & BKG...

- Updated Supporting Document & Conference Paper ready in a few days (in the case ICHEP is still the target).