

$B \rightarrow X_{s/d} \gamma$ & $B \rightarrow X_{s/d} l^+l^-$



Martino Margoni
Universita` di Padova & INFN
(on behalf of the BaBar Collaboration)

Outlook:

- $B \rightarrow X_{s/d} \gamma$:

Motivations

$X_s \gamma$ (Belle), Acp ($X_{s+d} \gamma$) (BaBar), $|V_{td}/V_{ts}|$ (BaBar)

Spectral Moments

- $B \rightarrow X_{s/d} l^+l^-$:

Motivations

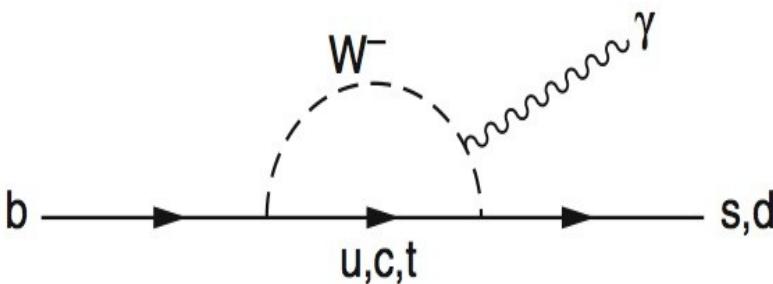
$K^{(*)} l^+l^-$ (Belle), $K^{(*)}\mu^+\mu^-$ (CDF), $K^+\tau^+\tau^-$ (BaBar)

πl^+l^-

- Conclusion



$B \rightarrow X_{s/d} \gamma$: Motivations



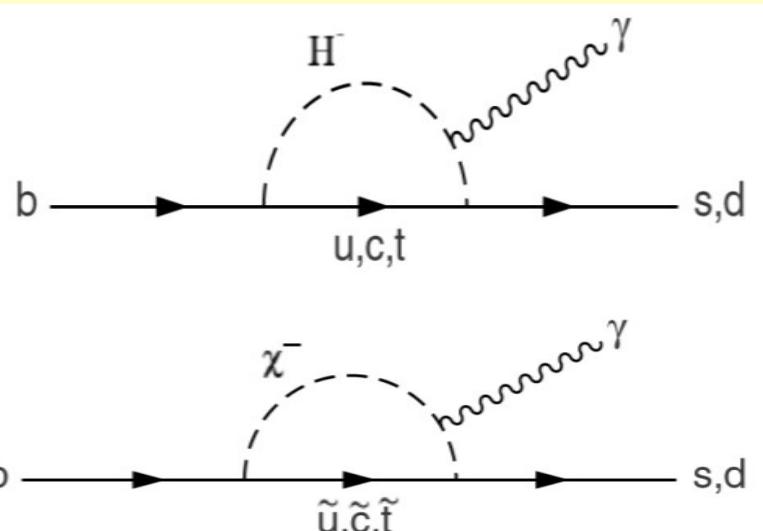
FCNC process forbidden at tree level:
Probe the SM!

NNLL order $\text{BR}(b \rightarrow s\gamma)_{(E^*\gamma > 1.6 \text{ GeV})} = (3.15 \pm 0.23) * 10^{-4}$
(Misiak et al. PRL 98 022002)

Search for New Physics

New heavy particles in the loop
could:

- Modify BR wrt SM prediction
- Modify Direct A_{CP}



**Radiative
Penguins are
an Excellent
Laboratory for**

Study the dynamics
of b-quark inside B
mesons

- Provide inputs to Global Fits in the Kinetic Scheme to V_{cb} , V_{ub} & Heavy Quark Expansion parameters.

Measure $|V_{td}/V_{ts}|$ from

- $\text{BR}(b \rightarrow d\gamma)/\text{BR}(b \rightarrow s\gamma)$
- NP could affect in different way
 $X_s \gamma$ vs $X_d \gamma$ final states

$B \rightarrow X_{s/d} \gamma$ Measurements

Exclusive Measurements

- Experimentally easier, reconstruct resonances ($K^*\gamma$, $\rho(\omega)\gamma$) with low Background
- Need Form Factors, modeling X_s fragmentation
- Affected by large theoretical uncertainties ($\delta|V_{td}/V_{ts}| \sim 7\%$)

VS

Inclusive Measurements

- Smaller theoretical error exploiting quark-hadron duality (small hadronization effects)
- Experimentally harder, large background

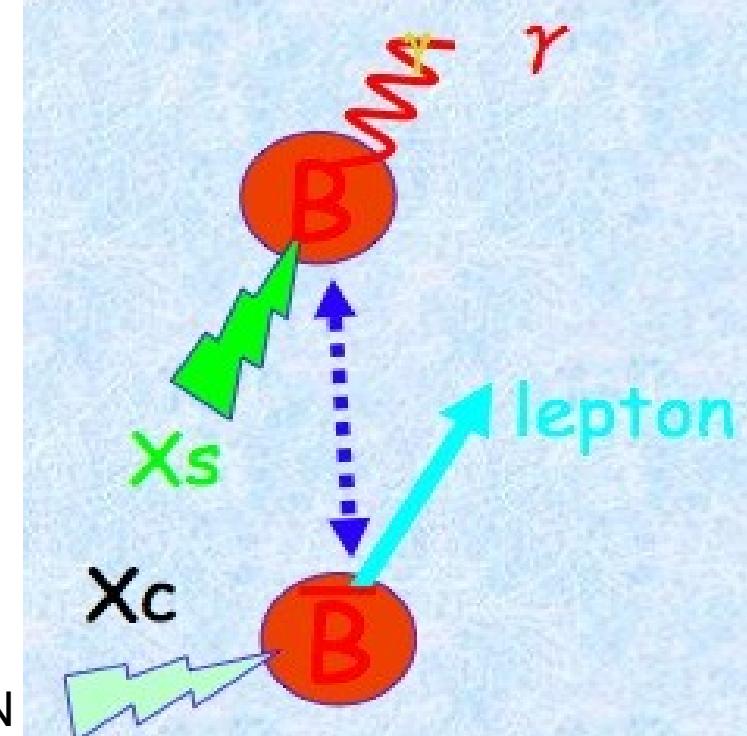
Recent Analyses Strategies:

Make the measurement **as inclusive as possible**, suppressing backgrounds via:

- Cut on $E_\gamma > [1.7-2.0] \text{ GeV}$
- Use recoil of reconstructed B or Lepton Tag

OR

- Cut on $E_\gamma, M(X_{s/d}) < [1.8-2.0] \text{ GeV}$
- Sum over many exclusive modes



Belle Inclusive $B \rightarrow X_s \gamma$ (605 fb⁻¹)

PRL 103, 241801

- B-Meson Not Reconstructed: **Not distinguish Xs & Xd !**

- Select High Energy Isolated γ
 $E\gamma(B_{CM}) > 1.7$ GeV

Lowest threshold up to now, covered
97% of Xs spectrum, smallest model
uncertainty

- π^0/η suppressed exploiting $m_{\gamma\gamma}$,
shower profile, $E\gamma$, $\theta\gamma$
- Bhabha events overlapped with B
decays removed using timing
informations in 60% of Data

- Dominant Background from Continuum suppressed by means of two
different analyses streams (largely statistically uncorrelated) based on:

- Lepton Tag:
 $(1.26 \text{ GeV} < P_{\text{lept}}^* < 2.20 \text{ GeV})$

- Two Fisher discriminants exploiting
Energy Flow & Event Shape

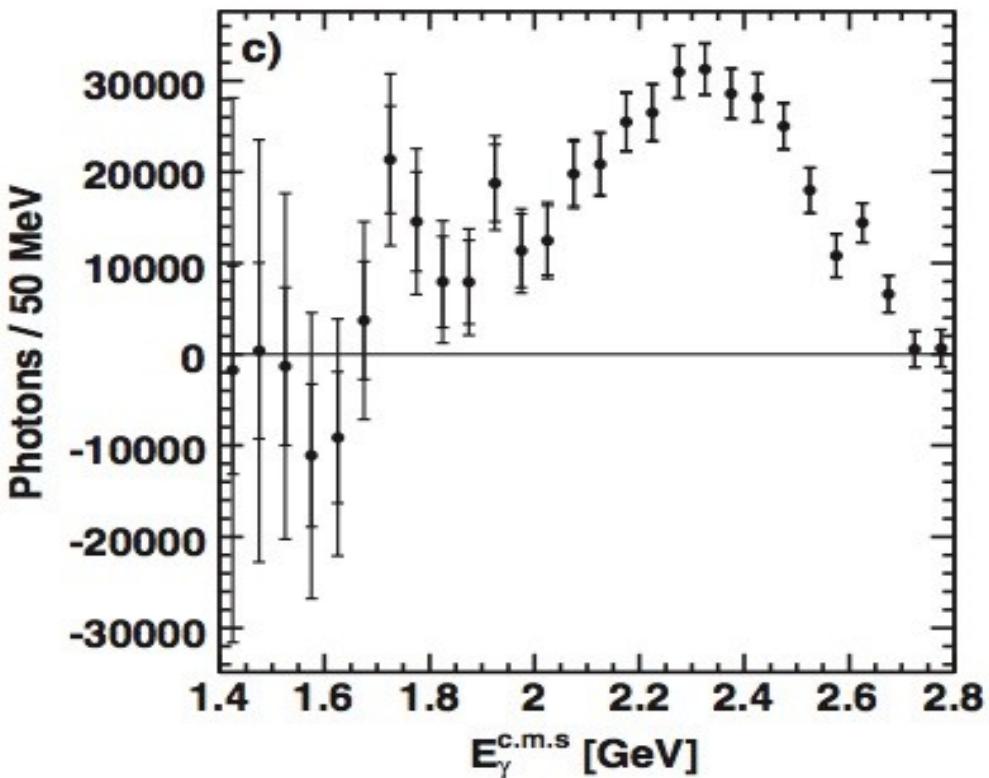
- Residual amount subtracted used off-resonance Data (corrected for Energy
effects)

- $B\bar{B}$ Background from π^0/η decays estimated using Data-Corrected MC
samples and subtracted

- BKG Subtraction checked in control regions $E\gamma(Y_{CM}) < 1.7 \text{ GeV} (> 2.8 \text{ GeV})$
for $B\bar{B}$ (Continuum): No bias found

Belle Inclusive $B \rightarrow X_s \gamma$ (605 fb $^{-1}$)

PRL 103, 241801



E_γ Cut (GeV) $\text{BR}(B \rightarrow X_s \gamma) (10^{-4})$

1.7 $3.45 \pm 0.15 \pm 0.40$

2.0 $3.02 \pm 0.10 \pm 0.11$

- True Spectrum obtained by means of efficiency correction & unfolding procedure

- X_d contribution subtracted assuming $B(X_d)/B(X_s)=4.5\%$
[Hurth et al., Nucl. Phys. B704 56,
Charles et al., Eur. Phys. C41 1]

To date:

- Most Inclusive Result, lowest theory error**
- Most Precise Result, lowest systematic error**

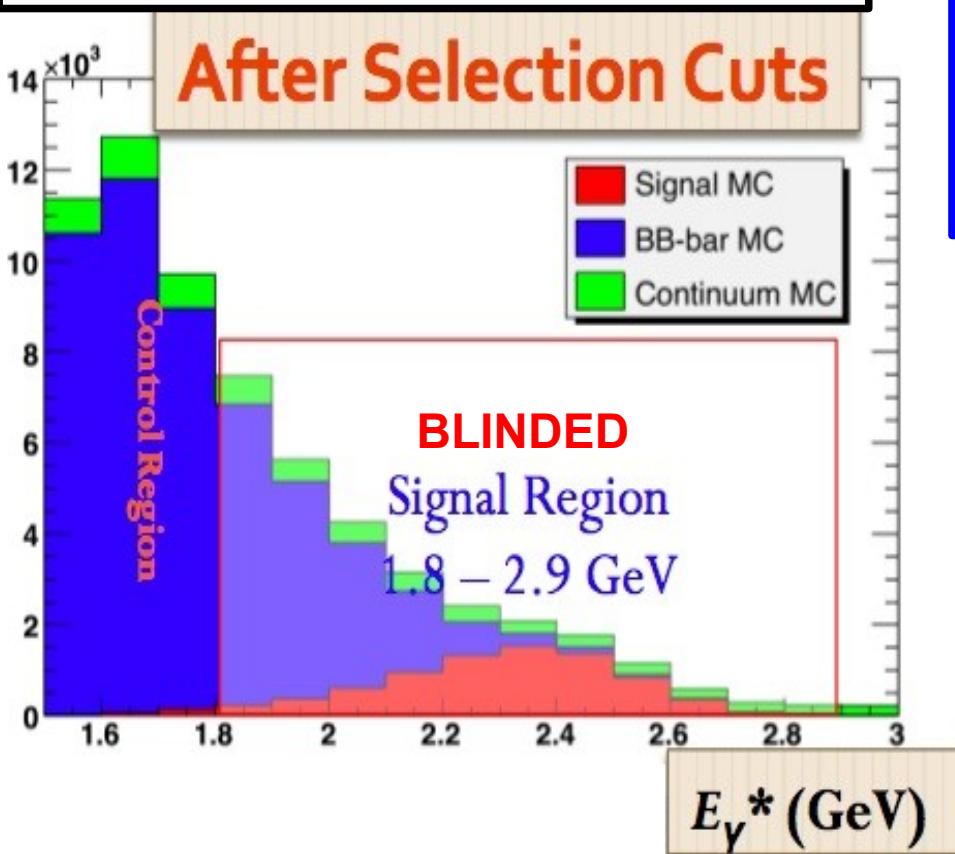
- Systematics dominated by Continuum & $\bar{B}B$ BKG subtraction

BaBar $B \rightarrow X_{s+d} \gamma$ Lepton Tag (347 fb^{-1})

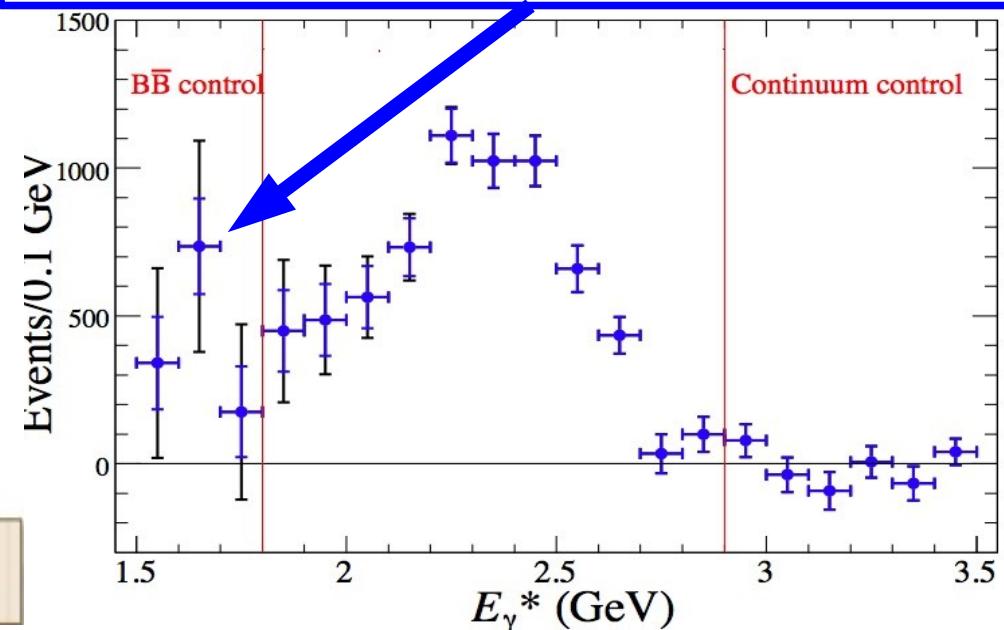
PRELIMINARY

Similar to Lepton-Tag Belle Analysis:

- Continuum suppressed using Lepton-Tag & Neural Network (Event Shape, P^* _{lept}, $\theta_{\gamma\text{-lept}}$)



- $\bar{B}\bar{B}$ Background Estimated on MC & corrected on DATA control samples (97% of BKG yield)
- Background subtraction test: 1.4σ bias found in the BB control region, partly due to a tail of 100-400 signal events (depending on model)



BaBar $B \rightarrow X_{s+d} \gamma$ Lepton Tag (347 fb^{-1})

SM predicts $A_{CP}^{SM}(s+d) \sim 10^{-6}$

from almost perfect cancellation between X_s and X_d

[Hurth et al., hep-ph 0312260, hep-ph 0103331]

Experimentally:

$$A_{CP}(B \rightarrow X_{s+d}\gamma) = \frac{1}{1 - 2\omega} \cdot \frac{N^+ - N^-}{N^+ + N^-}$$

Lepton Charge gives B flavor

- Dilution due to mixing, cascade decays, fakes, $\omega \sim 13\%$

- Most of the systematics common for +/- leptons cancel in A_{CP}

Possible Bias from:

- $B\bar{B}$ Background asymmetry: checked in control region (-0.004 ± 0.006 effect)
- Lepton tag asymmetry = 0.011 ± 0.011 measured in DATA control samples (e^+e^- , $\mu\mu\gamma$, $K^*J/\Psi(l^+l^-)$)
- Estimated error ± 0.013 (Main Systematic Uncertainty)

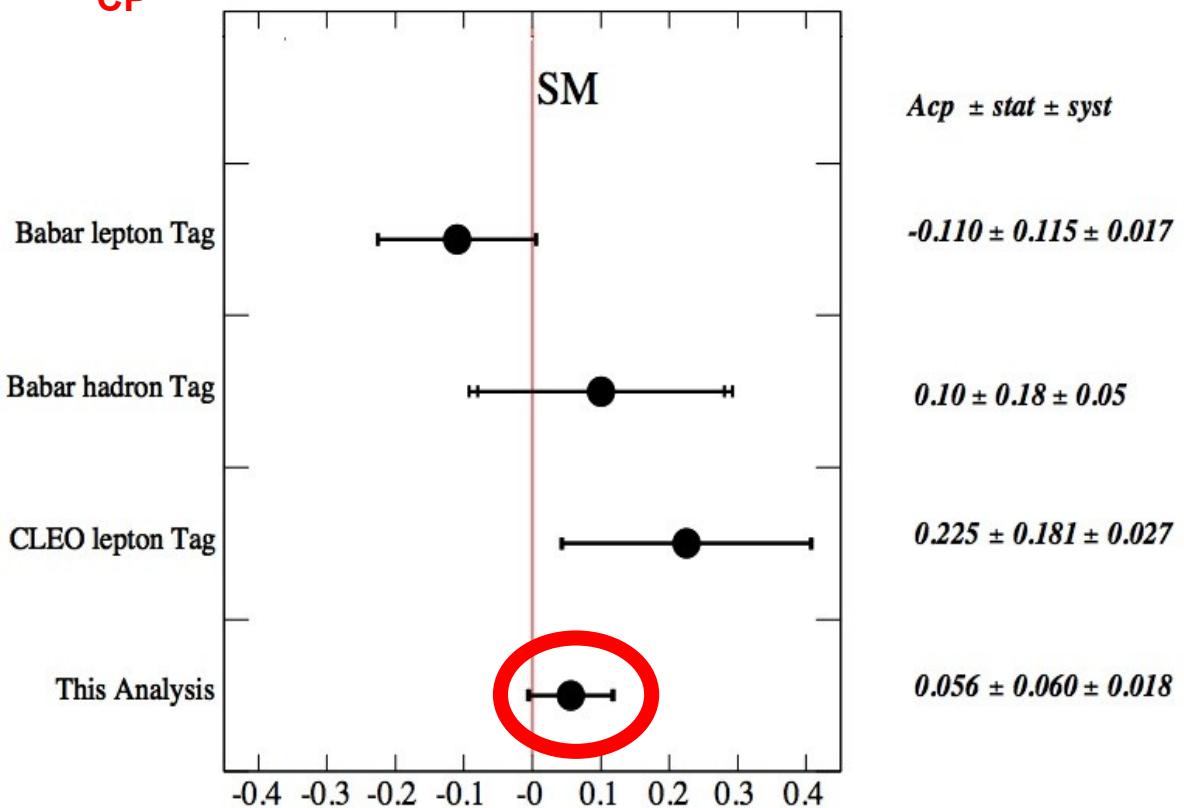
BaBar $B \rightarrow X_{s+d} \gamma$ Lepton Tag (347 fb^{-1})

Preliminary Result

$$N(l^+) = 2623 \pm 158$$

$$N(l^-) = 2397 \pm 151$$

$$A_{CP} = 0.056 \pm 0.060(\text{stat}) \pm 0.018(\text{syst})$$



- A_{CP} total error minimized with $2.1 \text{ GeV} < E\gamma(Y_{CM}) < 2.8 \text{ GeV}$

- Statistical error dominated by continuum subtraction

- Most precise measurement to date
- Consistent with SM expectation

Same analysis will provide soon also BR and spectral moments.

BaBar $|V_{td}/V_{ts}|$ (423 fb $^{-1}$)

[PRD-RC 82, 051101]

- Ratio of Exclusive modes $B \rightarrow (\rho, \omega)\gamma$, $K^*\gamma$ provides a $|V_{td}/V_{ts}|$ measurement complementary to the more precise result from $\Delta m_d/\Delta m_s$

- New Physics could affect $b \rightarrow s\gamma/d\gamma$ in different way

Inclusive Measurements reduce theory error from 7% to ~1%

Experimentally:

- Inclusive rates extrapolated from a sum of 7 exclusive modes:

$B \rightarrow X_d\gamma$	$B \rightarrow X_s\gamma$
$B^0 \rightarrow \pi^+ \pi^- \gamma$	$B^0 \rightarrow K^+ \pi^- \gamma$
$B^+ \rightarrow \pi^+ \pi^0 \gamma$	$B^+ \rightarrow K^+ \pi^0 \gamma$
$B^+ \rightarrow \pi^+ \pi^- \pi^+ \gamma$	$B^+ \rightarrow K^+ \pi^+ \pi^- \gamma$
$B^0 \rightarrow \pi^+ \pi^- \pi^0 \gamma$	$B^0 \rightarrow K^+ \pi^- \pi^0 \gamma$
$B^0 \rightarrow \pi^+ \pi^- \pi^+ \pi^- \gamma$	$B^0 \rightarrow K^+ \pi^- \pi^+ \pi^- \gamma$
$B^+ \rightarrow \pi^+ \pi^- \pi^+ \pi^0 \gamma$	$B^+ \rightarrow K^+ \pi^- \pi^+ \pi^0 \gamma$
$B^+ \rightarrow \pi^+ \eta \gamma$	$B^+ \rightarrow K^+ \eta \gamma$

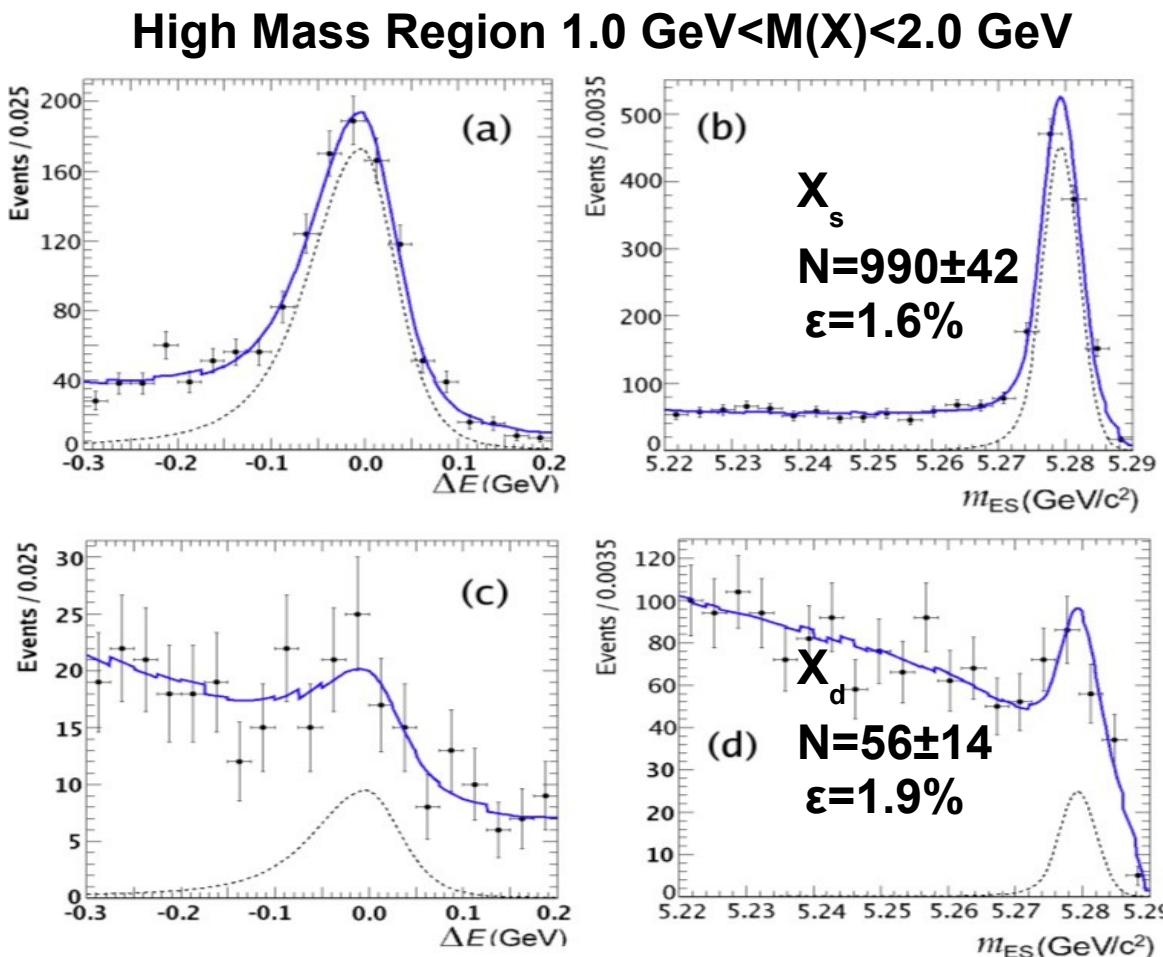
Add estimated missing states using Jetset $X_{s/d}$ fragmentation models corrected for measured exclusive X_s BRs [PRD 72, 052005]

Use two hadronic mass bins:

- $0.5 < M(X) < 1.0 \text{ GeV}$ (contain the previously measured K^* , ρ, ω states)
- $1.0 < M(X) < 2.0 \text{ GeV}$

BaBar $|V_{td}/V_{ts}|$ (423 fb $^{-1}$)

- Select High Energy Isolated γ
- π^0/η suppression by $m_{\gamma\gamma}$ cut
- Same cuts to $s\gamma/d\gamma$ final states reduce systematics in the BR ratio
- Continuum suppressed using Neural Network (event shape)



- Yields from Simultaneous Fit to

$$\Delta E = E_B^* - E_{\text{beam}}$$

$$m_{\text{ES}} = \sqrt{E_{\text{beam}}^{*2} - \vec{p}_B^{*2}}$$

0.5 GeV < M_{HAD} < 2.0 GeV

$\text{BR}(b \rightarrow s\gamma) = 230 \pm 8 \pm 30 \times 10^{-6}$

$\text{BR}(b \rightarrow d\gamma) = 9.2 \pm 2.0 \pm 2.3 \times 10^{-6}$

first measurement in high mass region

BaBar $|V_{td}/V_{ts}|$ (423 fb $^{-1}$)

- Extract $|V_{td}/V_{ts}|$ from:

$$\frac{\Gamma(b \rightarrow d\gamma)}{\Gamma(b \rightarrow s\gamma)} = \xi^2 \left| \frac{V_{td}}{V_{ts}} \right|^2 (1 + \Delta R)$$

[Ali et al. Phys. Lett. B 429, 87]

- Unmeasured $M(X) > 2.0$ GeV extrapolated using Kagan-Neubert spectral shape

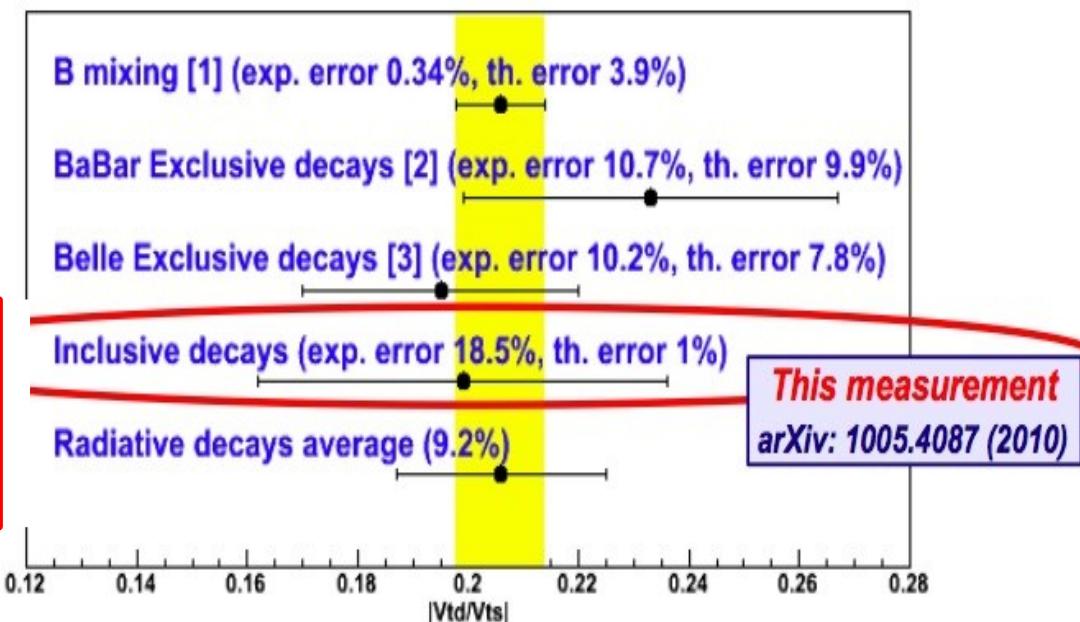
[PRD 58, 094012]

$$|V_{td}/V_{ts}| = 0.199 \pm 0.022(\text{stat}) \pm 0.024(\text{syst}) \pm 0.002(\text{th})$$

- Systematics dominated by Extrapolation to Inclusive Rates (alternative fragmentation models)

- Compatible & Competitive with Previous Exclusive Decays Results (with lower theory error) !

- ξ (SU(3) Breaking), ΔR (annihilation correction) computed in terms of Wolfenstein parameters (ρ, η)
- (ρ, η) re-expressed in terms of angle β to avoid circularity from previous $|V_{td}/V_{ts}|$ measurements



$\text{BR}(\text{B} \rightarrow \text{X}_s \gamma)$: Summary

- Experiments cut on minimum E_γ
- BR extrapolated to $E_{\min} = 1.6 \text{ GeV}$ using Shape Functions (correlated error)
- Error dominated by Systematics

HFAG 2010 Inclusive $\text{BR}(\text{b} \rightarrow \text{s}\gamma) \times 10^{-6}$:

Mode	\mathcal{B}	E_{\min}	$\mathcal{B}(E_\gamma > E_{\min})$	$\mathcal{B}^{\text{env}}(E_\gamma > 1.6)$
CLEO Inc. [3]	$321 \pm 43 \pm 27^{+18}_{-10}$	2.0	$306 \pm 41 \pm 26$	$327 \pm 44 \pm 28 \pm 6$
Belle Semi.[4]	$336 \pm 53 \pm 42^{+50}_{-54}$	2.24	—	$369 \pm 58 \pm 46^{+56}_{-60}$
BABAR Semi.[6]	$335 \pm 19^{+56+4}_{-41-9}$	1.9	$327 \pm 18^{+55+4}_{-40-9}$	$349 \pm 20^{+59+4}_{-46-3}$
BABAR Inc. [7]	—	1.9	$367 \pm 29 \pm 34 \pm 29$	$390 \pm 31 \pm 47 \pm 4$
BABAR Full [8]	$391 \pm 91 \pm 64$	1.9	$366 \pm 85 \pm 60$	$389 \pm 91 \pm 64 \pm 4$
Belle Inc.[5]	—	1.7	$345 \pm 15 \pm 40$	$347 \pm 15 \pm 40 \pm 1$
Average				$355 \pm 24 \pm 9$

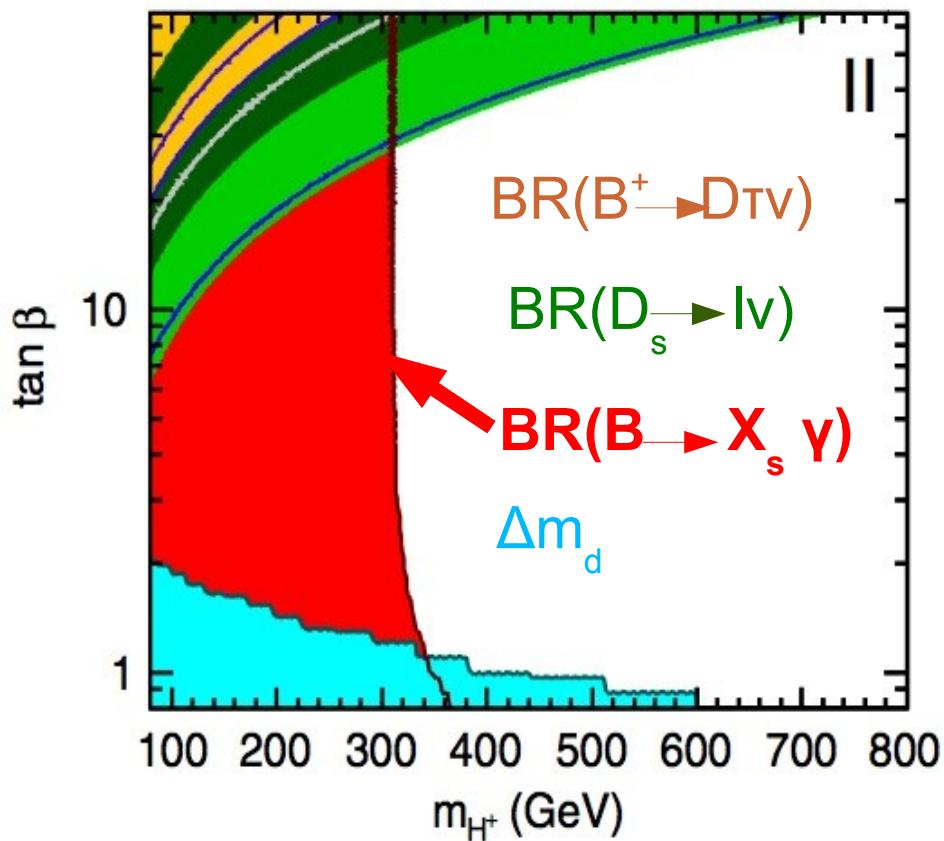
SM: $\text{BR}(\text{b} \rightarrow \text{s}\gamma)_{(E^*\gamma > 1.6 \text{ GeV})} = (315 \pm 23) \times 10^{-6}$

Misiak et al. PRL 98 022002 (2007)

5% non-perturbative error

Good Agreement (1.2σ) with NNLL prediction

$\text{BR}(\text{B} \rightarrow X_s \gamma)$: Summary



- Recent Calculations in the 2Higgs-Doublet-Model framework provide Constraints on the coupling of the 2nd & 3rd generation fermions to H^+ obtained from flavor physics experimental results:
 - $\text{BR}(B \rightarrow X_s \gamma)$, Δm_d , $\text{BR}(B^+ \rightarrow (D)\tau\nu)$, $\text{BR}(D_s \rightarrow l\nu)$
- Best Limit on $M_{H^+} > 300 \text{ GeV @ 95% CL}$**
[Mahmoudi, Stal, PRD81 035016]

$B \rightarrow s\gamma$ Spectral Moments

V_{cb} & V_{ub} from Inclusive Semileptonic Decays

- $|V_{cb}|$ from inclusive $B \rightarrow X_c^- l \bar{\nu}$ using HQET & OPE requires non perturbative parameters (mb)

Universal motion of b-quark inside B meson:

- Global Fits to the moments of inclusive distributions in $B \rightarrow X_c^- l \bar{\nu}$ & $B \rightarrow X_s^- \gamma$ in the kinetic mass scheme provides $|V_{cb}|$ together with non-perturbative parameters

[Gambino et al., Eur. Phys. C34 181-189;
Benson et al., Nucl Phys. B710, 371-401]

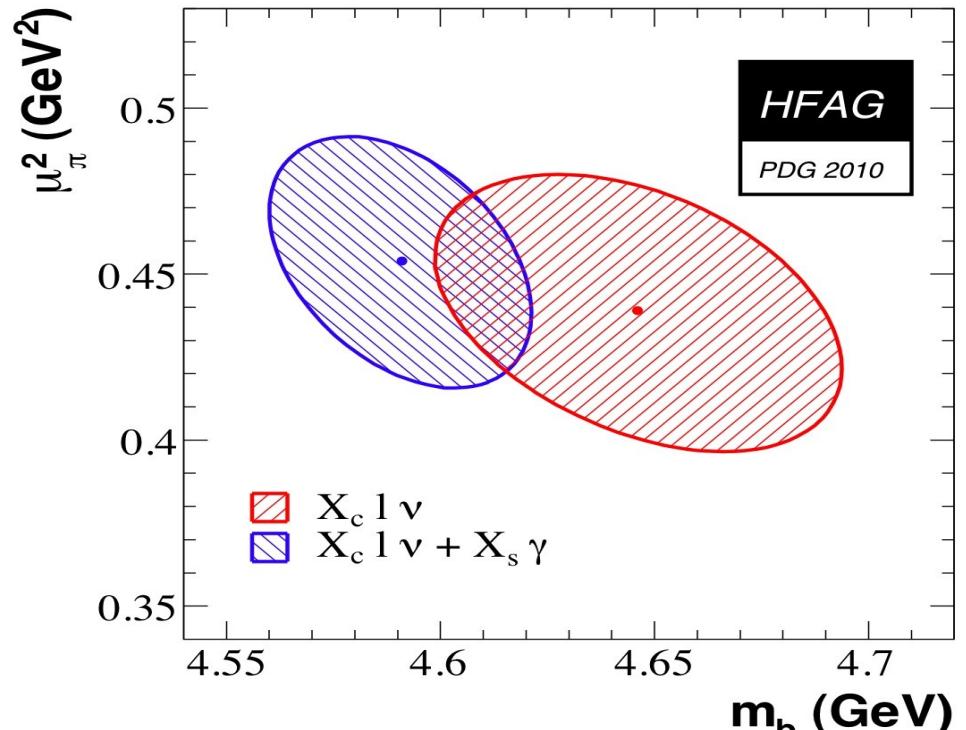
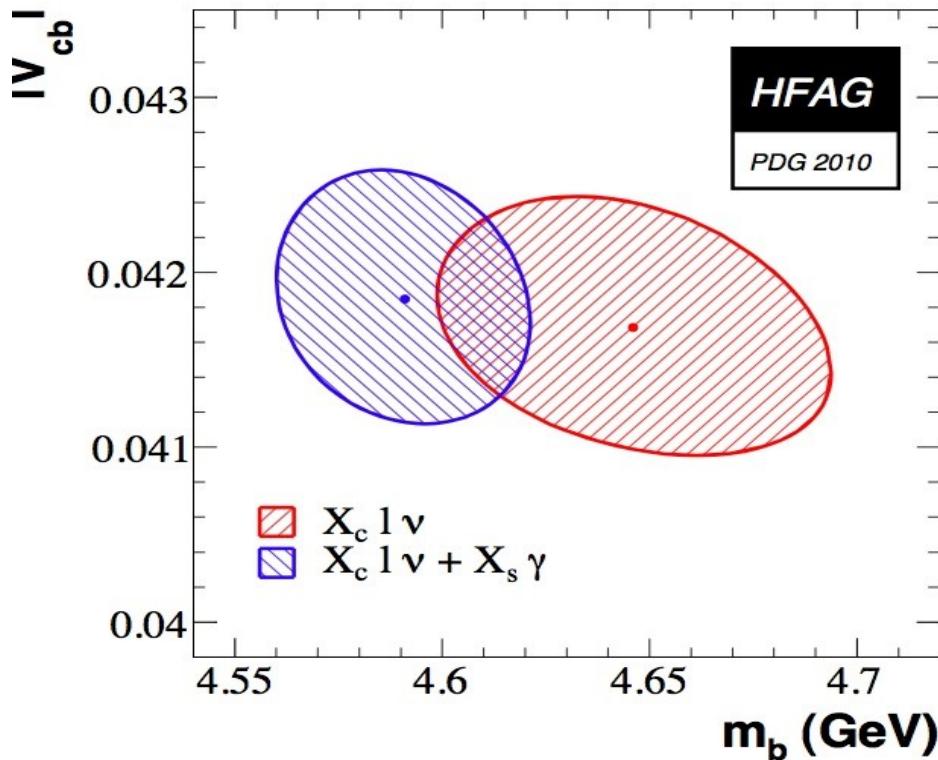
- $|V_{ub}|$ from inclusive $B \rightarrow X_u^- l \bar{\nu}$ requires Shape Function to extrapolate the Inclusive BR from Partial Rates & compute kinematic acceptances

- Uncertainties on shape function limited by comparing the inclusive $B \rightarrow X_u^- l \bar{\nu}$ rate & inclusive $B \rightarrow X_s^- \gamma$ photon spectrum

[Neubert et al., PRD 49 4623-4633 ; Leibovich et al., PRD 61 053006; Lange et al., JHEP 10 084]

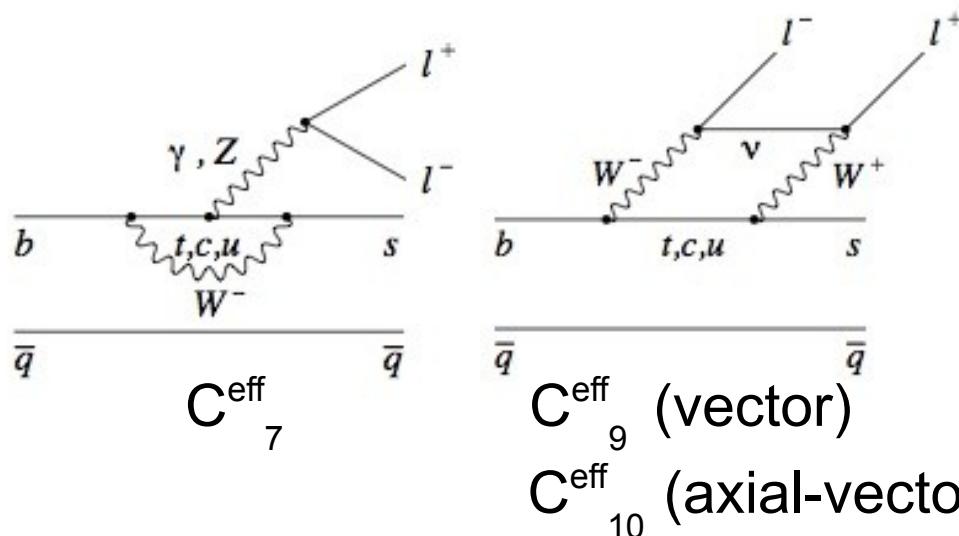
B \rightarrow s γ Spectral Moments

HFAG Fit in Kinetic Mass Scheme (2010)



Data	χ^2/dof	$ V_{cb} (10^{-3})$	$m_b^{\text{kin}} (\text{GeV})$	$\mu_\pi^2 (\text{GeV}^2)$
All moments ($X_c \ell \nu_\ell$ and $X_s \gamma$)	$29.7/(66 - 7)$	41.85 ± 0.73	4.591 ± 0.031	0.454 ± 0.038
$X_c \ell \nu_\ell$ only	$24.2/(55 - 7)$	41.68 ± 0.74	4.646 ± 0.047	0.439 ± 0.042

$B \rightarrow X_{s/d} l^+ l^-$: Motivations



FCNC process forbidden at tree level, $\text{BF} \sim 10^{-6}$: Probe the SM!
 Amplitudes expressed using OPE in terms of:

- Hadronic FF (accuracy $\sim 20\%$)
 [Bharucha et al. Hep-ph 1004.3249]
- Wilson coefficients $C_{\text{eff}}^{\text{eff}}_7$, $C_{\text{eff}}^{\text{eff}}_9$, $C_{\text{eff}}^{\text{eff}}_{10}$
 [Ali et al. PRD 61 074024, Z. Phys. C 67 417]

New Particles in the loop could:

- Modify SM Wilson Coefficients
- Introduce additional ones

Observables Include:

- Inclusive BR, $d\text{BR}/dq^2$
- A_{CP} , A_{ISOSPIN} , $\text{RK}^{(*)}$ (theory error suppressed in the ratios!)
- A_{FB} & K polarization from angular analyses (defined below)

SM predicts ($q^2 = m_{l^+ l^-}^2$):

$$A_{\text{CP}}^{K^{(*)}} \equiv \frac{\mathcal{B}(\bar{B} \rightarrow \bar{K}^{(*)} \ell^+ \ell^-) - \mathcal{B}(B \rightarrow K^{(*)} \ell^+ \ell^-)}{\mathcal{B}(\bar{B} \rightarrow \bar{K}^{(*)} \ell^+ \ell^-) + \mathcal{B}(B \rightarrow K^{(*)} \ell^+ \ell^-)} \quad \sim 10^{-3}$$

$$A_I \equiv \frac{(\tau_{B^+}/\tau_{B^0})\mathcal{B}(K^{(*)0} \ell^+ \ell^-) - \mathcal{B}(K^{(*)\pm} \ell^+ \ell^-)}{(\tau_{B^+}/\tau_{B^0})\mathcal{B}(K^{(*)0} \ell^+ \ell^-) + \mathcal{B}(K^{(*)\pm} \ell^+ \ell^-)} \quad < 10\% \quad \text{All } q^2$$

$$R_{K^{(*)}} \equiv \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)} \quad \begin{array}{l} \text{RK=1} \\ \text{RK*}=0.75 \\ (q^2 \rightarrow 0 \text{ } \gamma\text{-pole}) \end{array}$$

Belle $B \rightarrow K^{(*)} l^+ l^-$ (605 fb $^{-1}$)

PRL 103, 171801

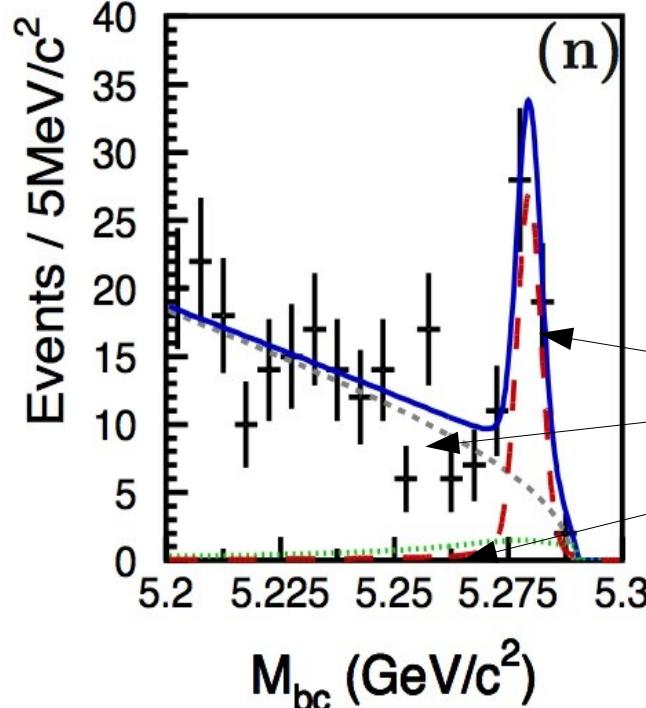
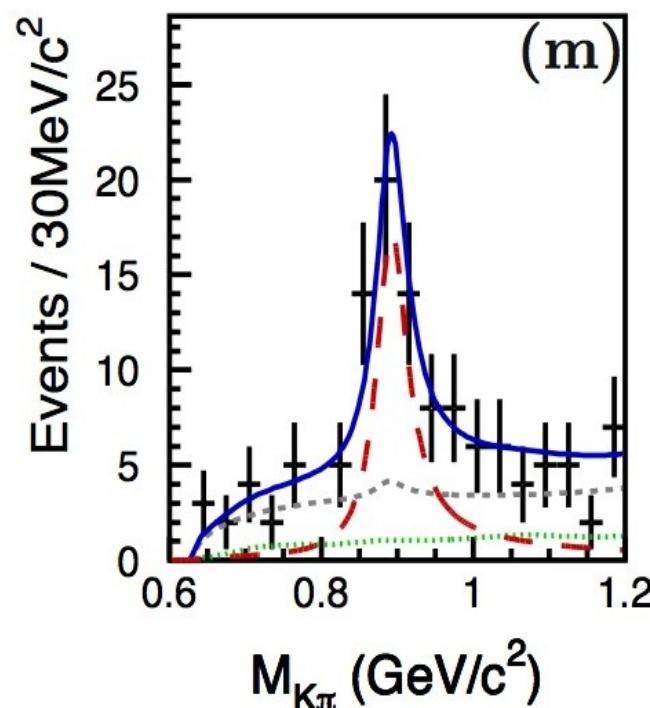
$B \rightarrow K^{(*)} l^+ l^-$ fully reconstructed in 10 final states: $(K^+ \pi^-, K_s^0 \pi^+, K^+ \pi^0, K^+, K_s^0) + l^+ l^-$

- Peaking $B \rightarrow J/\Psi(\Psi') X$ rejected by $m(l^+ l^-)$ cut

- Continuum Suppressed exploiting Event Shape Variables

- B Semileptonic Decays Suppressed using Event Shape, Missing Mass, Lepton separation

K* Fit single bin: $10.09 < q^2 < 12.86 \text{ GeV}^2$



- $K^{(*)}$ Signal Yields determined by unbinned fit to $m_{ES}, (m_{K\pi})$ in 6 q^2 bins

Full Fit
Signal
Combinatorial
 $J/\Psi(\Psi') X$

Full $q^2 = m_{l^+ l^-}^2$ range:

$N(K l^+ l^-) = 162 \pm 22$
 $N(K^* l^+ l^-) = 246 \pm 15$

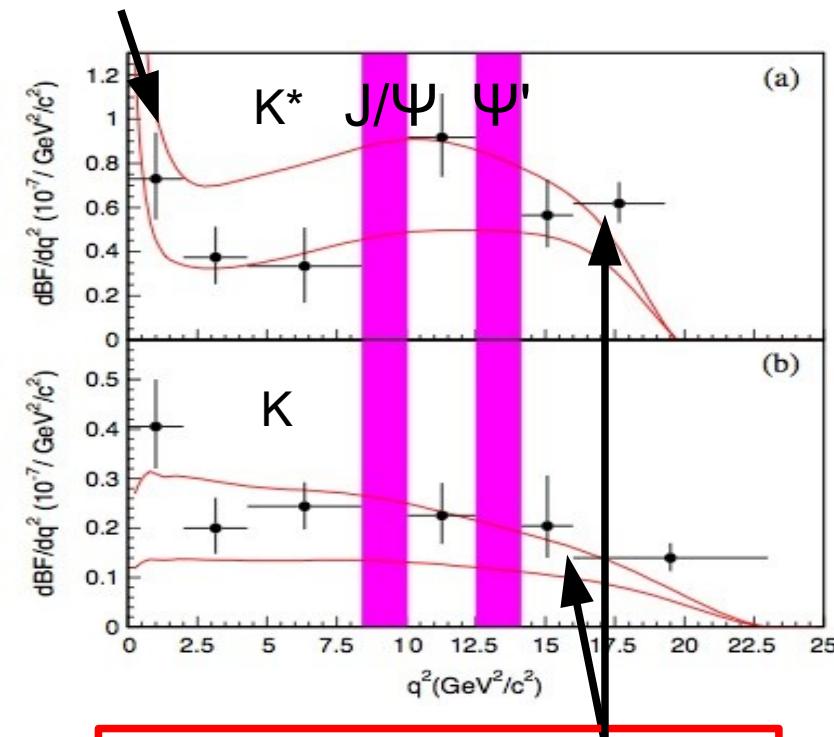
17

Belle $B \rightarrow K^{(*)} l^+ l^-$ (605 fb $^{-1}$)

$q^2 \rightarrow 0$ γ -pole

$d\text{BR}/dq^2$ from Signal Yields corrected for $\epsilon(q^2)$

PRL 103, 171801



SM prediction with different FF assumptions
 [Ali et al. PRD61 074024, PRD66 034002]

Inclusive BR, A_{CP} , A_I & e/ μ ratio agree with SM:

$$\mathcal{B}(B \rightarrow K^* \ell^+ \ell^-) = (10.7^{+1.1}_{-1.0} \pm 0.9) \times 10^{-7},$$

$$\mathcal{B}(B \rightarrow K \ell^+ \ell^-) = (4.8^{+0.5}_{-0.4} \pm 0.3) \times 10^{-7},$$

$$A_{CP}(K^* \ell^+ \ell^-) = -0.10 \pm 0.10 \pm 0.01;$$

$$A_{CP}(K^+ \ell^+ \ell^-) = 0.04 \pm 0.10 \pm 0.02.$$

$$A_I(B \rightarrow K^* \ell^+ \ell^-) = -0.29^{+0.16}_{-0.16} \pm 0.09$$

$$A_I(B \rightarrow K \ell^+ \ell^-) = -0.31^{+0.17}_{-0.14} \pm 0.08$$

$$R_{K^*} = 0.83 \pm 0.17 \pm 0.08,$$

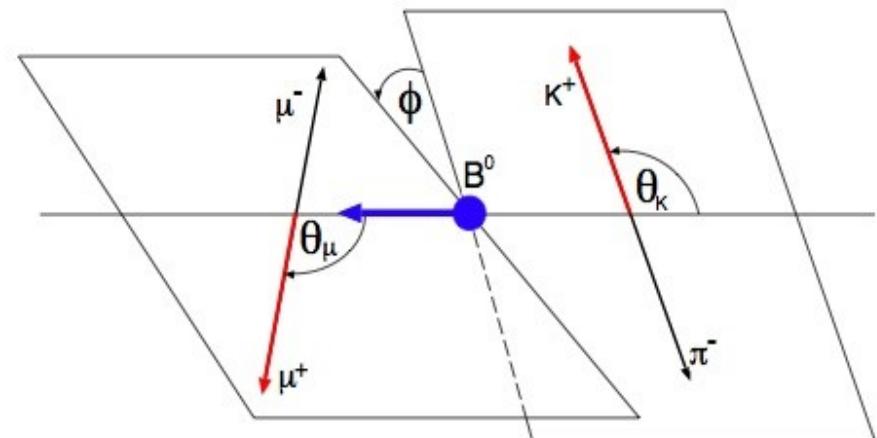
$$R_K = 1.03 \pm 0.19 \pm 0.06.$$

- Systematics dominated by tracking, PID, lepton selection & MC Decay Models

Belle $B \rightarrow K^{(*)} l^+ l^-$ (605 fb $^{-1}$)

PRL 103, 171801

- Event Angular Distribution depends on three angles
- K^* longitudinal polarization fraction F_L & lepton A_{FB} obtained from fits to θ_{K^*} & θ_l in q^2 bins

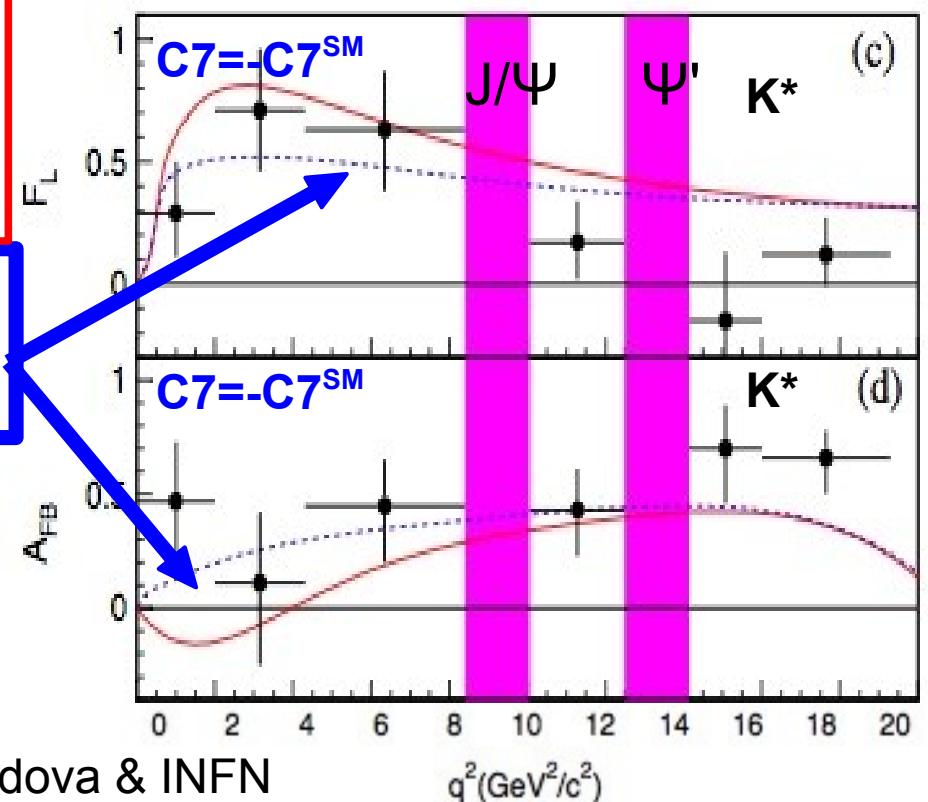


$$w(\theta_{K^*}) \sim [\frac{3}{2}F_L \cos^2 \theta_{K^*} + \frac{3}{4}(1 - F_L)(1 - \cos^2 \theta_{K^*})] \epsilon(\cos \theta_{K^*})$$

$$w(\theta_l) \sim [\frac{3}{4}F_L(1 - \cos^2 \theta_{B\ell}) + \frac{3}{8}(1 - F_L)(1 + \cos^2 \theta_{B\ell}) + A_{FB} \cos \theta_{B\ell}] \epsilon(\cos \theta_{B\ell}),$$

**AFB($q^2=m^2_{l^+l^-} < m^2(J/\Psi)$)
sensitive to C7 sign-flip**

- Dominant Systematics from fixed normalization & fixed F_L in A_{FB} fit



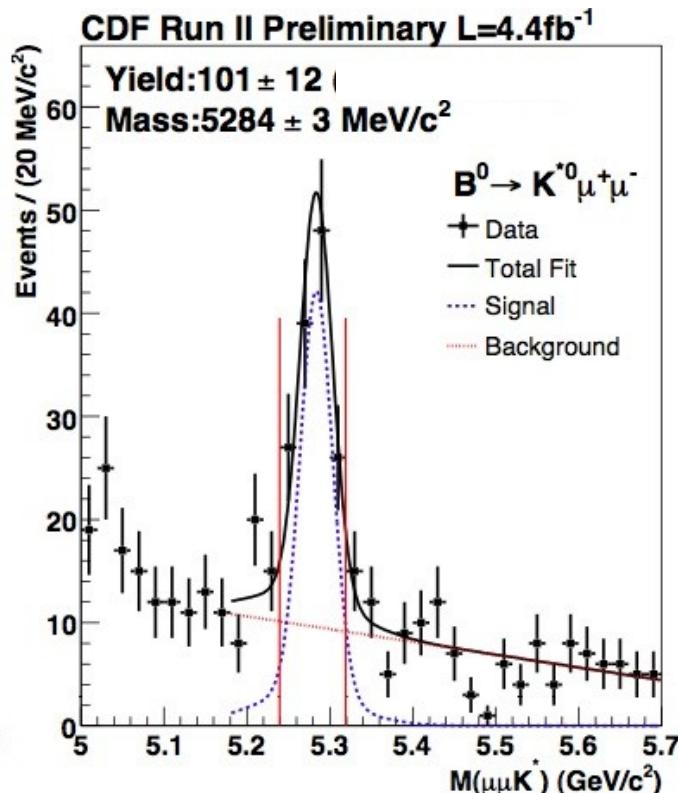
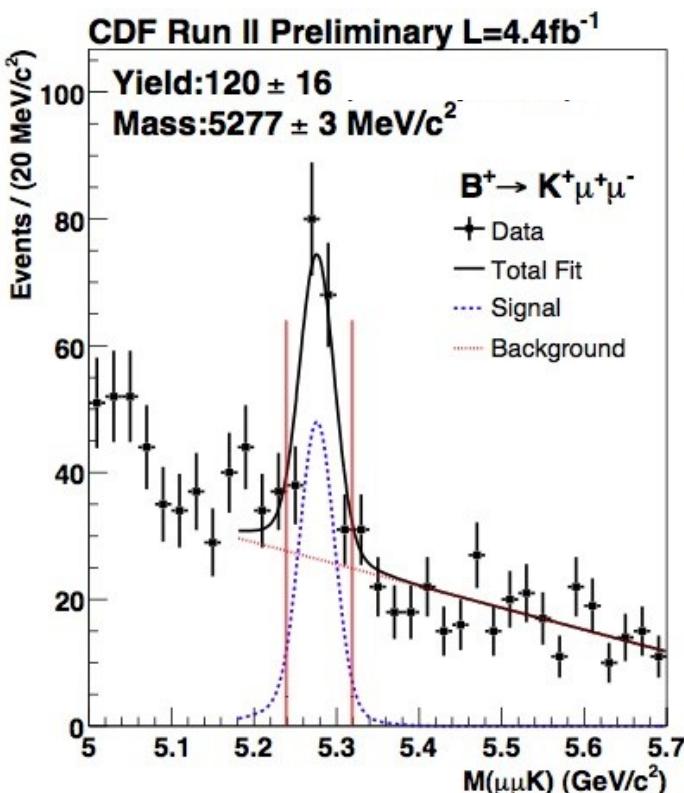
CDF $B \rightarrow K\mu\mu$ (4.4 fb^{-1})

$B \rightarrow K^{(*)}\mu^+\mu^-$ fully reconstructed ($K^* \rightarrow K^+\pi^-$)

PRELIMINARY
CDF Note 10047

- Dimuon level-3 trigger applied (P_T , VTX($\mu^+\mu^-$) informations)
- Vetoes applied to reject peaking $B \rightarrow J/\Psi (\Psi')$, $D\pi$

- Signal selected using a Neural Network (vertexes, event shape, lepton separation)



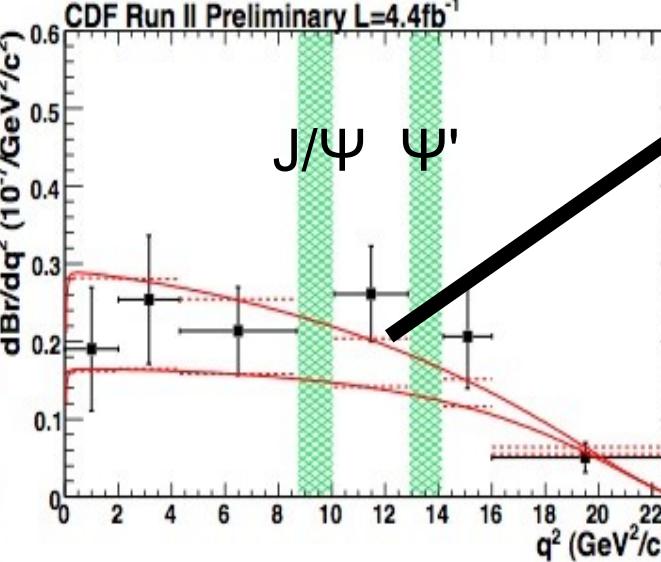
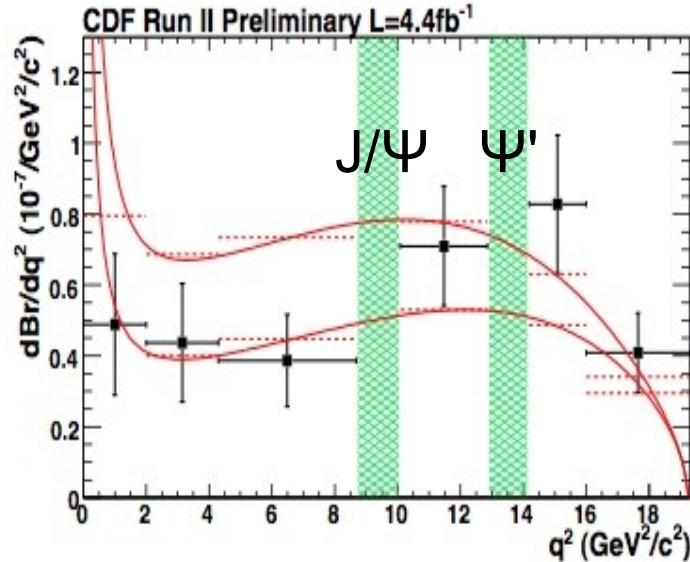
- Signal yield from unbinned likelihood fit to $m(B)$

$$N(K\mu^+\mu^-) = 120 \pm 16$$

$$N(K^*\mu^+\mu^-) = 101 \pm 12$$

CDF $B \rightarrow K\mu\mu$ (4.4 fb^{-1})

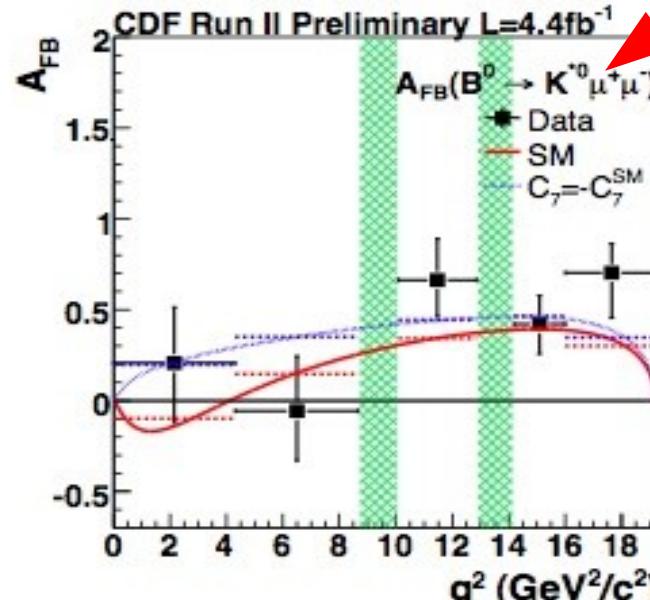
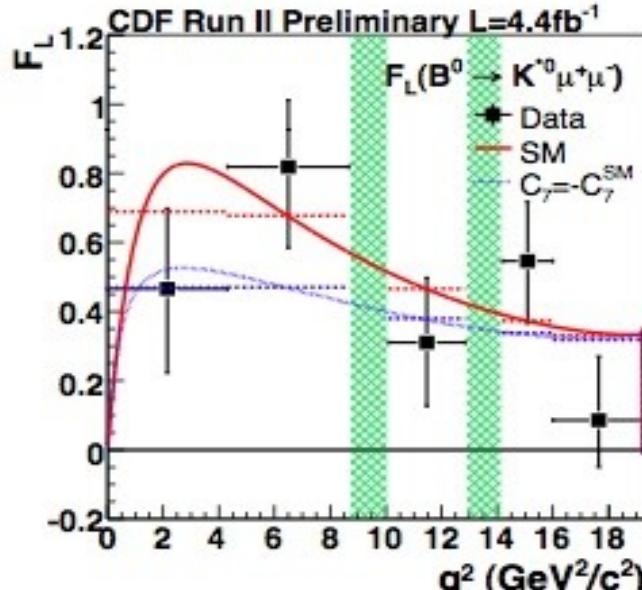
- BR computed relative to $\text{BR}(B \rightarrow J/\Psi K^{(*)})$ (identical final states) to reduce efficiency systematics in the ratio



Results consistent with SM

BR Systematics from:

- Background PDF
- $\text{BR}(B \rightarrow J/\Psi K^{(*)})$



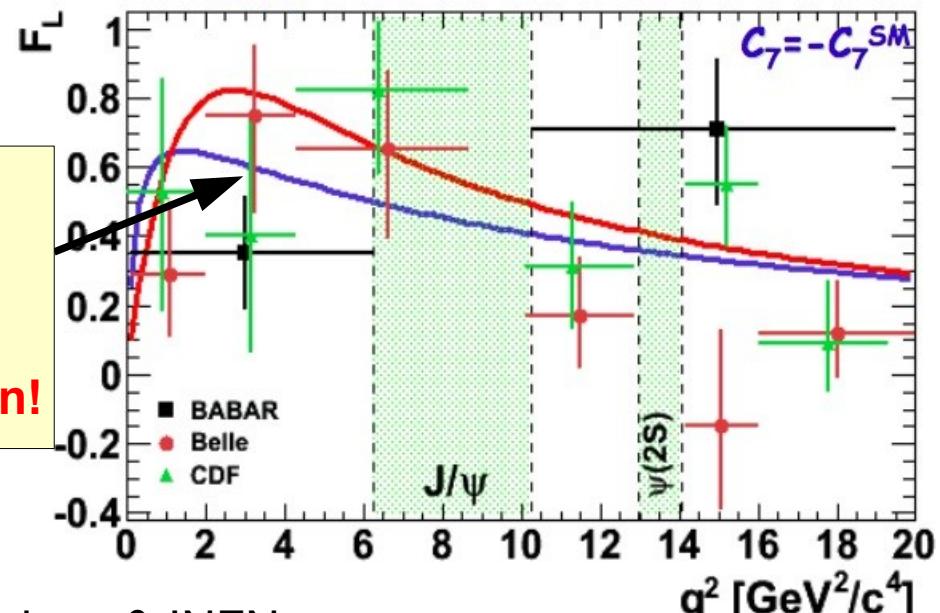
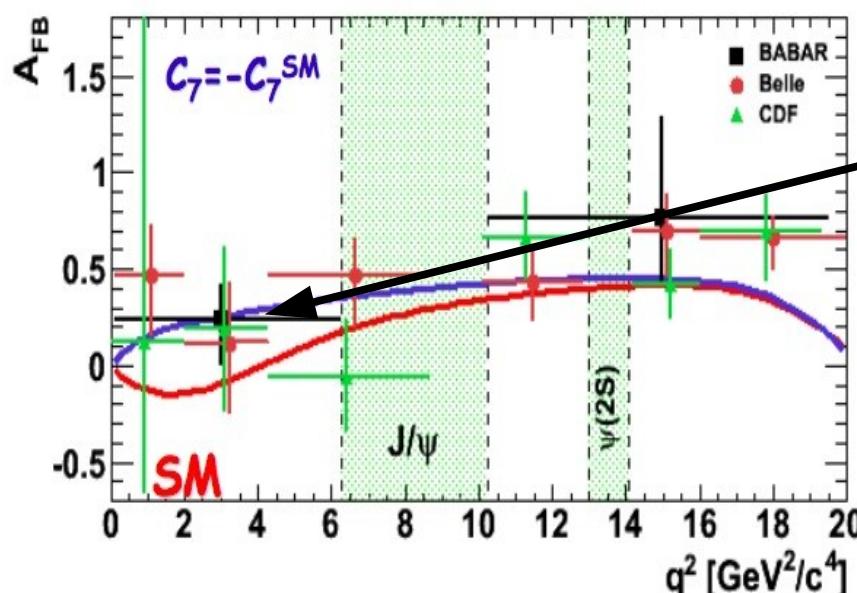
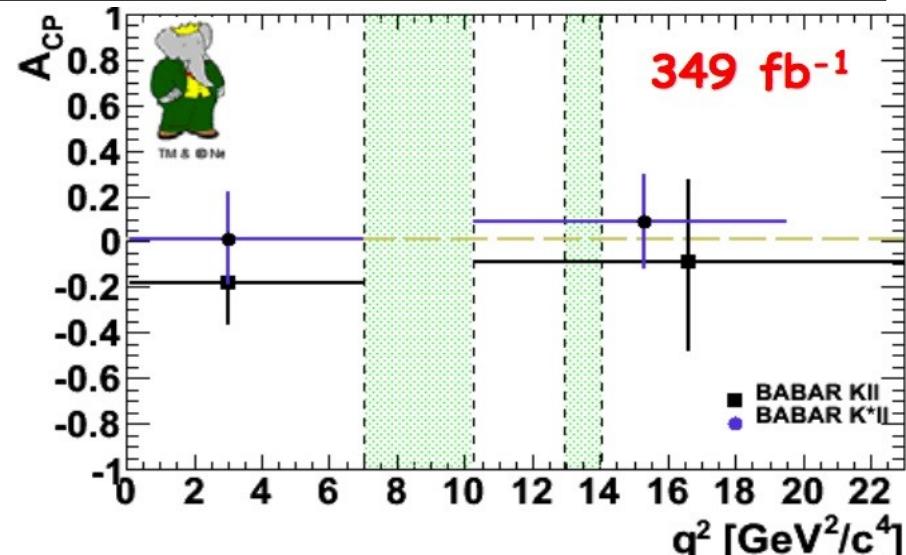
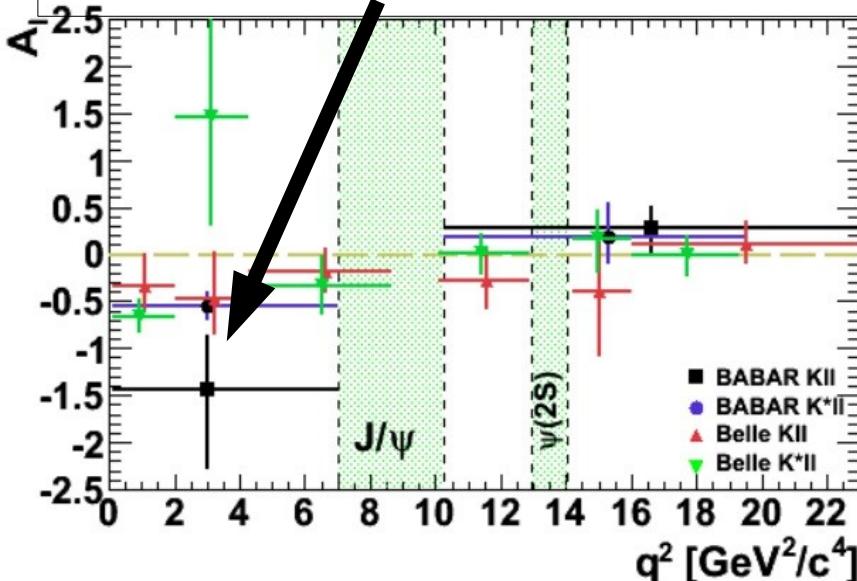
A_{FB} : first measurement in hadron collision !

Angular Analysys Systematics from:

- Fraction of $K-\pi$ swapped K^* (~7%)
- Combinatorial PDF from B-mass Side Band

$B \rightarrow X_s^- l^+ l^-$: Summary

- BaBar finds a hint of A_{ISOSPIN} deviation in the low q^2 region [PRL 102 091803]
- Belle results in agreement both with SM & BaBar [PRL 103 171801]



BaBar $B^+ \rightarrow K^+ \tau^+ \tau^-$ (423 fb $^{-1}$)

- $\text{BR}(B \rightarrow X_s l^+ l^-)$ expected to show weak dependence on lepton flavor in the high q^2 region
- $B^+ \rightarrow K^+ \tau^+ \tau^- \sim 50\%$ of total $X_s \tau^+ \tau^-$ inclusive rate
[Hewett, PRD53 4964-4969]

$$\text{BR}(B \rightarrow X_s l^+ l^-) \quad 0.6 < (q/m_b)^2 < 1$$

Electron	8.5×10^{-7}
Muon	8.5×10^{-7}
Tau	4.3×10^{-7}

- In NMSSM New Physics could couple with strength $\sim m_{\text{LEPTON}}^2$
- [Hiller, PRD70 034018]



Important Channel!

Experimentally:

Exclusive reconstruction not possible due 2-4 neutrinos in the final state

BaBar performed the first search for $B^+ \rightarrow K^+ \tau^+ \tau^-$

BaBar $B^+ \rightarrow K^+ \tau^+ \tau^-$ (423 fb $^{-1}$)

PRELIMINARY

- $K^+ \tau^+ \tau^-$ Decays searched on the recoil of fully reconstructed $B \rightarrow D^{(*)} X$
- $\varepsilon_{tag} = 0.13\%$

Main Backgrounds:

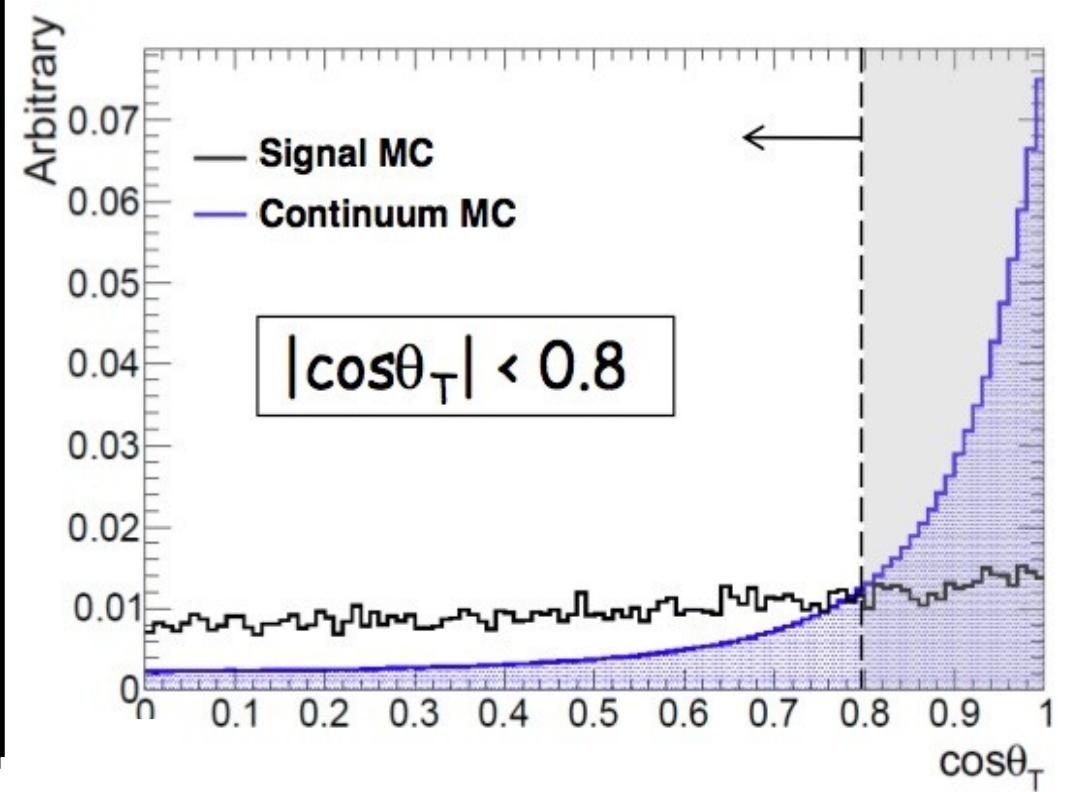
Continuum

- Suppressed exploiting the opening angle between the tag B thrust and the rest-of-event thrust

Peaking

- B semileptonic Decays Suppressed by P_{Lepton} cut
- $B \rightarrow D X$ Reduced by $m(K\pi)$ cut

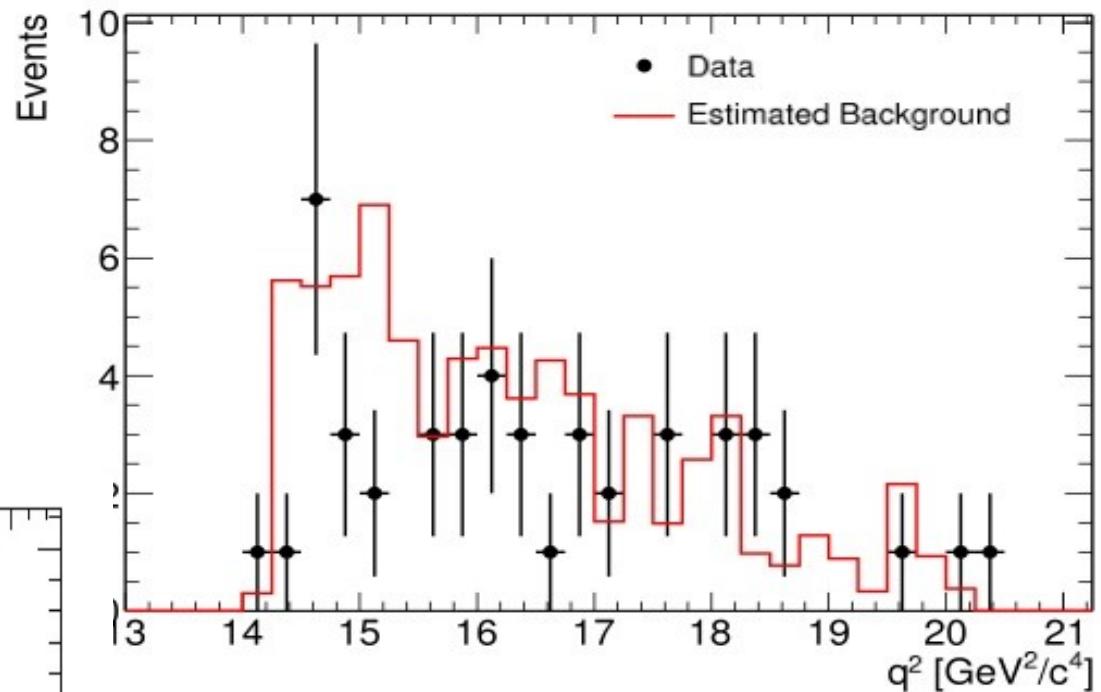
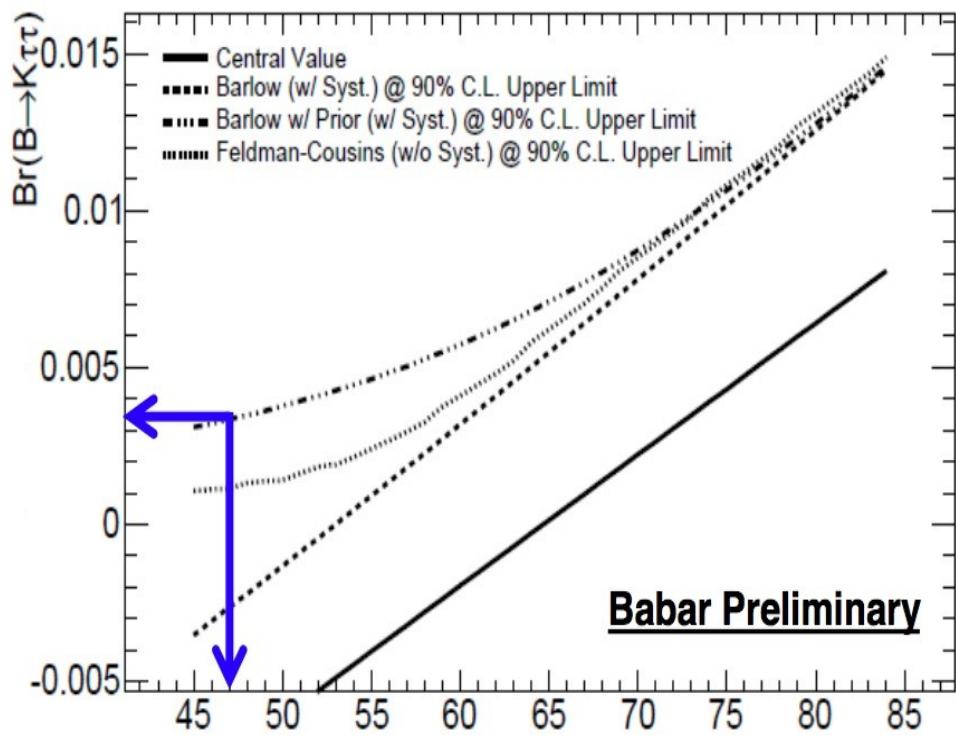
- One-prong τ decays reconstructed: $\tau \rightarrow e(\mu)vv$, τvv
- Signal events with 3 charged tracks only selected exploiting Missing Energy, $m(\tau\text{-daughters})$
- Veto applied to remove J/Ψ



BaBar $B^+ \rightarrow K^+ \tau^+ \tau^-$ (423 fb $^{-1}$)

- Systematics from ϵ_{SIGNAL} ,
Background shape & yield, ϵ_{TAG}

**47 events observed
(65 expected from BKG)**



- Upper Limit obtained using Barlow method [Comput. Phys. Commun. 149, 97] with prior assuming the model of Ali et al. [PRD66 034002]
- Conservative Approach!

BR($B^+ \rightarrow K^+ \tau^+ \tau^-$) < 3.3×10^{-3} @ 90%CL

$$B \rightarrow X_d^- l^+ l^-$$

No Inclusive Analyses performed. Experiments Fully reconstruct $B \rightarrow \pi l^+ l^-$

Main Backgrounds:

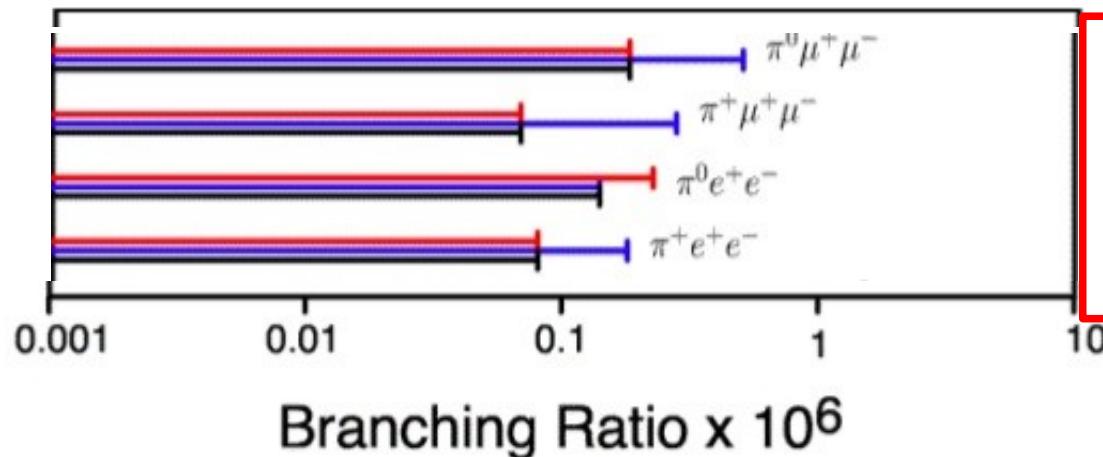
- Continuum reduced exploiting event shape variables & B-flavor tagging

Belle (605 fb⁻¹) [PRD 78 011101R]

$$\text{BR}(B \rightarrow \pi l^+ l^-) < 6.2 \times 10^{-8}$$

BaBar (209 fb⁻¹) [PRL 99 051801]

$$\text{BR}(B \rightarrow \pi l^+ l^-) < 9.1 \times 10^{-8}$$



Hfag 2010:

$$\text{BR}(B \rightarrow \pi l^+ l^-) < 6.2 \times 10^{-8}$$

Conclusion

Radiative penguin decays are an excellent laboratory for the search for physics beyond the SM & the study of b-quark dynamics

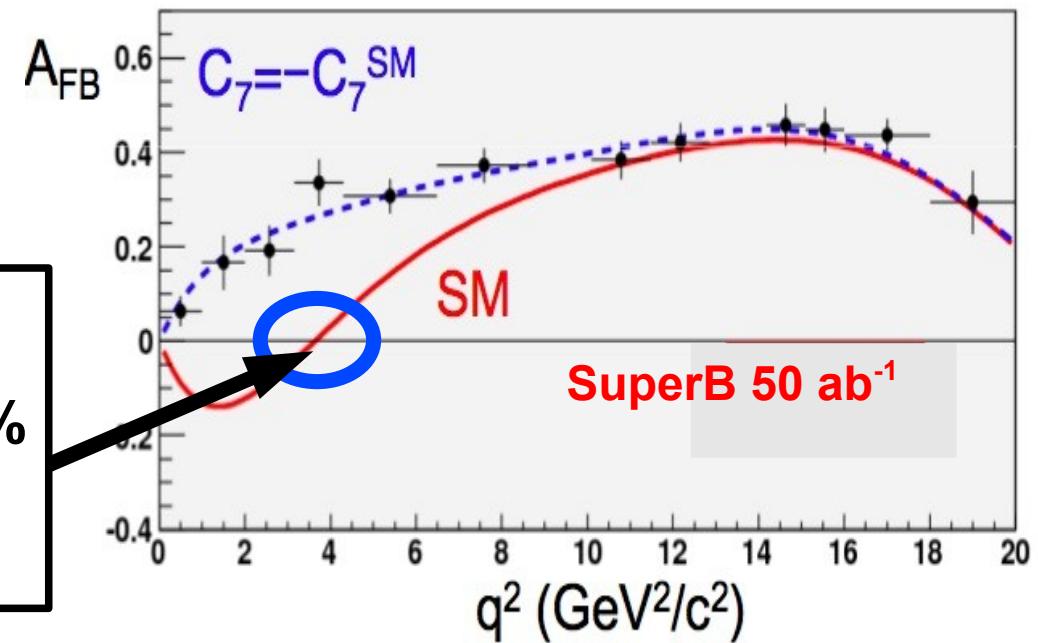
Almost all results in agreement with expectations

In the Future they will offer Opportunity to:

- Improve Experimental Technics by using New Observables with reduced dependence on Form Factors (e.g. Transversity Amplitudes)
[Bobeth et al., arXiv:1006.5013]

$A_{FB}(q^2_0)=0$
 $\text{SuperBelle}(50\text{ab}^{-1}) \delta q^2_0 \sim 5\%$
 $\text{LHCb}(2\text{fb}^{-1}): \delta q^2_0 \sim 13\%$

- Provide very stringent SM tests:



- Discover/Understand New Physics

Backup

Extract $X=|V_{td}/V_{ts}|$ from Ratio of Inclusive BFs

- Use NLO calculation [Ali et al., Phys. Lett. B429 87]

$$R = \lambda^2[1 + \lambda^2(1 - 2\bar{\rho})] \left[(1 - \bar{\rho})^2 + \bar{\eta}^2 + \frac{D_u}{D_t}(\bar{\rho}^2 + \bar{\eta}^2) + \frac{D_r}{D_t}(\bar{\rho}(1 - \bar{\rho}) - \bar{\eta}^2) \right]$$

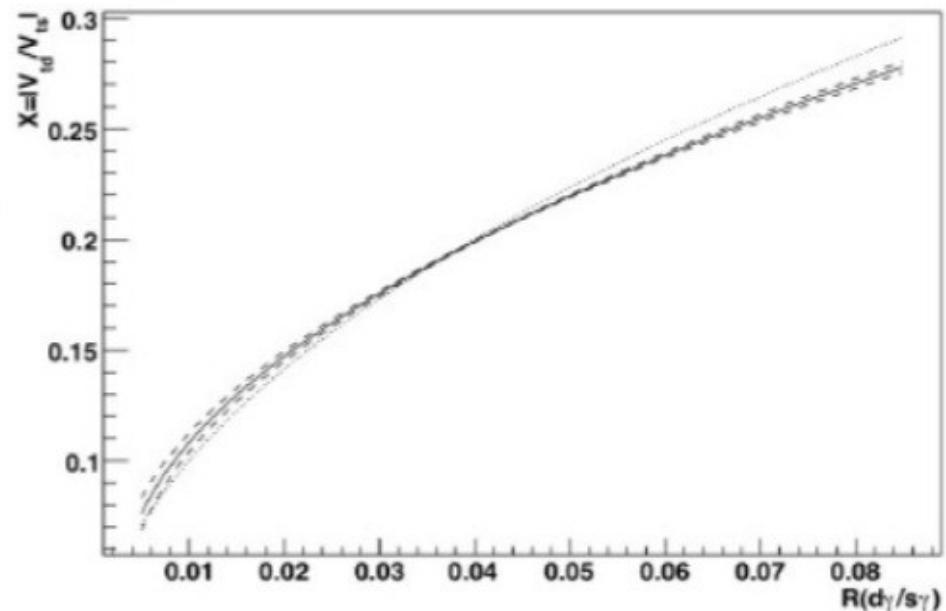
- Rewrite in terms of X and UT angle β

$$R = \kappa_1 X^2 + \kappa_2 X + \kappa_3,$$

$$\kappa_1 = 1 + \frac{D_u}{D_t} (1 - 2\lambda^2 \cos^2 \beta) - \frac{D_r}{D_t} (\lambda^2 \cos^2 \beta + 1),$$

$$\kappa_2 = \lambda \cos \beta \left[\frac{D_u}{D_t} (3\lambda^2 - 2) + \frac{D_r}{D_t} \left(1 + \frac{\lambda^2}{2} \right) \right],$$

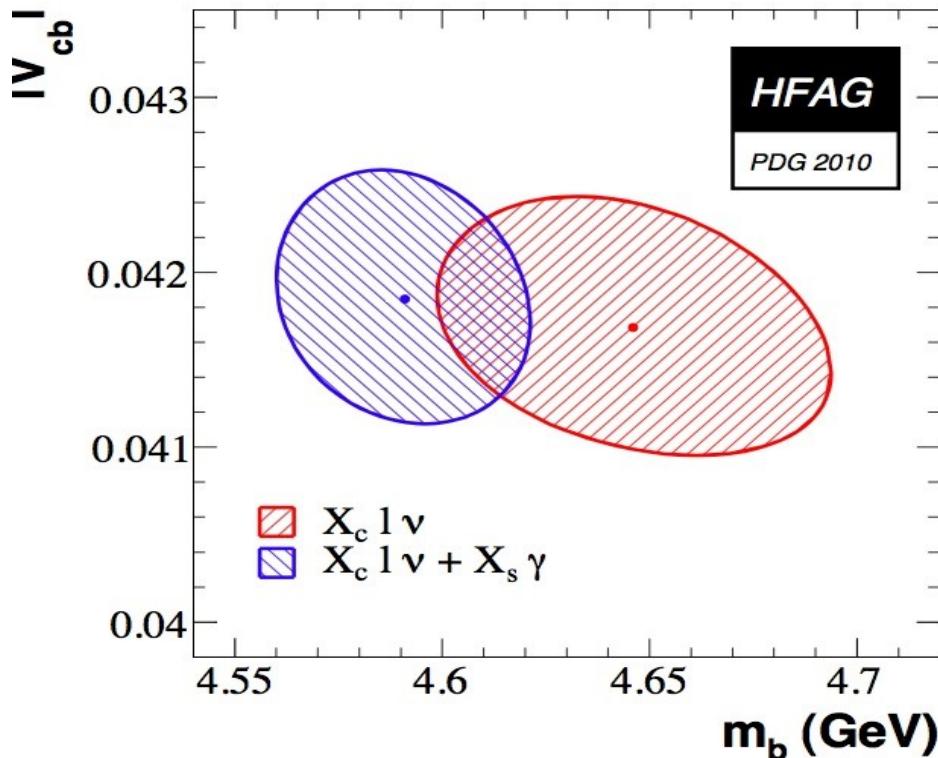
$$\kappa_3 = \lambda^2 \frac{D_u}{D_t} (1 - \lambda^2).$$



- Uncertainties from PDG & numerical calculation of D factors

B \rightarrow s γ Spectral Moments

HFAG Fit in Kinetic Mass Scheme (2010)



$|V_{ub}|$ From Inclusive BR in different Theoretical Frameworks using $X_s \gamma$ Moments [HFAG2010]

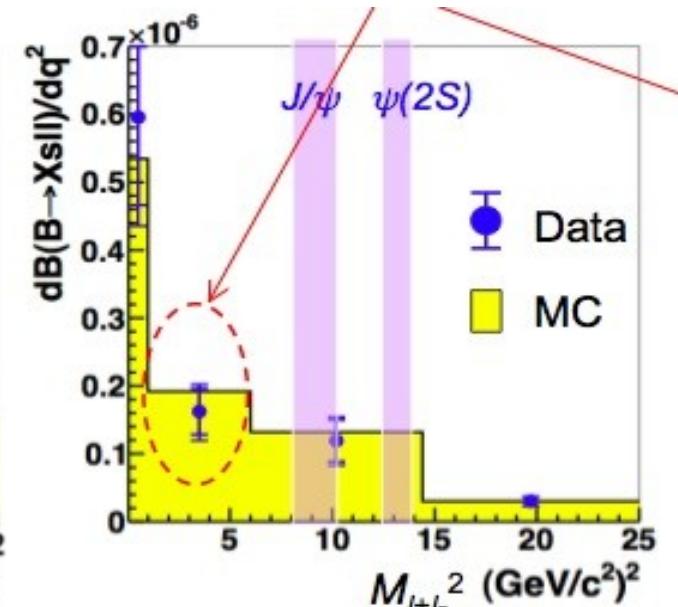
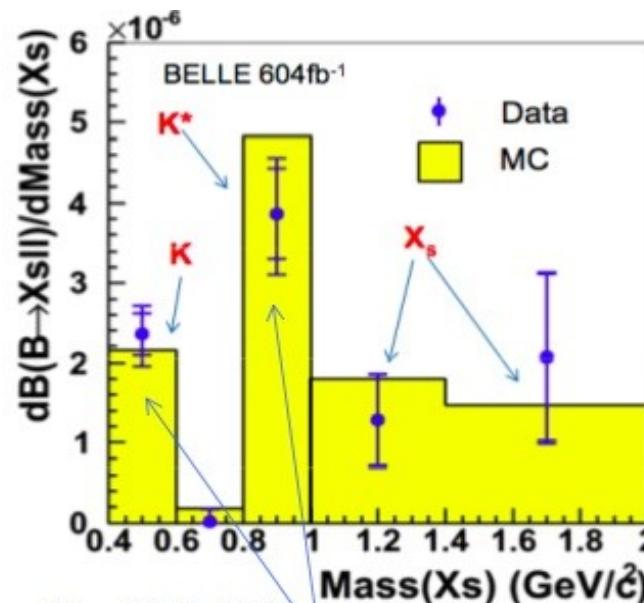
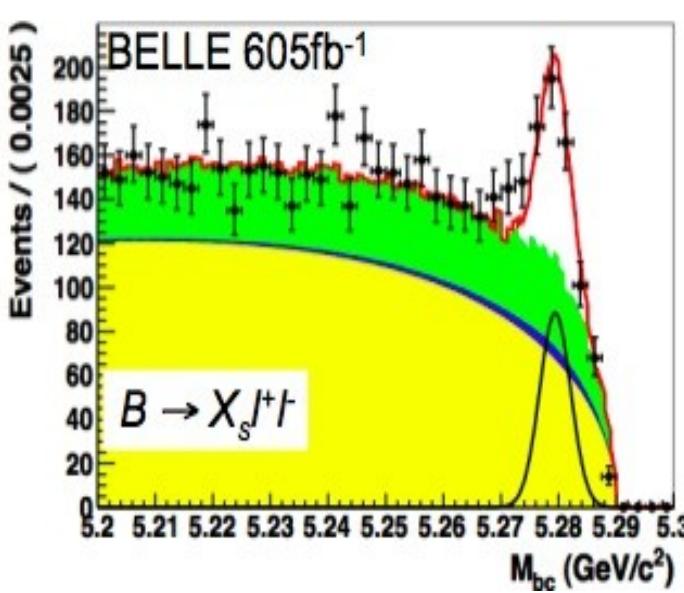
Framework	$ V_{ub} [10^{-3}]$
BLNP	$4.32 \pm 0.16^{+0.22}_{-0.23}$
DGE	$4.46 \pm 0.16^{+0.18}_{-0.17}$
GGOU	$4.34 \pm 0.16^{+0.15}_{-0.22}$
ADFR	$4.16 \pm 0.14^{+0.25}_{-0.22}$
BLL (m_X/q^2 only)	$4.87 \pm 0.24 \pm 0.38$
LLR (BABAR) [394]	$4.43 \pm 0.45 \pm 0.29$
LLR (BABAR) [395]	$4.28 \pm 0.29 \pm 0.29 \pm 0.26 \pm 0.28$
LNP (BABAR) [395]	$4.40 \pm 0.30 \pm 0.41 \pm 0.23$

Data	χ^2/dof	$ V_{cb} (10^{-3})$	$m_b^{\text{kin}}(\text{GeV})$	$\mu_\pi^2(\text{GeV}^2)$
All moments ($X_c \ell \nu_\ell$ and $X_s \gamma$)	$29.7/(66 - 7)$	41.85 ± 0.73	4.591 ± 0.031	0.454 ± 0.038
$X_c \ell \nu_\ell$ only	$24.2/(55 - 7)$	41.68 ± 0.74	4.646 ± 0.047	0.439 ± 0.042

Belle $B \rightarrow X_s l^+ l^-$ (605 fb $^{-1}$) PRELIMINARY

Improved Analysis, sum up 36 exclusive modes (~80% coverage)

- Continuum Suppressed by event shape variables
- Cascades $b \rightarrow c \rightarrow s/d$ rejected exploiting missing mass & energy



Mode	Yield	$\text{BF} (\times 10^{-6})$	Σ
$B \rightarrow X_s e^+ e^-$	$121.6 \pm 19.3(\text{stat.}) \pm 2.0(\text{syst.})$	$4.56 \pm 1.15(\text{stat.})^{+0.33}_{-0.40}(\text{syst.})$	7.0
$B \rightarrow X_s \mu^+ \mu^-$	$118.5 \pm 17.3(\text{stat.}) \pm 1.5(\text{syst.})$	$1.91 \pm 1.02(\text{stat.})^{+0.16}_{-0.18}(\text{syst.})$	7.9
$B \rightarrow X_s l^+ l^-$	$238.3 \pm 26.4(\text{stat.}) \pm 2.3(\text{syst.})$	$3.33 \pm 0.80(\text{stat.})^{+0.19}_{-0.24}(\text{syst.})$	10.1

ps: $\text{BF}(X_s e^+ e^-) / \text{BF}(X_s \mu^+ \mu^-) = 2.39 \pm 1.41$

In agreement with SM

Transversity Amplitudes

[Bobeth et al., arXiv:1006.5013]

- HQET Calculations Give possibility to disentangle QCD Effects from possible New Physics Effects at high $q^2 = m_{l^\pm}^{-2}$ in $B \rightarrow K^* l^+ l^-$ angular analyses
- New Observables defined with **do not depend on FF** at low recoil and cleanly test SM:

$$H_T^{(1)} = \frac{\text{Re}(A_0^L A_{\parallel}^{L*} + A_0^{R*} A_{\parallel}^R)}{\sqrt{(|A_0^L|^2 + |A_0^R|^2)(|A_{\parallel}^L|^2 + |A_{\parallel}^R|^2)}}$$

$$H_T^{(2)} = \frac{\text{Re}(A_0^L A_{\perp}^{L*} - A_0^{R*} A_{\perp}^R)}{\sqrt{(|A_0^L|^2 + |A_0^R|^2)(|A_{\perp}^L|^2 + |A_{\perp}^R|^2)}}$$

$$H_T^{(3)} = \frac{\text{Re}(A_{\parallel}^L A_{\perp}^{L*} - A_{\parallel}^{R*} A_{\perp}^R)}{\sqrt{(|A_{\parallel}^L|^2 + |A_{\parallel}^R|^2)(|A_{\perp}^L|^2 + |A_{\perp}^R|^2)}}$$

Computed in terms of left & right Transversity Amplitudes:

$$A_{\perp}^{L,R} = +i \left\{ (\mathcal{C}_9^{\text{eff}} \mp \mathcal{C}_{10}) + \kappa \frac{2\hat{m}_b}{\hat{s}} \mathcal{C}_7^{\text{eff}} \right\} f_{\perp},$$

$$A_{\parallel}^{L,R} = -i \left\{ (\mathcal{C}_9^{\text{eff}} \mp \mathcal{C}_{10}) + \kappa \frac{2\hat{m}_b}{\hat{s}} \mathcal{C}_7^{\text{eff}} \right\} f_{\parallel},$$

$$A_0^{L,R} = -i \left\{ (\mathcal{C}_9^{\text{eff}} \mp \mathcal{C}_{10}) + \kappa \frac{2\hat{m}_b}{\hat{s}} \mathcal{C}_7^{\text{eff}} \right\} f_0,$$

Form Factors

- Other Observables which do not depend on Wilson Coefficients at low recoil probe some $B \rightarrow K^*$ FF combinations